

*The State of the Art and Science of Coastal Engineering*

# Consideration of Storm Surge Caused by Hurricane Irma Based on STOC-WRF Coupling Model

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# 1. Introduction



There was serious damage at Caribbean Islands because of the storm surge and rain fall caused by Hurricane Irma.



British Virgin Islands  
(Above : Before, Below : After )  
REFERENCE : AccuWeather



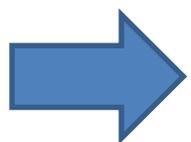
To estimate storm surge, it is necessary to evaluate the wind and atmospheric pressure.



# 1. Introduction



	<b>Empirical Atmospheric pressure model</b>	<b>Provided data by Metrological Agency (GPV)</b>	<b>Mesoscale Weather model (WRF)</b>
<b>Cost</b>	○	×	△
<b>Resolution</b>	Optional setting	×	Optional setting
<b>Accuracy</b>	×	○	○



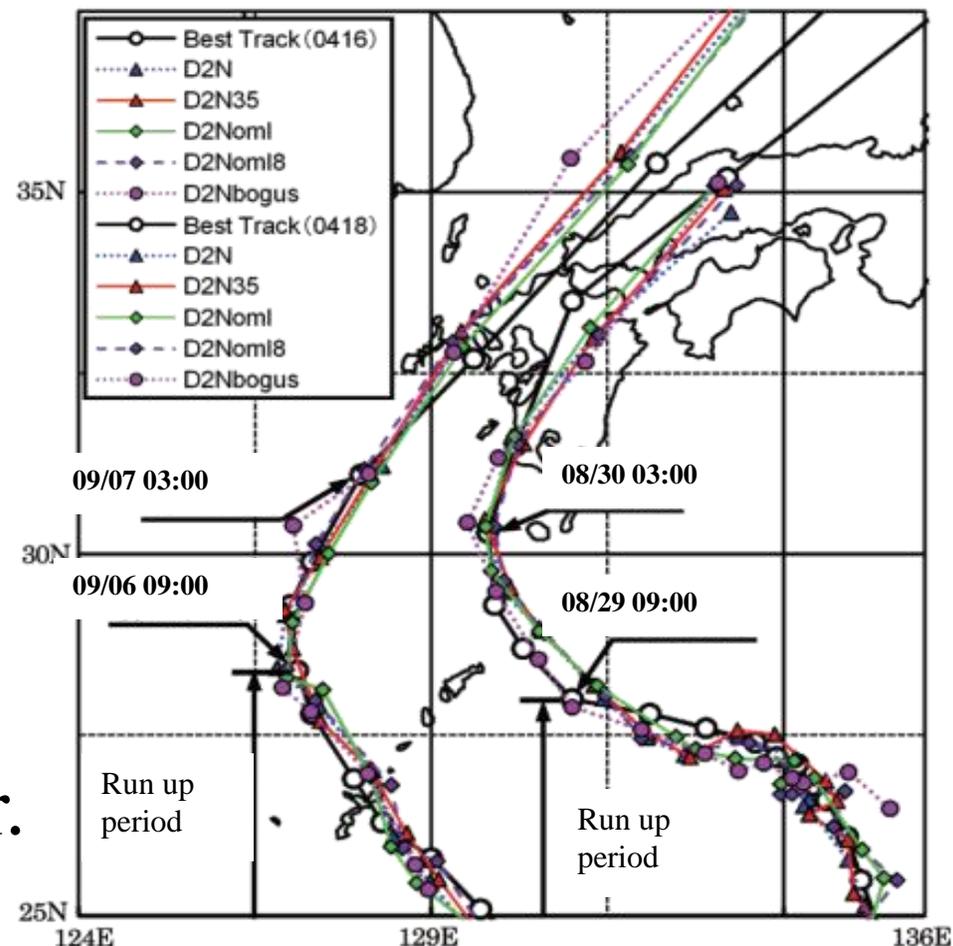
Mesoscale weather model is high accuracy, however there are a lot of choices in numerical conditions (grid size, physics model, and boundary condition, etc.) .

# 1. Introduction

## Previous research

Suzuyama *et al.* (2011) : Study of some characteristics of WRF calculation

- Domain size (moving nests)...700 to 1000km including typhoon margin
- Ocean mixed layer  $\Rightarrow$  maximum wind speed
- Thompson model (Micro physics)  
 $\Rightarrow$  underestimation can be suppressed



It is said WRF still depends on the experience of the model user.



# 1. Introduction

## Previous researches on hurricane and typhoon by WRF

Author	Target	mp	bl_pbl	cu	ra_sw	ra_lw
Suzuyama <i>et al.</i> (2012)	T5115	Thompson	YSU	Kain-Fritsch	Old Goddard	RRTM
Tanemoto <i>et al.</i> (2012)	Typhoon (10 years)	Eta	MYJ	Kain-Fritsch	Dudhia	RRTM
Ninomiya <i>et al.</i> (2012)	T0918	WSM6	MYJ	Kain-Fritsch	Dudhia	RRTM
Nakamura <i>et al.</i> (2016)	T1115	WSM6	YSU	-	RRTMG	RRTMG
Ninomiya <i>et al.</i> (2015)	T5915	WSM6	YSU	Kain-Fritsch	RRTMG	RRTMG
Shigeta <i>et al.</i> (2014)	T0416, T0418	WSM6	MYJ	Kain-Fritsch	RRTM	RRTM

mp : Micro Physics, bl\_pbl :Planetary Boundary Layer Physics, cu : Cumulus Parameterization, ra\_sw and ra\_lw : Shortwave and Longwave Radiation



# 1. Introduction

In this study...

- ✓ Evaluate **the impact of different model conditions** on the reproducibility, performance
- ✓ Estimate storm tide using storm surge prediction model and wave prediction model **by applying meteorological fields calculated by mesoscale model (verification of WRF to STOC, SWAN)**



# 1. Introduction – Numerical Model

WRF<sup>1)</sup>(Weather Research and Forecasting model)

➔ 3 dimensional fully compressible non-hydrostatic model

STOC-ML<sup>2)</sup>(Storm surge and Tsunami simulator  
in Oceans and Coastal areas)

➔ Quasi 3 dimensional model using hydrostatic approximation in z direction

SWAN<sup>3)</sup>(Simulating WAVes Nearshore)

➔ Calculate wave propagation in time and space based on spectral action Balance equation

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<sup>1)</sup>Skamarock *et al.* (2008) : A Description of the Advanced Research WRF Version3

<sup>2)</sup>Tomita *et al.* (2005) : Development of numerical simulator of seawater flow and Application to Tsunami Analysis

<sup>3)</sup>Ris *et al.* (1999) : A third-generation wave model for coastal regions: Part 2. Verification

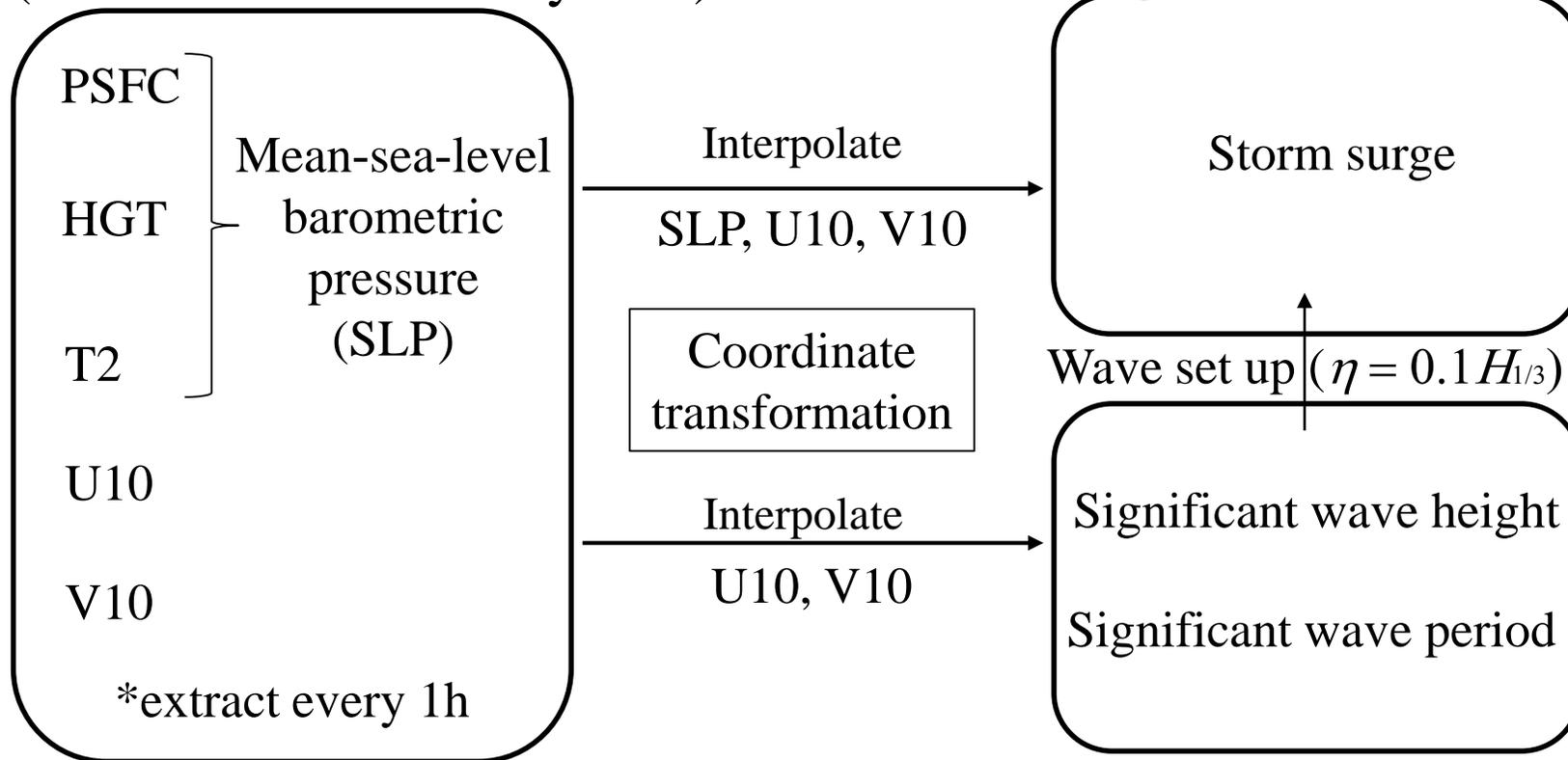


# 2. Application Method

## How to apply WRF to STOC and SWAN

WRF(Lat-Lon coordinate system)

STOC(Orthogonal coordinate system)



SWAN(Orthogonal coordinate system)

\*PSFC: Surface pressure  
HGT: Terrain Height  
T2: Temperature at 2m  
U10, V10: 10m-elevation wind speed

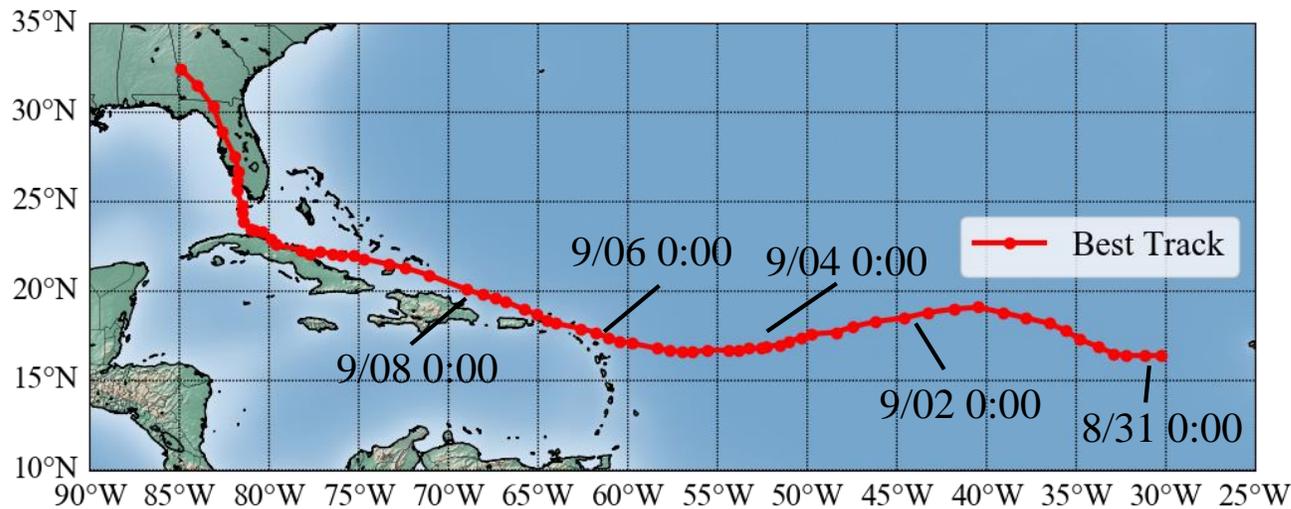


# 3. Consideration of WRF

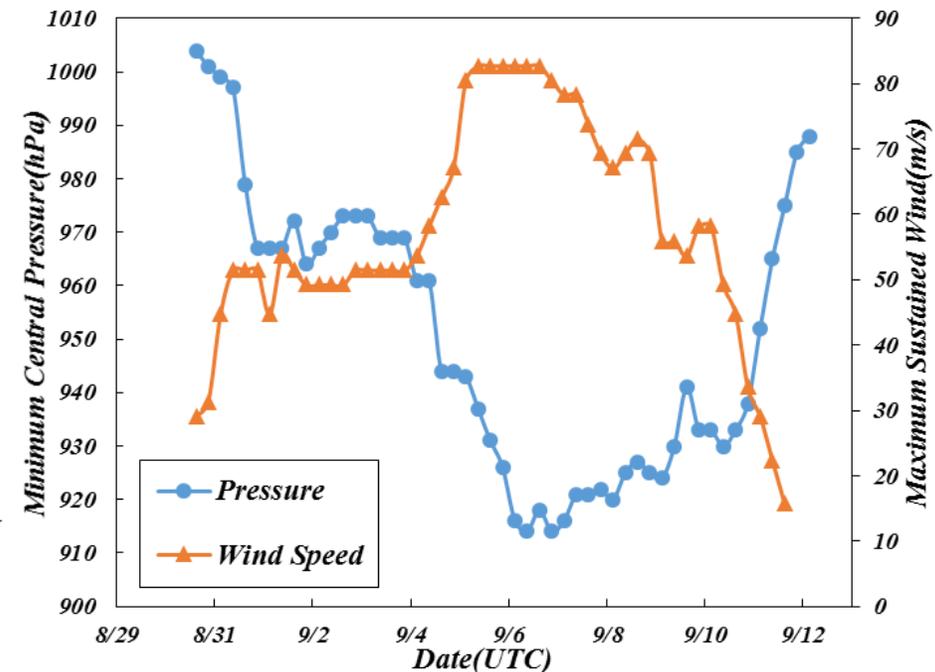
## Overview of Hurricane Irma

### Basic Information

Formed Date	August 30, 2017, at 3:00 p.m. (UTC)
Dissipated Date	September 12, 2017, at 3:00 a.m. (UTC)
Minimum Central Pressure	914 (hPa)
Maximum Sustained Wind	82 (m/s)

