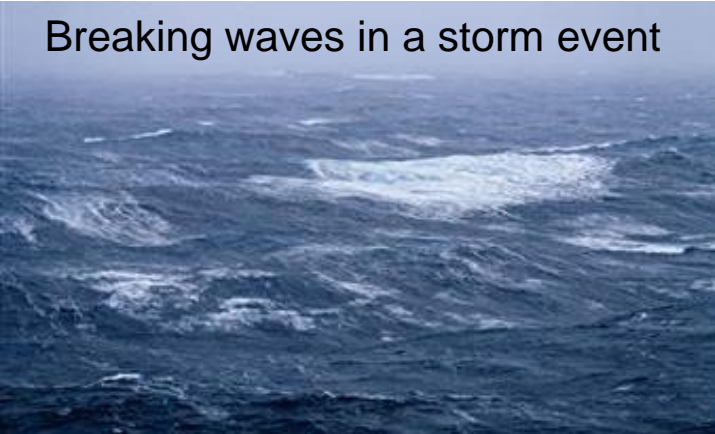


# Laboratory observations of dissolved carbon dioxide transport under regular breaking waves

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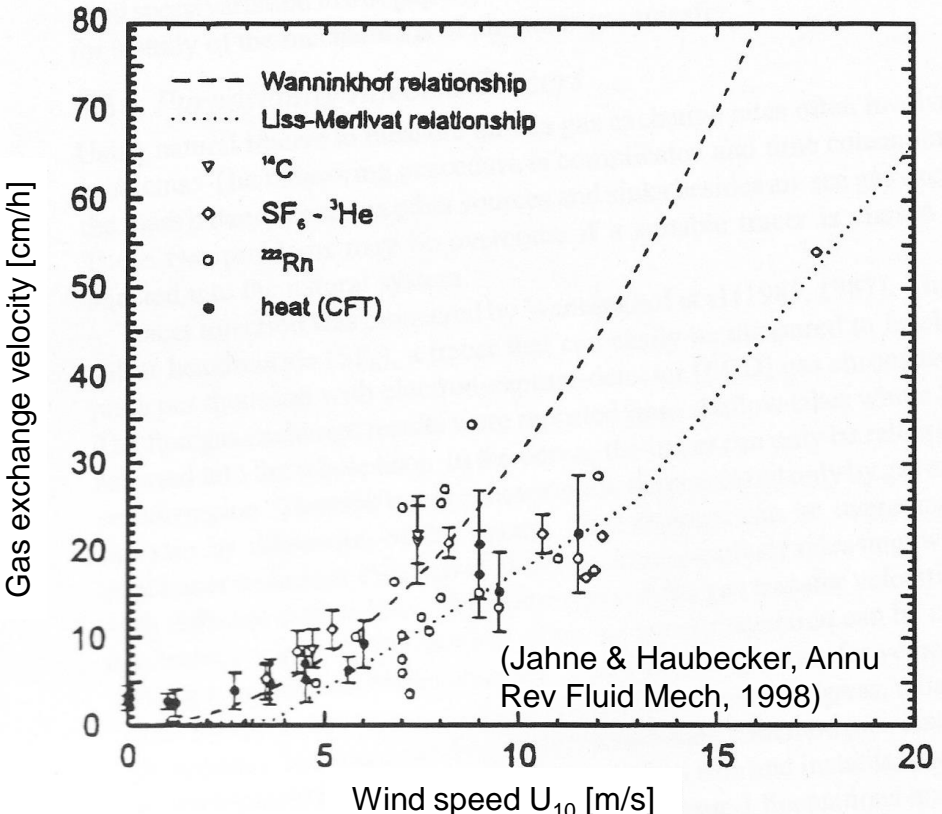