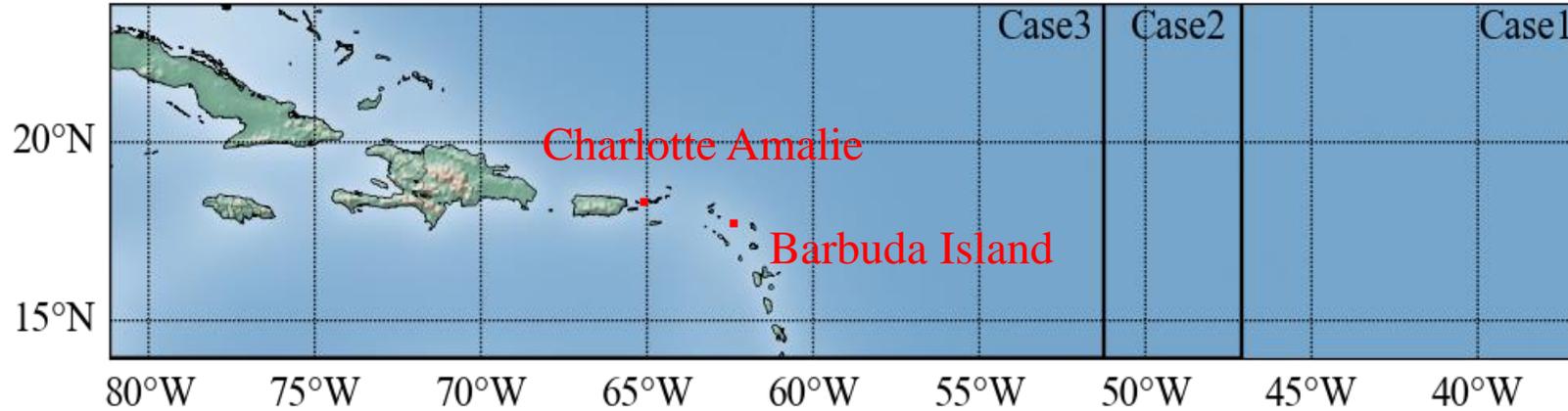


REFERENCE : NOAA



# 3. Consideration of WRF

WRF



Physics	Scheme
Microphysics(mp)	Thompson (2008)
Longwave Radiation(ra_lw)	RRTMG (2008)
Shortwave Radiation(ra_sw)	RRTMG (2008)
Planetary Boundary Layer(bl_pbl)	Mellor-Yamada-Janjic (1994)
Cumulus Parameterization(cu)	New Simplified Arakawa-Schubert (2011)
Surface Layer(sf_sfclay)	Eta Similarity (2002)
Land Surface(sf_surface)	Unified Noah (2004)

Input and nudging data is NCEP  $0.25 \times 0.25$  provided from July 2015.



# 3. Consideration of WRF

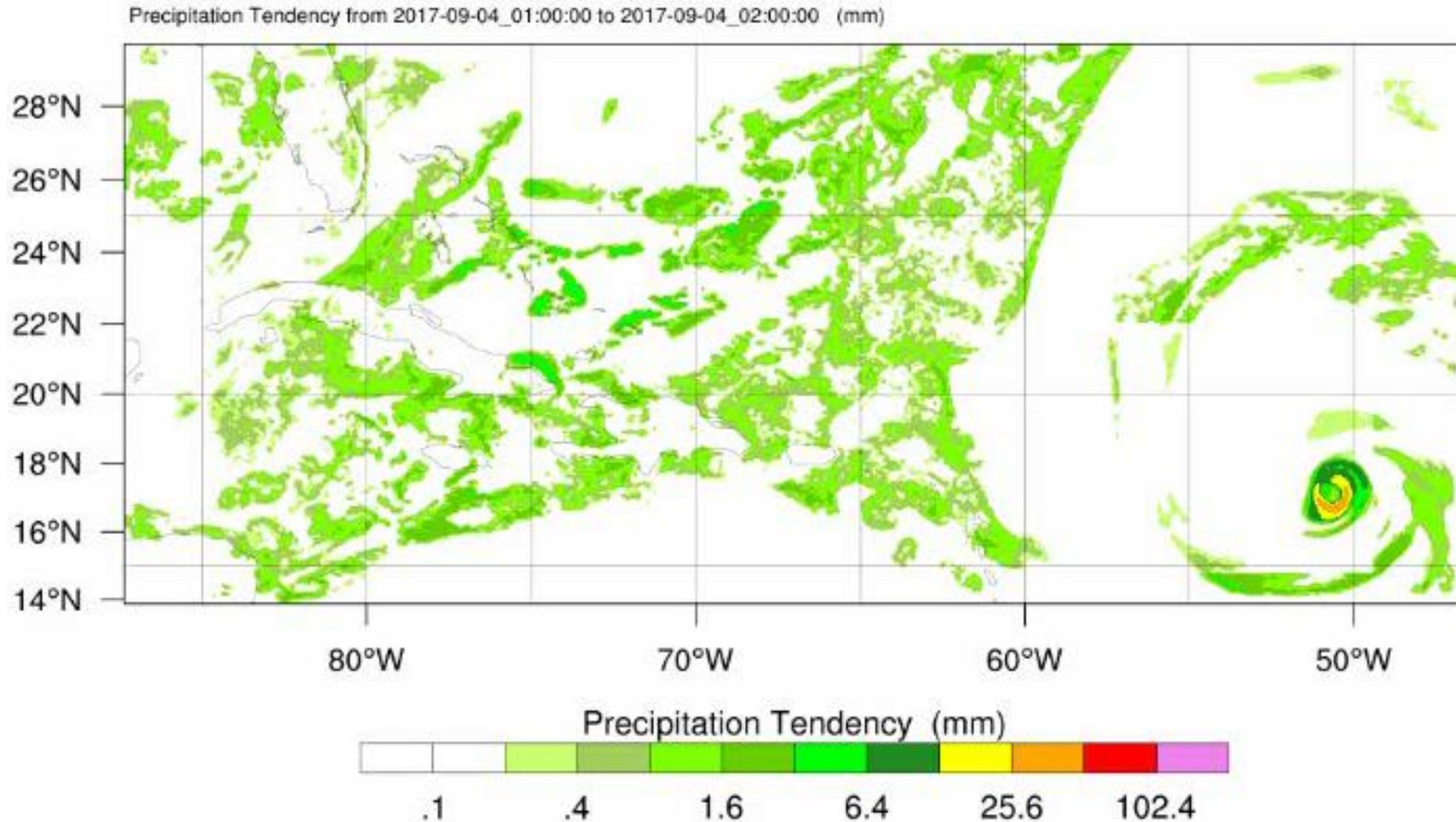
## Model condition

\*D.A. : Data assimilation

Case	Nesting	D.A.*	Cumulus Parameterization	Calculation Period
Case1	Moving Nest (Vortex following)	No D.A.	New Simplified Arakawa-Schubert	02/Sep./2017 ~ 09/Sep./2017
Case2				04/Sep./2017 ~ 09/Sep./2017
Case3				05/Sep./2017 ~ 09/Sep./2017
Case2-nonest	No Nesting			
Case2-Cu_0	Moving Nest (Vortex following)		No Option (for D2)	
Case2-O		Obs. Nudging	New Simplified Arakawa-Schubert	04/Sep./2017 ~ 09/Sep./2017  Base case <ul style="list-style-type: none"> <li>▪ Nesting</li> <li>▪ D.A.</li> <li>▪ Cumulus Parameterization</li> </ul>
Case2-G		Grid Nudging		
Case2-G-Air				
Case2-S600				
Case2-S2000	Spectral Nudging			

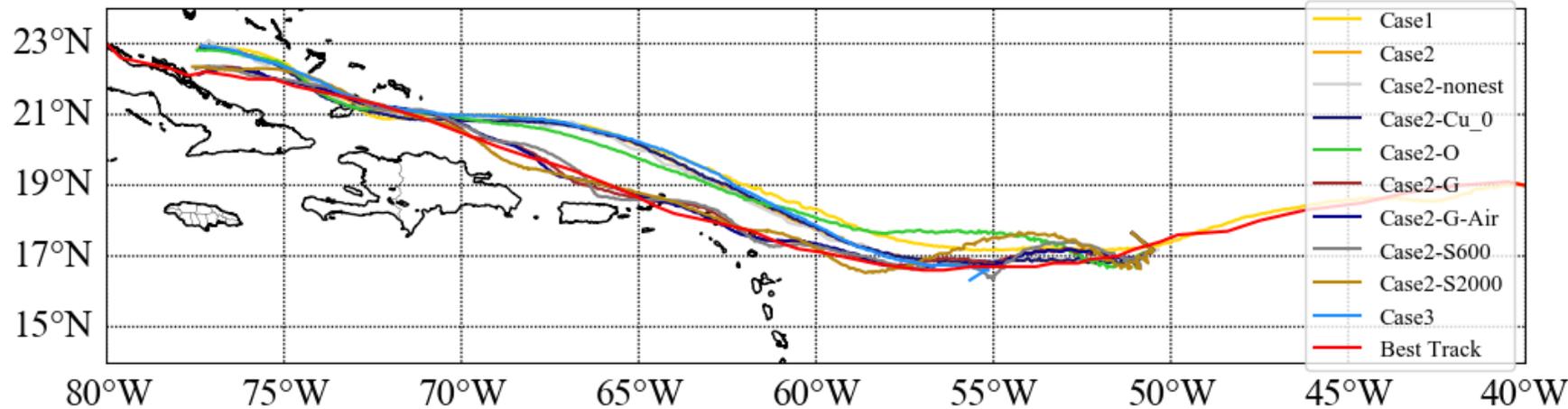
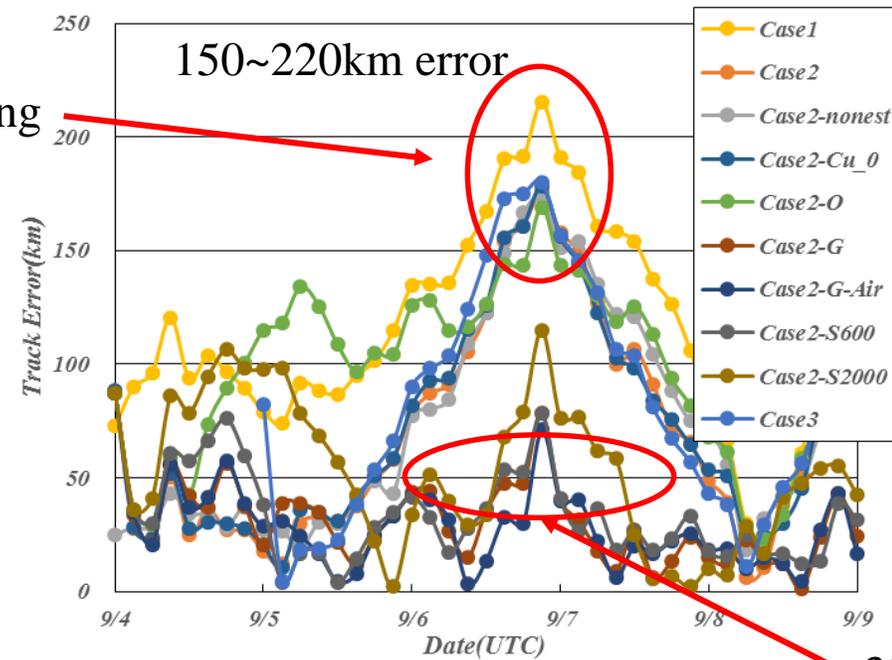
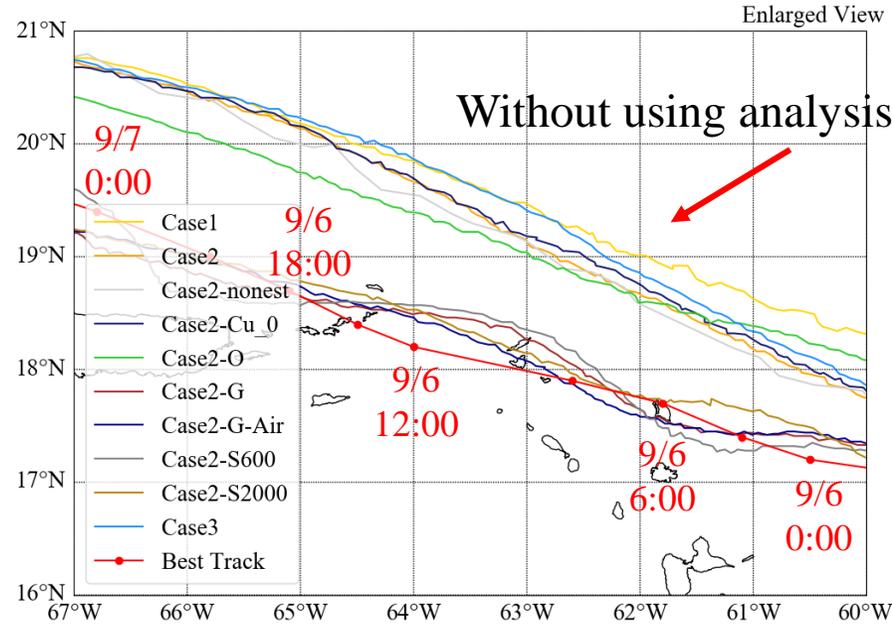
# 3. Consideration of WRF

## Precipitation Tendency (mm/h)



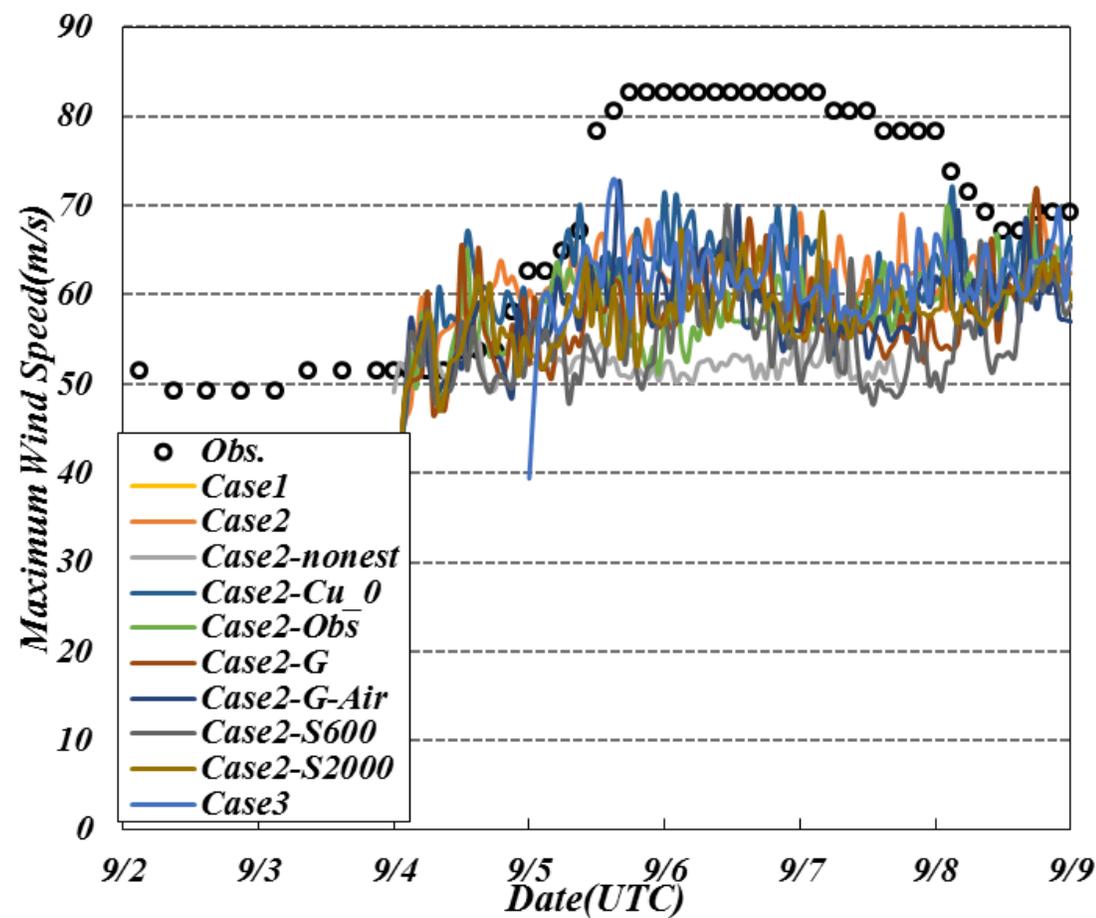
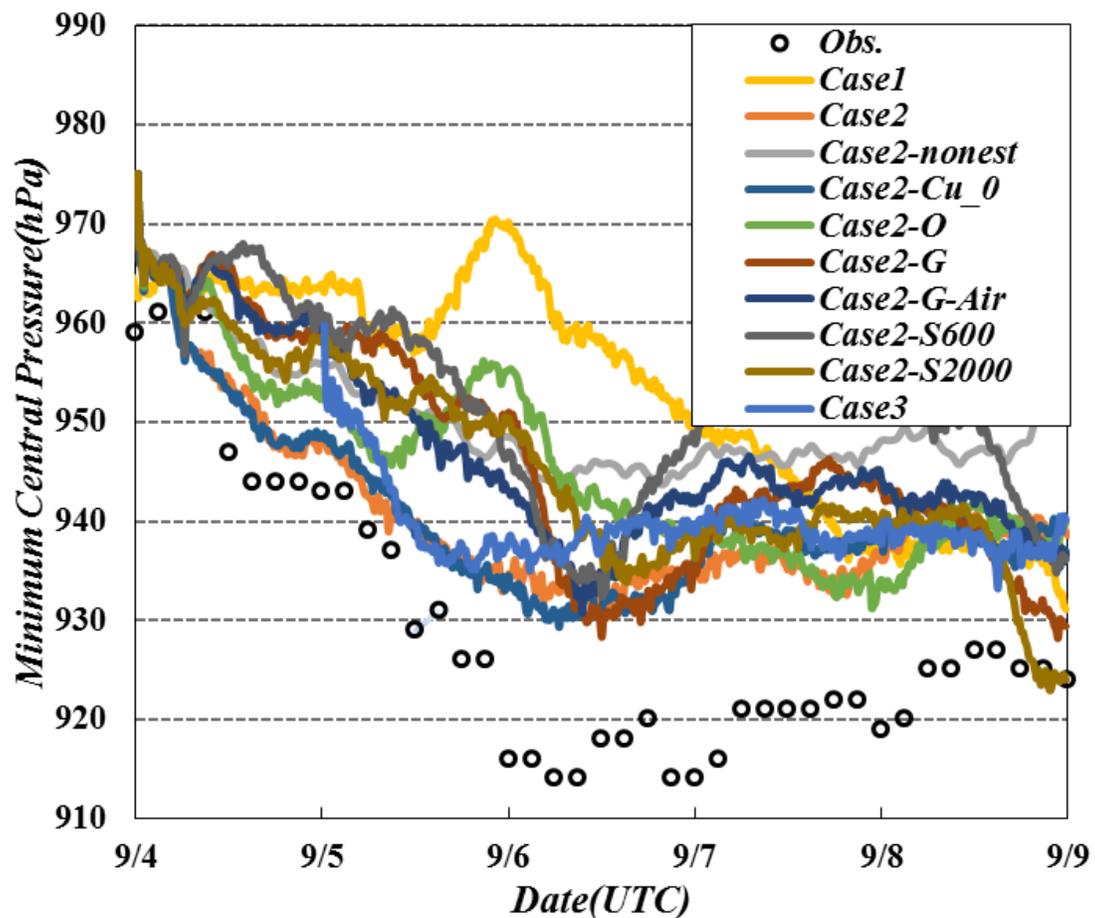
# 3. Consideration of WRF

## Comparison of track



# 3. Consideration of WRF

## Comparison of the intensity



# 3. Consideration of WRF

## Mean Error

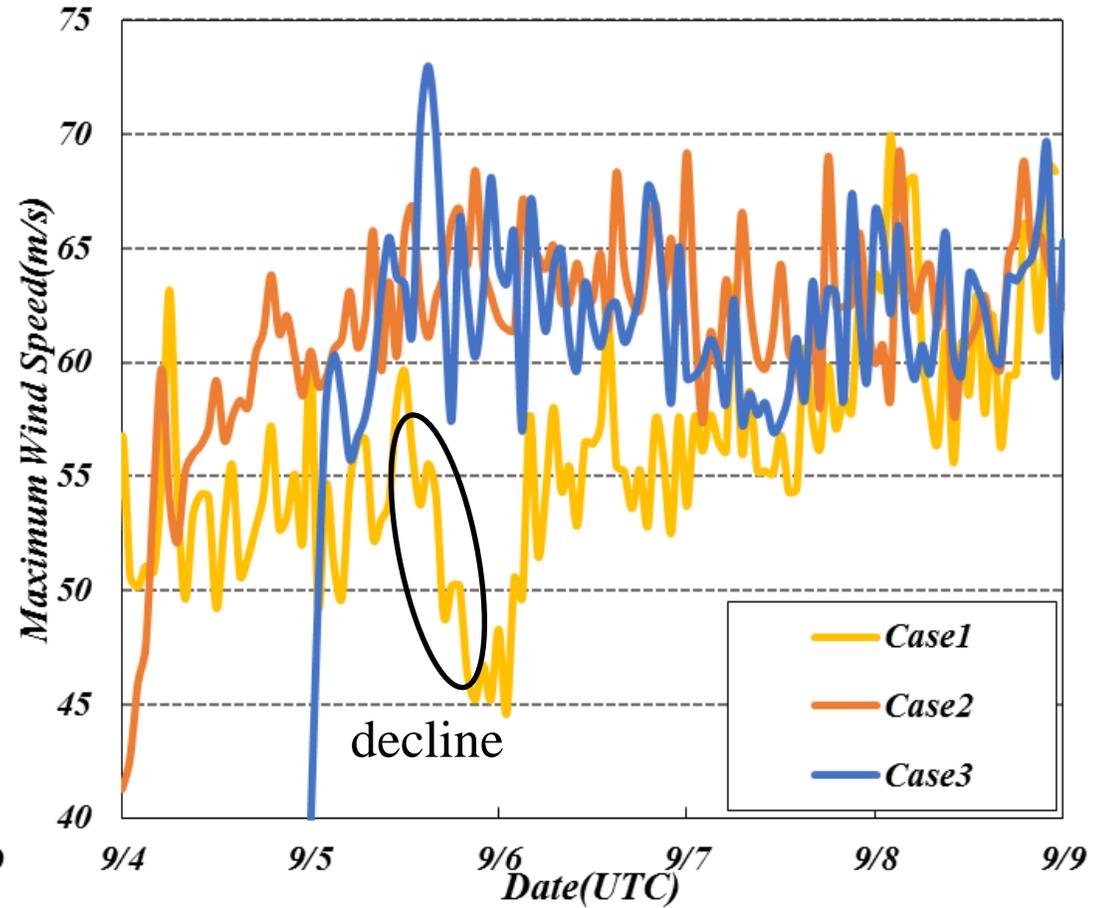
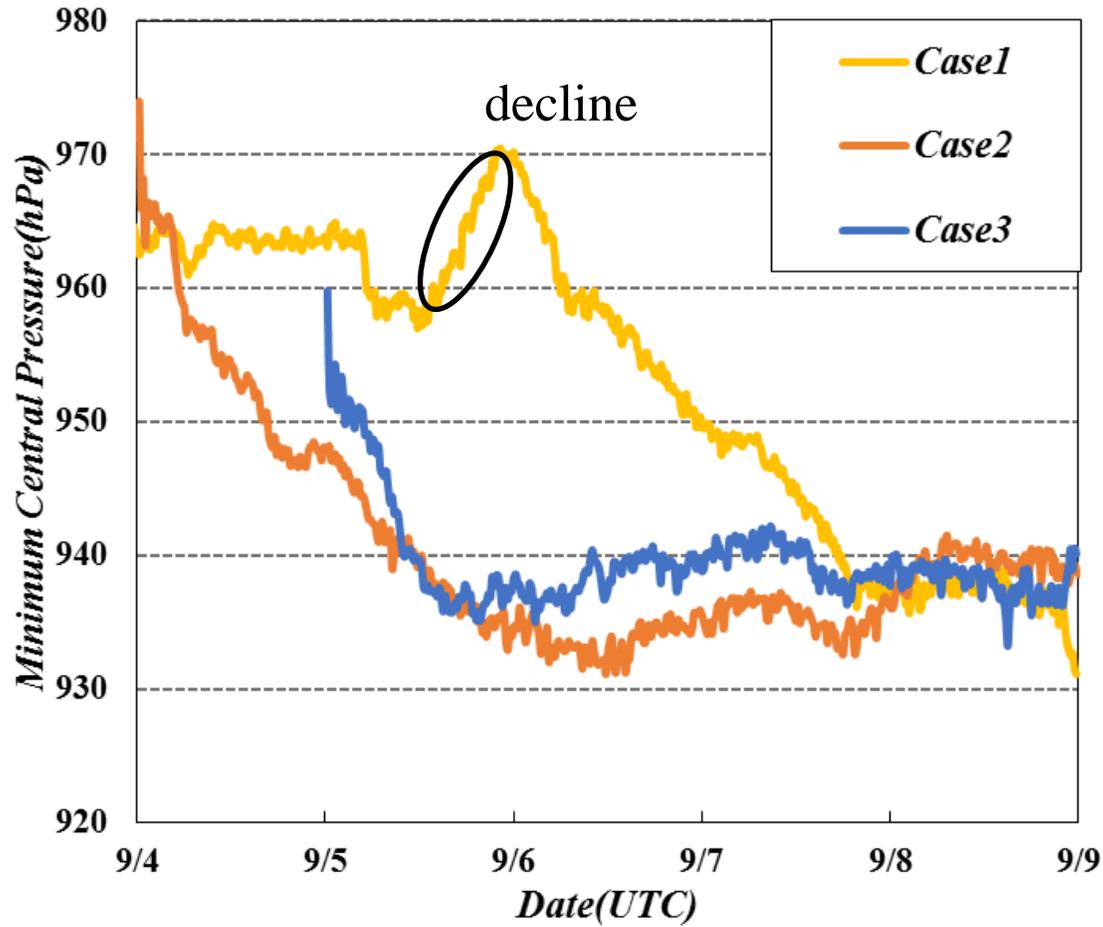
$$ME = \sum(F(i) - A(i)) \div N, \text{ F:Calculation, A:Observation}$$

Case	Location(km)	Pressure(hPa)	Wind Speed(m/s)
Case1	112.395	19.913	-13.205
Case2	69.890	11.783	-10.007
Case2-nonest	71.909	21.583	-20.577
Case2-Cu_0	71.172 40km	11.800 6hPa	-10.623 3m/s
Case2-O	96.252	16.480	-13.704
Case2-G	30.983	17.558	-13.416
Case2-G-Air	28.524	18.288	-14.554
Case2-S600	33.786 20km	23.195 1hPa	-16.560 0.4m/s
Case2-S2000	52.758	16.325	-13.837
Case3	82.672	16.377	-14.712

\*Blue : apply to STOC and SWAN

# 3. Consideration of WRF

Starting date of calculate



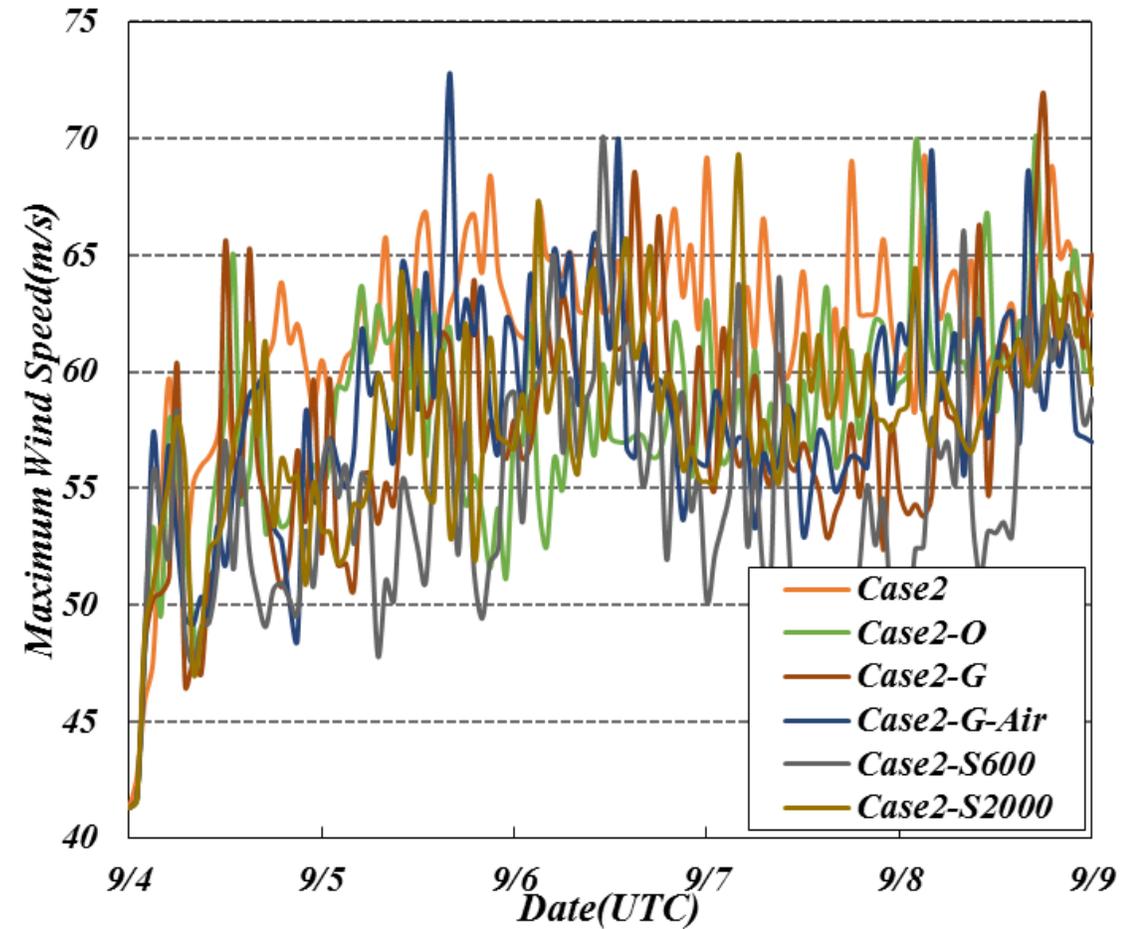
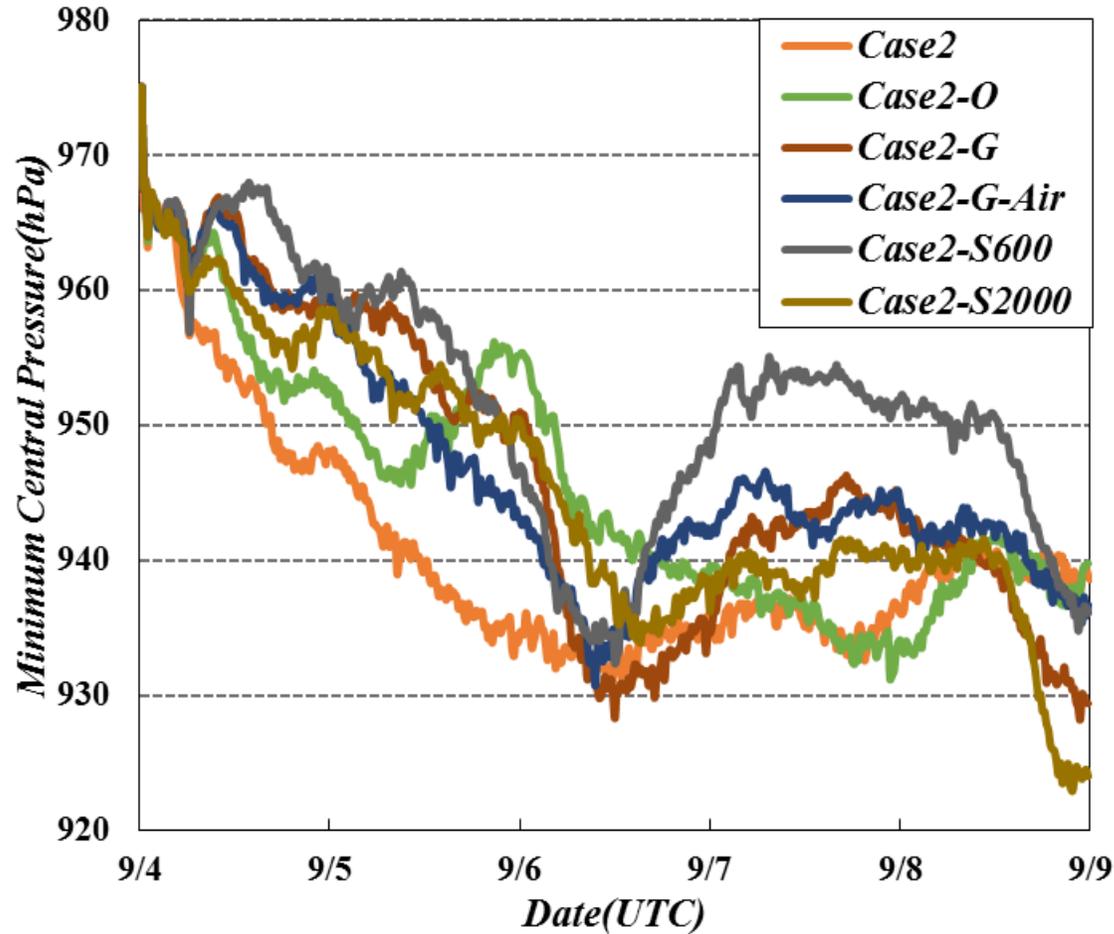
Case2 is most reproduced the strength

└─ Start calculation when we confirm the eye of Hurricane Irma



# 3. Consideration of WRF

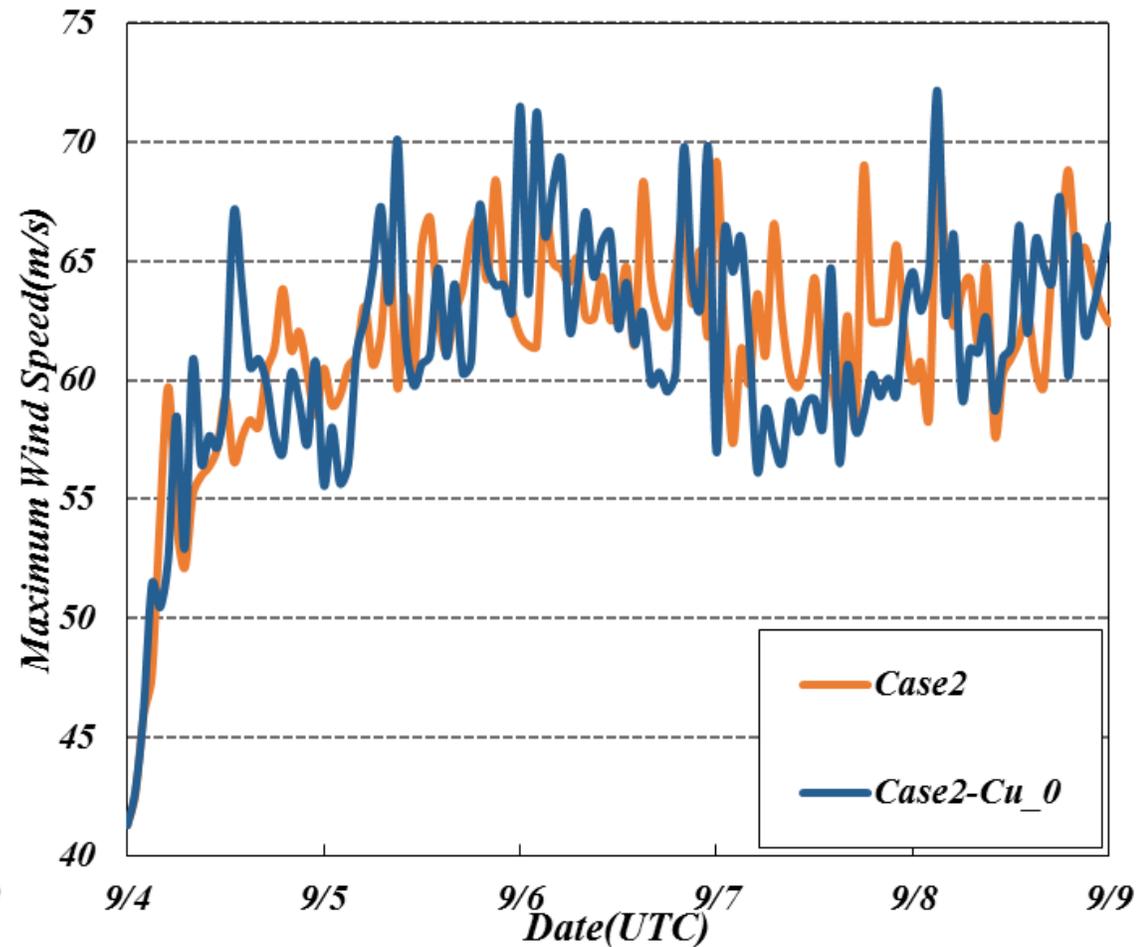
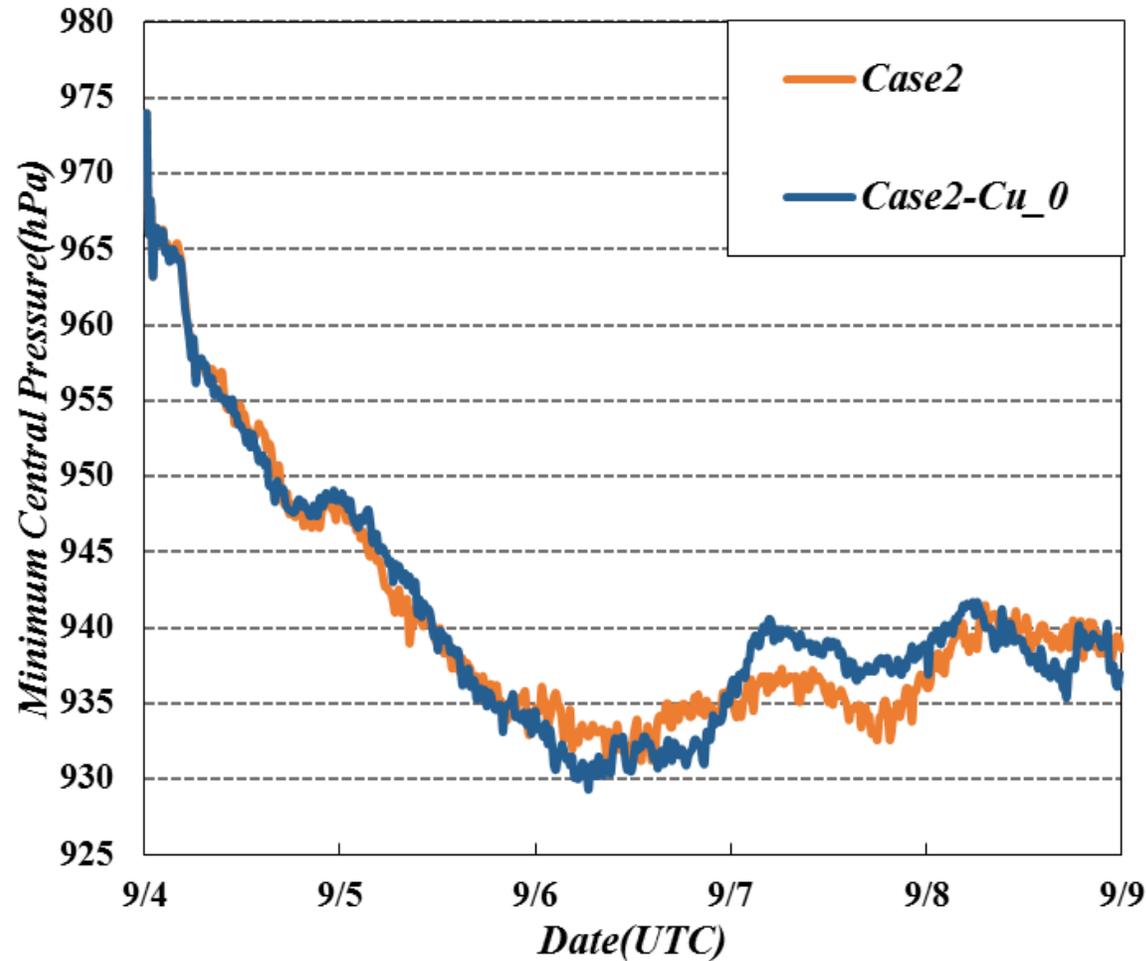
## Impact of data a assimilation



In any case, the result was **underestimated** because datasets can't reproduce accurately  
The intensity reproducibility of **Grid nudging is better way** than another nudging

# 3. Consideration of WRF

## Impact of cumulus parameterization



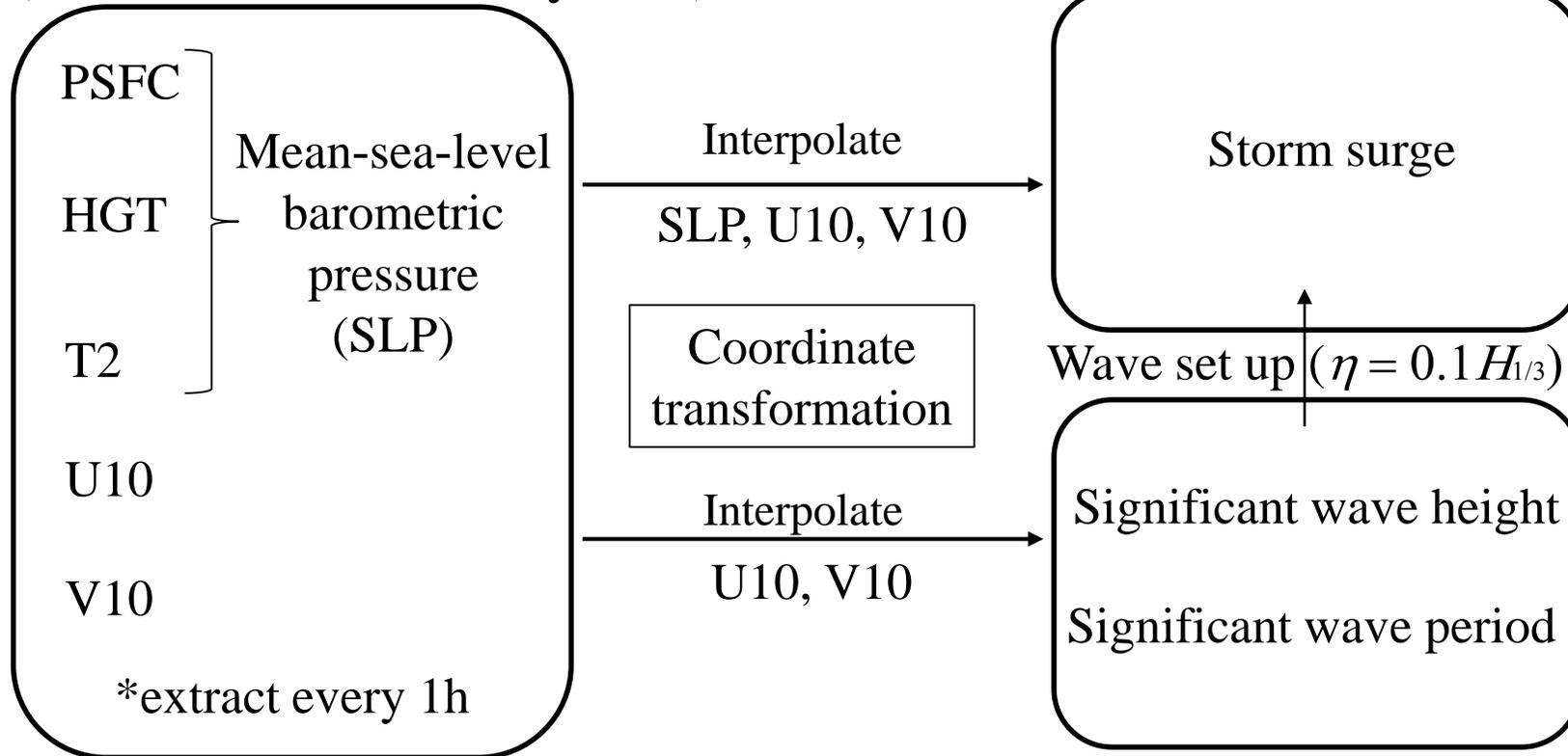
There aren't **much difference** when focus on meteorological fields and track

# 4. Application Method

## How to apply WRF to STOC and SWAN

WRF(Lat-Lon coordinate system)

STOC(Orthogonal coordinate system)



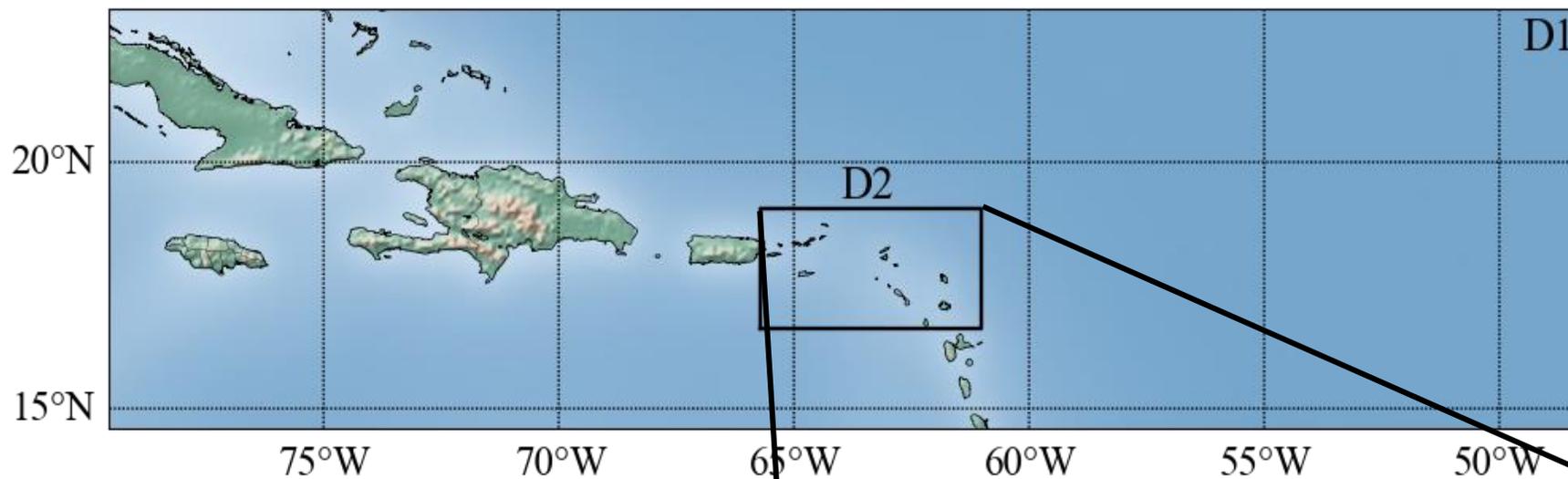
\*PSFC: Surface pressure  
HGT: Terrain Height  
T2: Temperature at 2m  
U10, V10: 10m-elevation wind speed

SWAN(Orthogonal coordinate system)



# 4. Consideration of Storm Surge and Wave Height

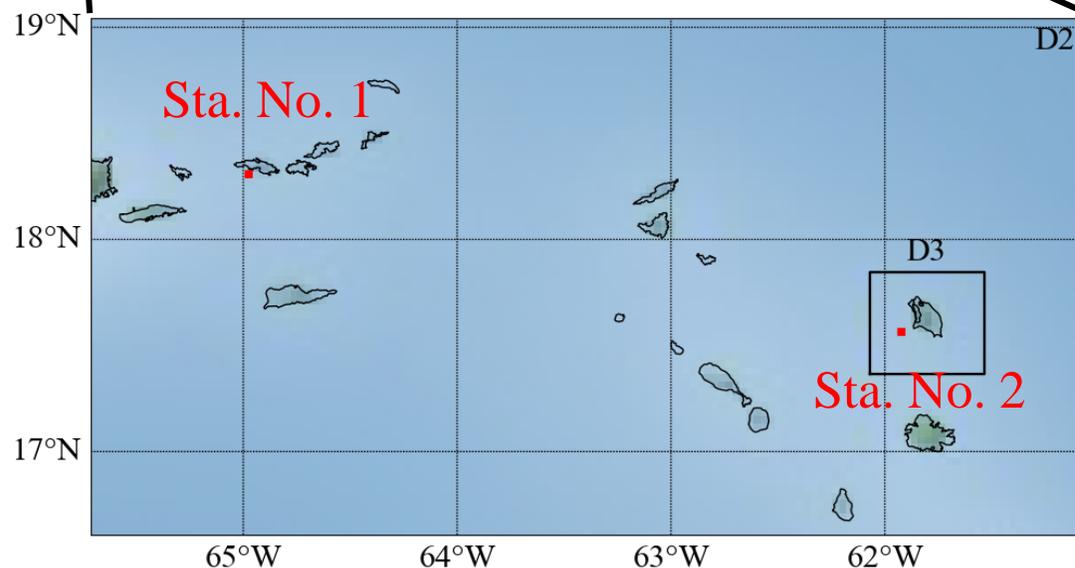
STOC, SWAN



Sta. No. 1 : Charlotte Amalie

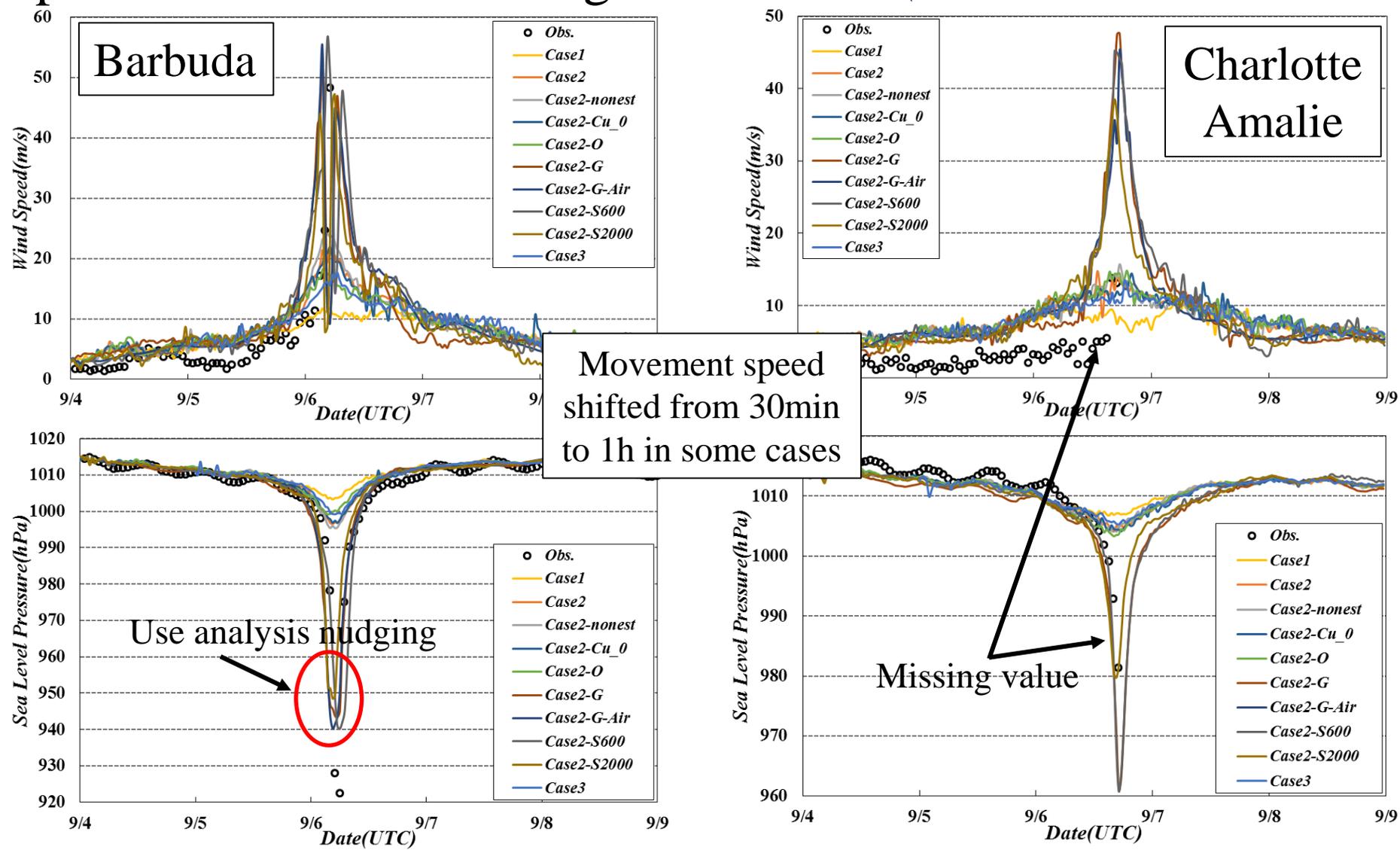
Sta. No. 2 : Barbuda Island

	Grid Size	Num. of Cell
D1	5000m	634*184
D2	1000m	500*275
D3	200m	300*300



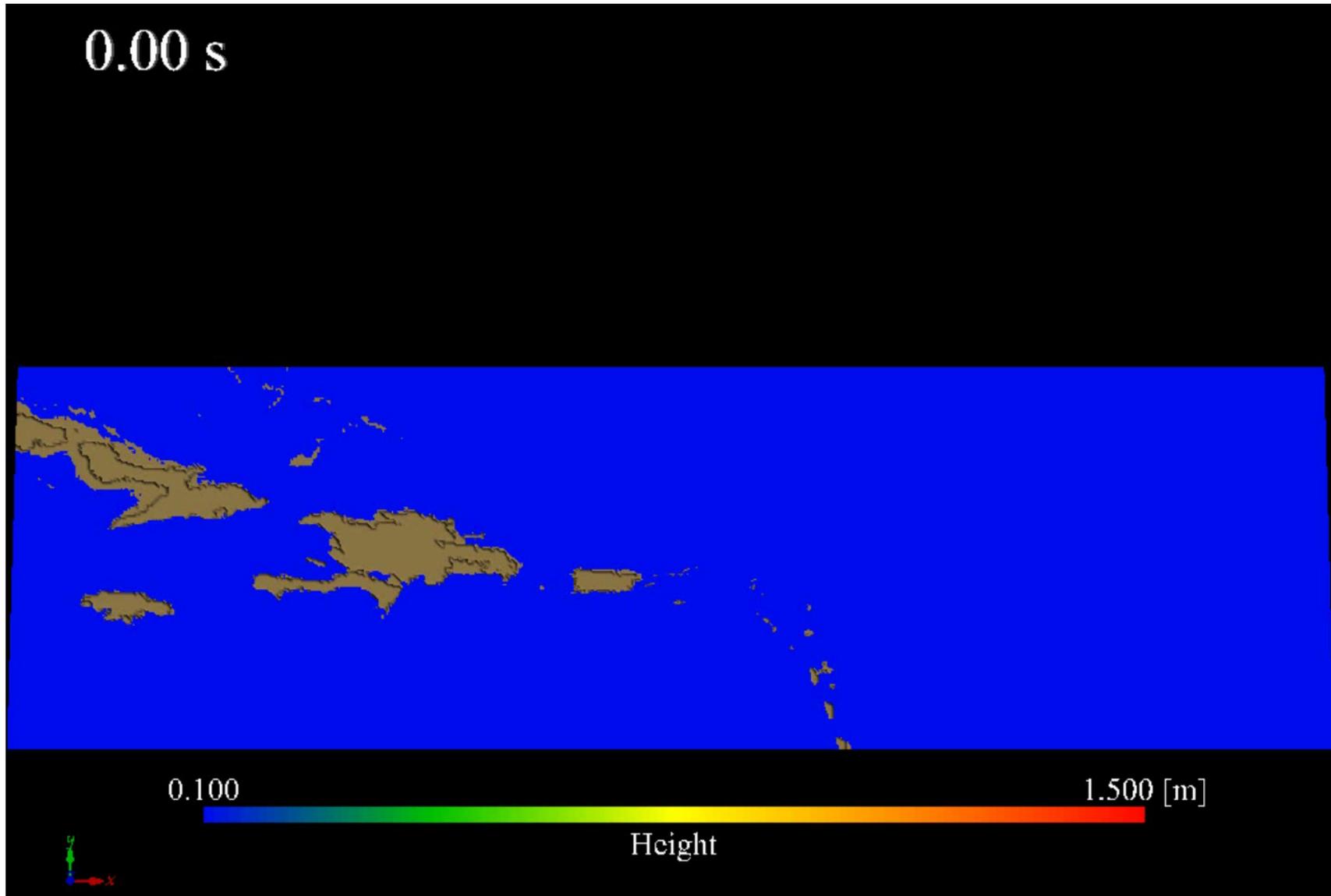
# 4. Consideration of Storm Surge and Wave Height

Comparison of the meteorological fields ← Depend on track



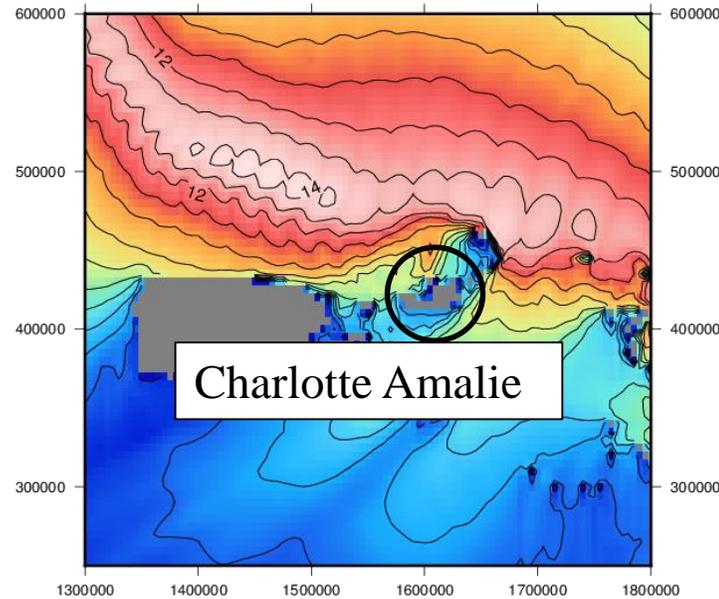
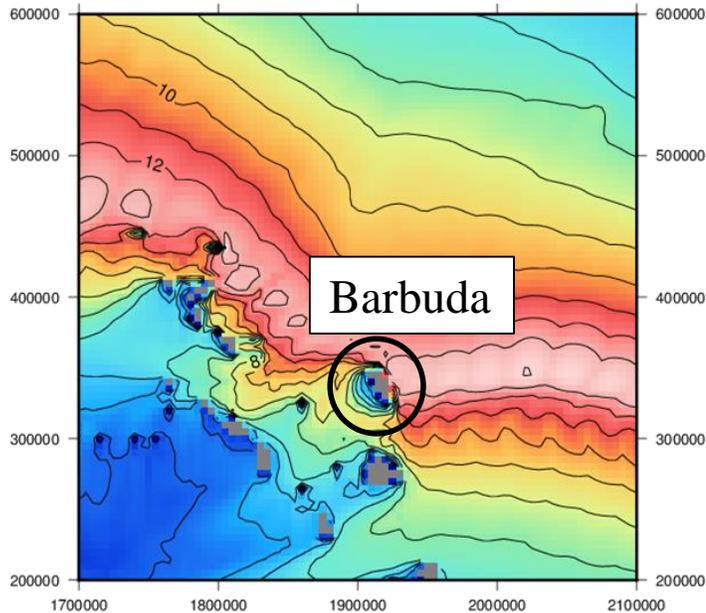
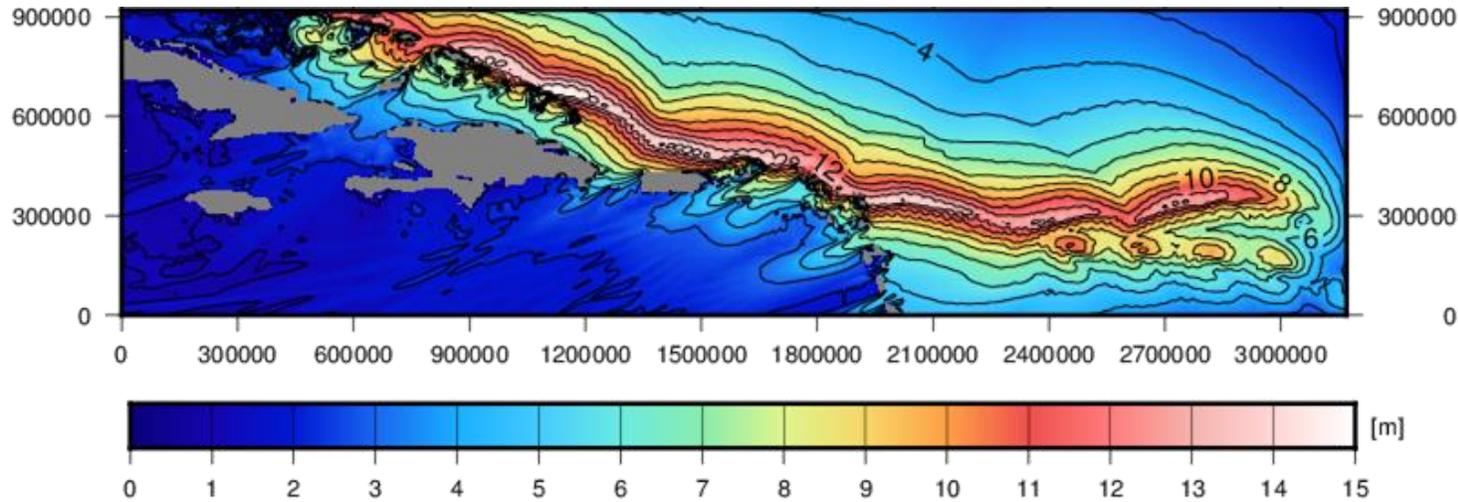
# 4. Consideration of Storm Surge and Wave Height

Animation of calculation result about storm surge



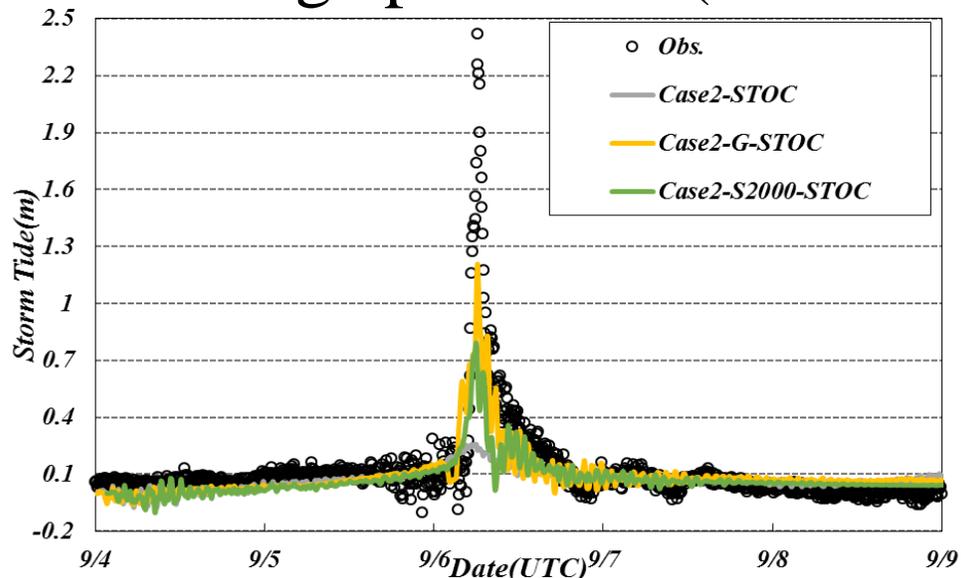
# 4. Consideration of Storm Surge and Wave Height

Maximum significant wave height distribution (Case2-G) using by SWAN

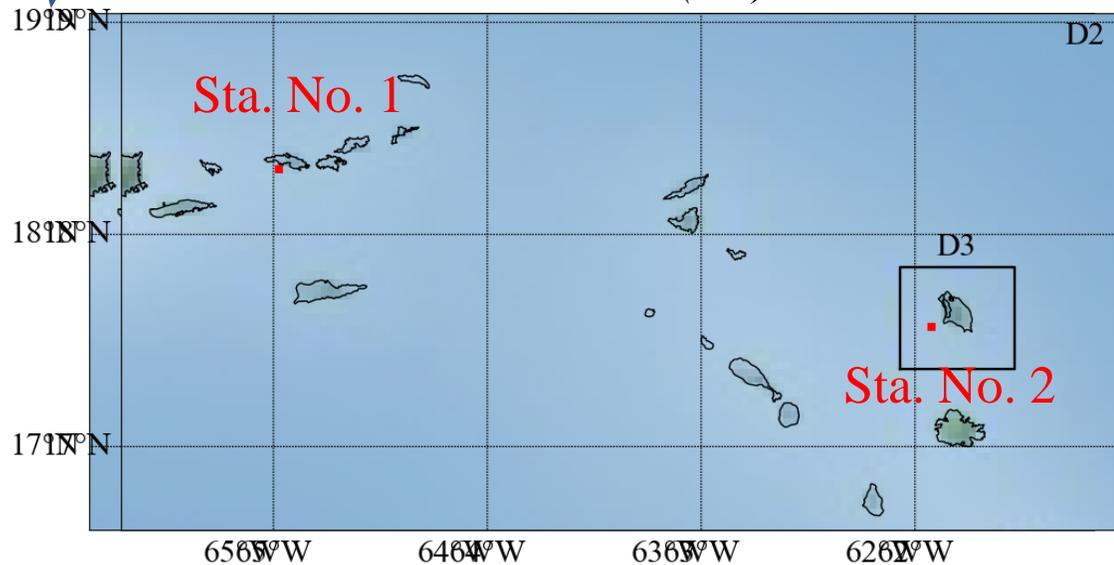
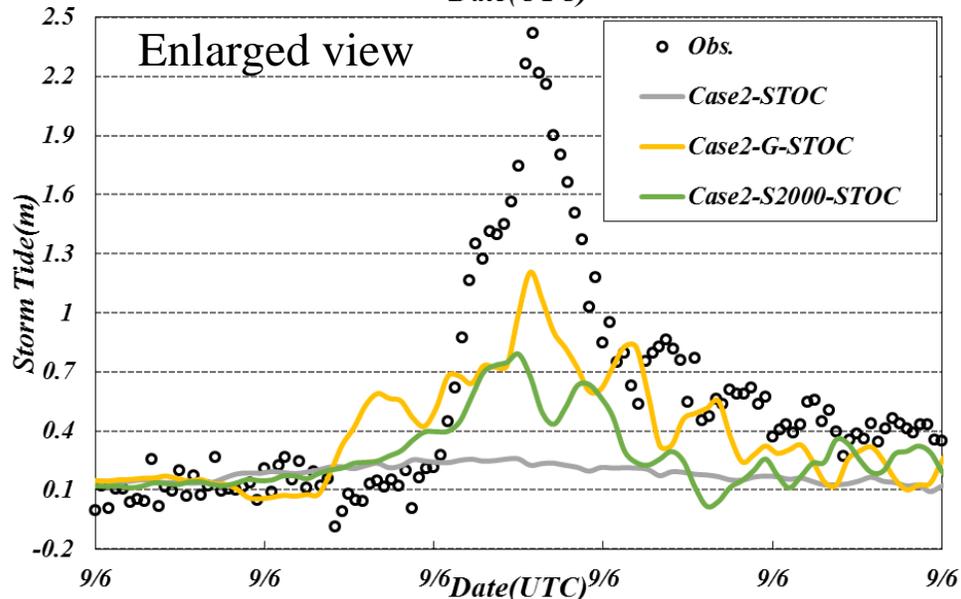
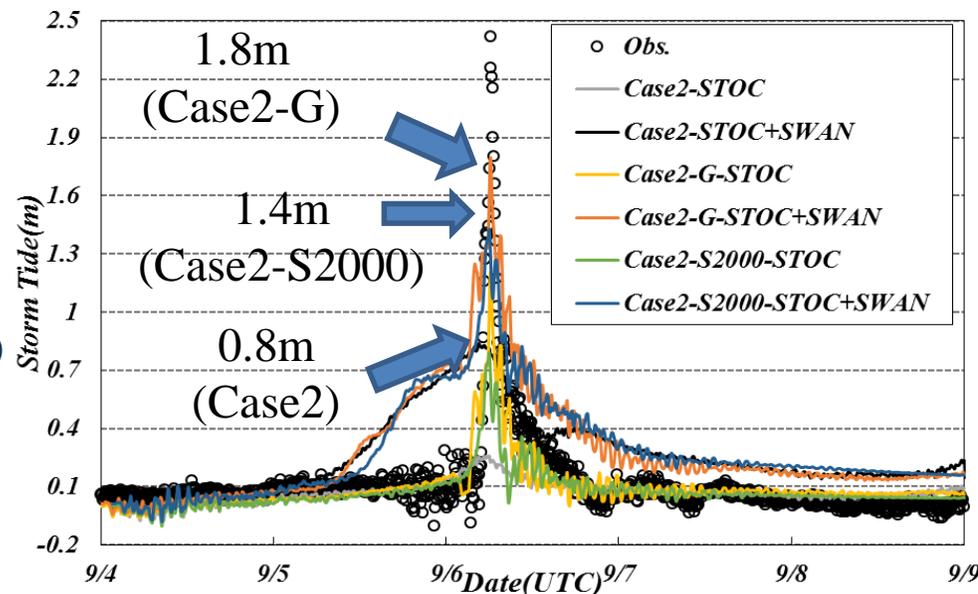
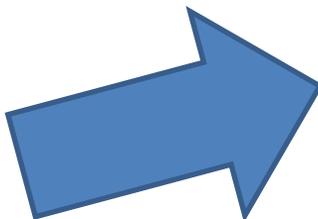


# 4. Consideration of Storm Surge and Wave Height

## Storm surge prediction(Barbuda)

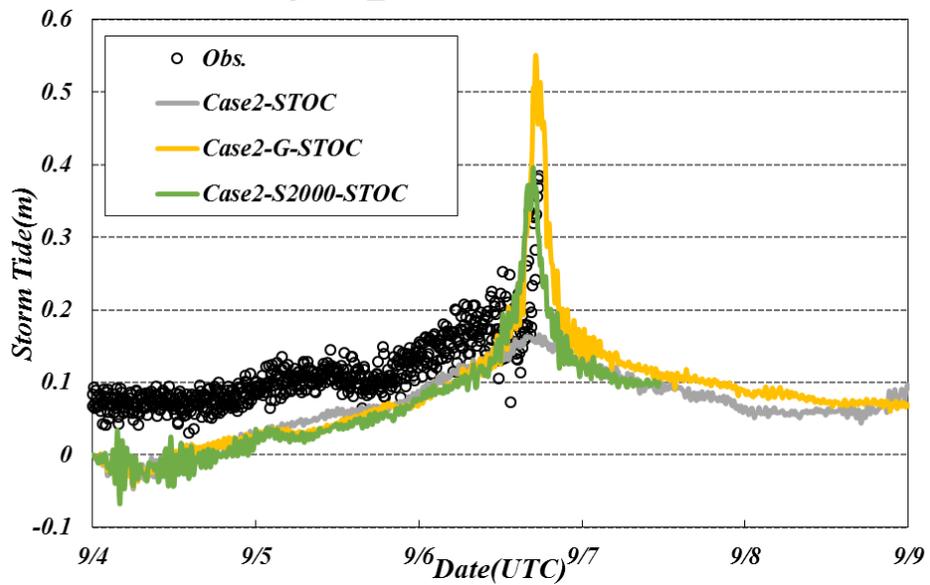


Wave set up

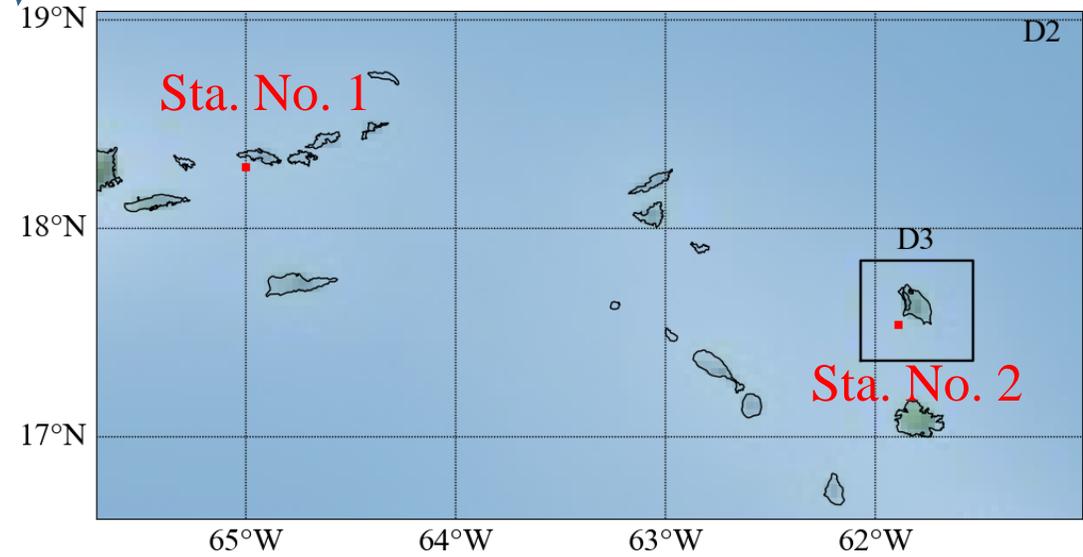
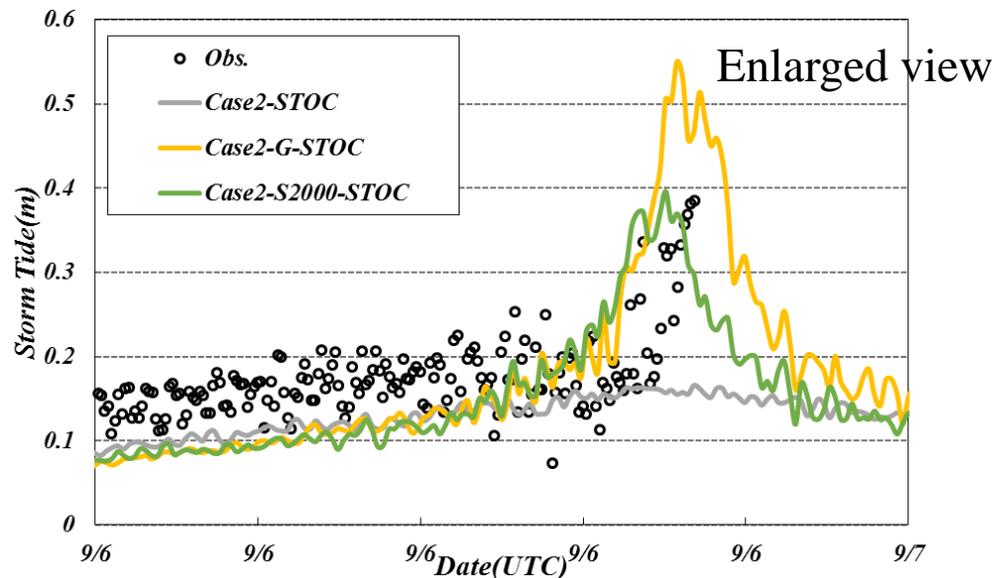
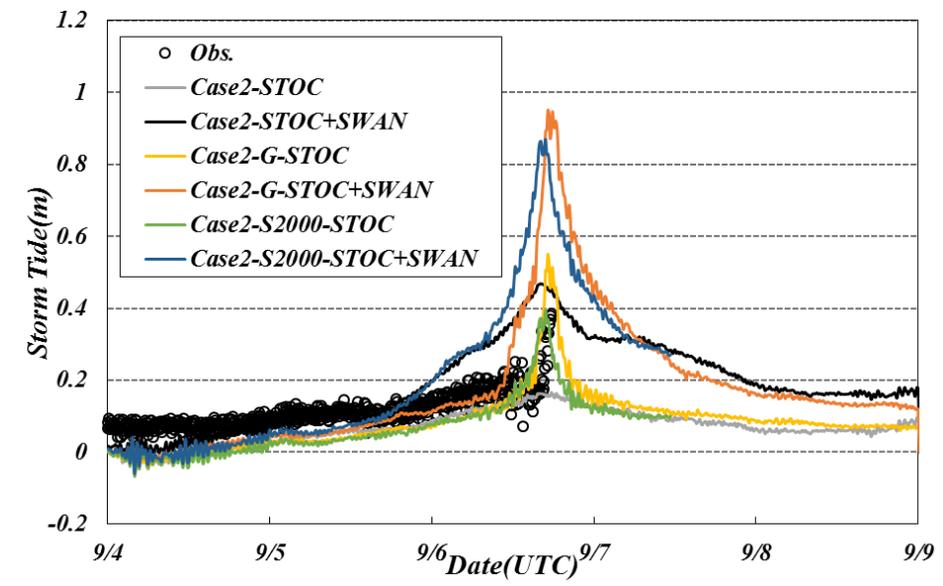


# 4. Consideration of Storm Surge and Wave Height

## Storm surge prediction (Charlotte Amalie)



Wave set up



# 5. Conclusion

- 1) By setting the initial time when the eye of Hurricane can be confirmed, the development of the strength can be reproduced well.
- 2) By applying grid analysis nudging for D1, the reproducibility of the hurricane track improved, specifically the error falls within the range of 30 to 50km as a whole.
- 3) If we use 1km moving nests, it doesn't significantly affect the reproducibility of meteorological fields without using cumulus parameterization because it is said to calculate vertical transport directly.
- 4) It is considered that if we accurate meteorological fields (WRF) to STOC, storm surge occurred at the points can be reproduced.

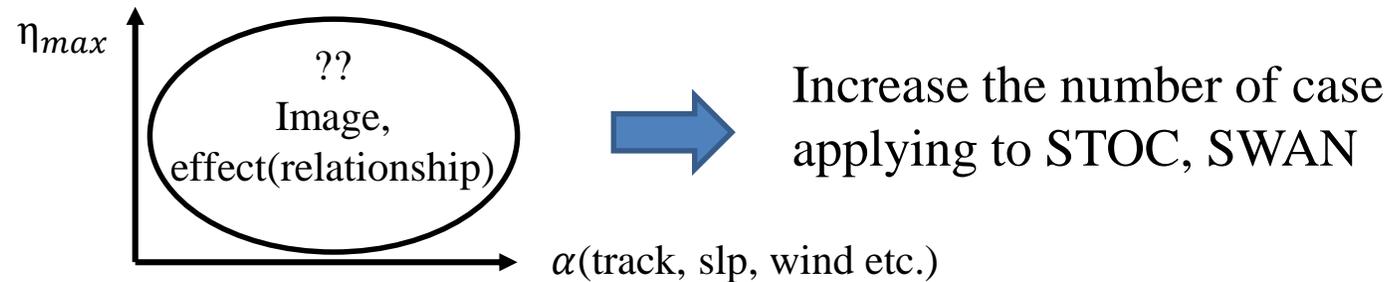


# 5. Conclusion

## Future works

- Further consideration

Ex.) apply to other weather disturbances, investigate the effect of WRF error to storm surge...



- Calculate wave setup correctly

- Floods and river inundation

➔ Eventually, want to make use to the evacuation

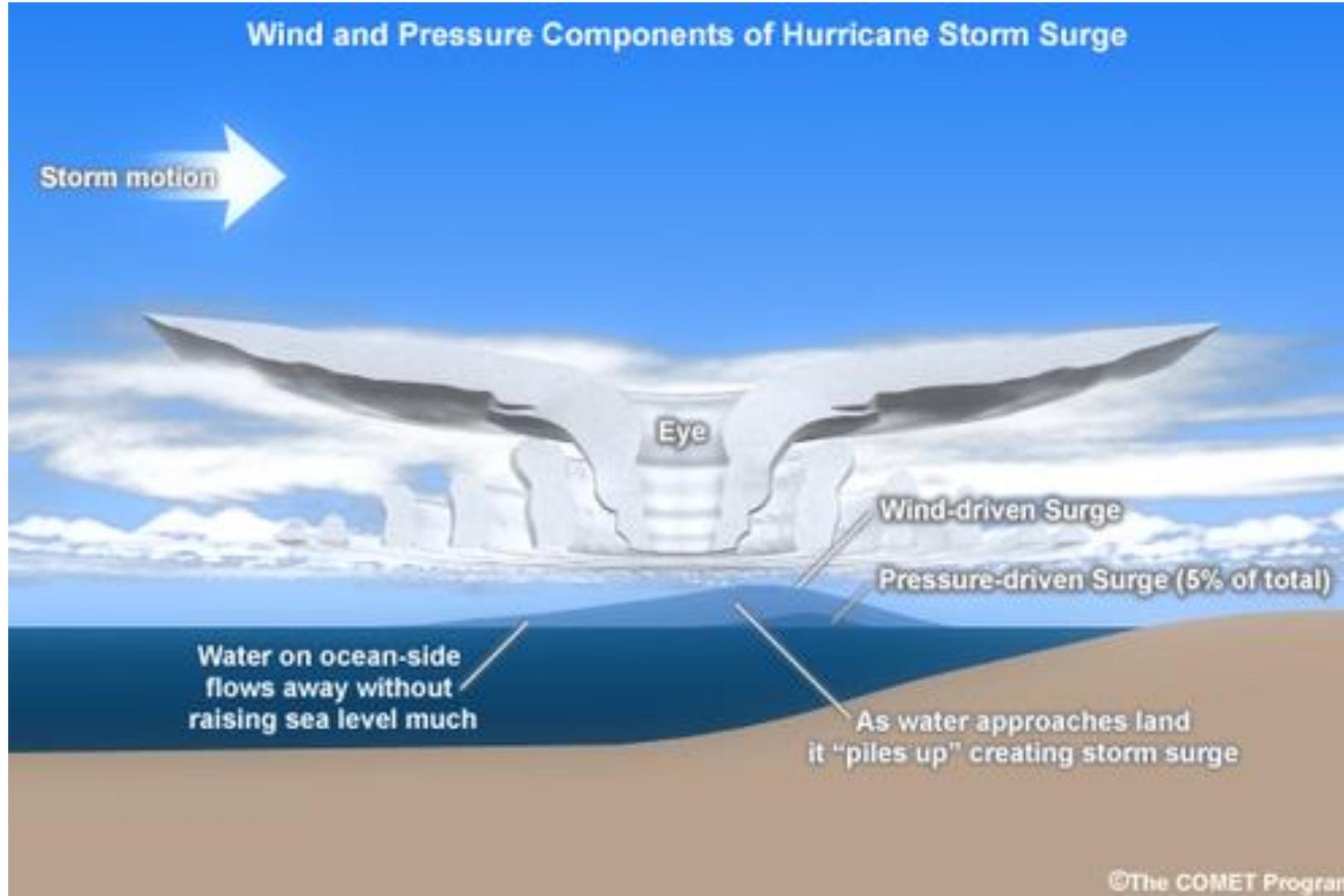
Thank you for your listening

# 2. Application Method

## How to apply WRF to STOC and SWAN

WRF

STOC,  
SWAN



# Appendix -Consideration of WRF

## Root Mean Square Error

$$RSME = SQRT\{\sum(F(i) - A(i))^2 \div N\}, \text{ F:Calculation, A:Observation}$$

Case	Location(km)	Pressure(hPa)	Wind Speed(m/s)
Case1	121.146	25.199	17.959
Case2	83.547	13.429	13.245
Case2-nonest	85.094	23.053	22.786
Case2-Cu_0	83.969	13.515	14.586
Case2-O	103.065	18.585	17.140
Case2-G	35.783	19.082	17.008
Case2-G-Air	33.533	19.324	17.335
Case2-S600	39.283	24.706	19.631
Case2-S2000	61.282	18.246	16.663
Case3	96.418	17.342	16.637



## WRF – Governing equation

$\eta$  coordinate system :  $\eta = \frac{(P_h - P_{ht})}{\mu}$ , where  $\mu = P_{hs} - P_{ht}$

(Conservation of momentum)

$$\left\{ \begin{array}{l} \partial_t U + (\nabla \cdot V_u) + \mu_d \alpha \partial_x p + (\alpha/\alpha_d) \partial_\eta p \partial_x \Phi = F_U \\ \partial_t V + (\nabla \cdot V_v) + \mu_d \alpha \partial_y p + (\alpha/\alpha_d) \partial_\eta p \partial_y \Phi = F_V \\ \partial_t W + (\nabla \cdot V_w) - g \left[ \left( \frac{\alpha}{\alpha_d} \right) \partial_\eta p - \mu_d \right] = F_W \end{array} \right.$$

, where  $\mathbf{V} = \mu_d \mathbf{v}$ , ( $\mathbf{V} = (U, V, W)$ ,  $\mathbf{v} = (u, v, w)$ )

(Conservation of mass)

$$\partial_t \mu_d + (\nabla \cdot \mathbf{V}) = 0$$

---

$P_h$  : hydrostatic component of the pressure,  $P_{hs}$  and  $P_{ht}$  : refer to values along the surface and top boundaries



# Appendix

(Entropy mass conservation)

$$\partial_t \Theta + (\nabla \cdot V \theta) = F_\Theta \quad , \text{ where } \Theta = \mu_d \theta$$

(Scalar mass conservation)

$$\partial_t Q_m + (\nabla \cdot V q_m) = F_{Q_m} \quad , \text{ where } Q_m = \mu_d q_m$$

(Geopotential law)

$$\partial_t \Phi + \mu_d^{-1} [(V \cdot \nabla \Phi) - gW] = 0 \quad , \text{ where } \Phi = gz$$

(Diagnostic relations)

$$\partial_\eta \Phi = -\alpha_d \mu_d$$

$$p = (R_d \theta_m / p_0 \mu_d \alpha_d)^\gamma$$

---

$R$  :gas constant,  $\alpha$  :specific volume,  $\gamma$  :ratio of  $c_p$  to  $c_v$  ( $= c_p/c_v$ ),  $d$  :dry air,  
 $q_m$  :mixing ratio of water vapor, cloud water, snow, ice, hailstone,  $\omega$  :vertical velocity,  
 $\theta_m$  :virtual potential temperature( $\theta_m = \theta[1 + (\frac{R_v}{R_d}) q_m] \approx \theta(1 + 1.61q_m)$ ),  $R_v$  :gas  
constant(moist air),  $W$  :vertical flux

## STOC – Governing equation

(Conservation of momentum)

$$\begin{aligned} \text{x-direction: } \rho \frac{\partial u}{\partial t} + \frac{\partial}{\partial x}(\gamma_x uu) + \frac{\partial}{\partial y}(\gamma_y uv) + \frac{\partial}{\partial z}(\gamma_z uw) - \gamma_v f_0 v = & -\gamma_v \frac{1}{\rho} \frac{\partial p}{\partial x} + \frac{\partial}{\partial x} \left( \gamma_x \nu_H^2 \frac{\partial u}{\partial x} \right) \\ & + \frac{\partial}{\partial y} \left\{ \gamma_y \nu_H \left( \frac{\partial u}{\partial y} + \frac{\partial v}{\partial x} \right) \right\} + \frac{\partial}{\partial z} \left\{ \gamma_z \nu_V \left( \frac{\partial u}{\partial z} + \frac{\partial w}{\partial x} \right) \right\} \end{aligned}$$

$$\text{(Conservation of mass)} \quad \frac{\partial}{\partial x}(\gamma_x u) + \frac{\partial}{\partial y}(\gamma_y v) + \frac{\partial}{\partial z}(\gamma_z w) = 0$$

$$\begin{aligned} \text{(Wind stress)} \quad \tau_{sx} = \rho_a \gamma_a^2 W_x \sqrt{W_x^2 + W_y^2} \quad \left\{ \begin{array}{l} \gamma_a^2 = 0.001 \times (1.29 - 0.024 \sqrt{W_x^2 + W_y^2}) \\ \text{(when } \sqrt{W_x^2 + W_y^2} < 8.0 \text{ m/s)} \\ \gamma_a^2 = 0.001 \times (1.29 - 0.024 \sqrt{W_x^2 + W_y^2}) \\ \text{(when } \sqrt{W_x^2 + W_y^2} \geq 8.0 \text{ m/s)} \end{array} \right. \end{aligned}$$

$$\text{(Bottom friction)} \quad \tau_{bx} = \frac{\rho g n^2 u_b \sqrt{u_b^2 + v_b^2}}{h^{1/3}}$$



## SWAN – Governing equation

(Spectral action balance equation)

$$\frac{\partial N}{\partial t} + \frac{\partial}{\partial x}(C_x N) + \frac{\partial}{\partial y}(C_y N) + \frac{\partial}{\partial \sigma}(C_\sigma N) + \frac{\partial}{\partial \theta}(C_\theta N) = S / \sigma$$

(Source term)

$$S = S_{in} + S_{ds} + S_{nl}$$

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$S_{in}$ : Energy transportation by wind

$S_{ds}$ : Dissipation of wave energy

$S_{nl}$ : Energy transportation by nonlinear wave-wave interactions



## What is Nudging method?

Assimilate observed values or objective analysis values as external force term

## How to assimilate gridded data

$$\frac{\partial \mu \alpha}{\partial t} = F(\alpha, X, t) + \mu \cdot G_{\alpha} \cdot W_{\alpha} \cdot \varepsilon \alpha(X)(\hat{\alpha} - \alpha)$$

---

$F$ : physical forcing terms of  $\alpha$ ,  $\mu$ : dry hydrostatic pressure,  $X$ : independent spatial variable,  $t$ : specified time window,  $\alpha$ : prediction variables (wind, temperature, water vapor),  $\hat{\alpha}$ : objective analysis values to the grid and interpolated linearly for  $\alpha$ ,  $G_{\alpha}$ : timescale controlling the nudging strength applied to variable  $\alpha$ ,  $W_{\alpha}$ : vertical weight,  $\varepsilon \alpha$ : horizontal weight for observation density



## How to assimilate obs. data

$$\frac{\partial \mu \alpha}{\partial t} = F(\alpha, X, t) + \mu \cdot G_{\alpha} \cdot \frac{\sum_{i=1}^N W_i^2(X, t) [\alpha_0(i) - \alpha_m(X_i, t)]}{\sum_{i=1}^N W_i(X, t)}$$

$$W_i(X, t) = w_{xy} \cdot w_{\sigma} \cdot w_t \left\{ \begin{array}{l} w_{xy} = \frac{R^2 - D^2}{R^2 + D^2} \quad (0 \leq D \leq R) \quad , w_{xy} = 0 \quad (D > R) \\ w_t = 1 \quad (|t - t_0| < \frac{\tau}{2}) \quad , w_t = \frac{\tau - |t - t_0|}{\tau/2} \quad (\frac{\tau}{2} \leq |t - t_0| \leq \tau) \end{array} \right.$$

---

$N$ : total number of the observed points,  $i$ : index to the current observation,  $\alpha_m$ : model value of  $\alpha$  interpolated to the observation location,  $w_{\sigma}$ : vertical weight,  $R$ : radius of influence,  $D$ : distance from observation modified by difference of elevation



- **Grid nudging**

Assimilate objective analysis values for lattice points

- **Spectral nudging**

For arbitrary scale disturbance

This may be useful for controlling longer wave phases for long analysis-driven simulations

- **Observation nudging**

Each grid point is nudged using a weighted average of differences from observations within a radius of influence and time window

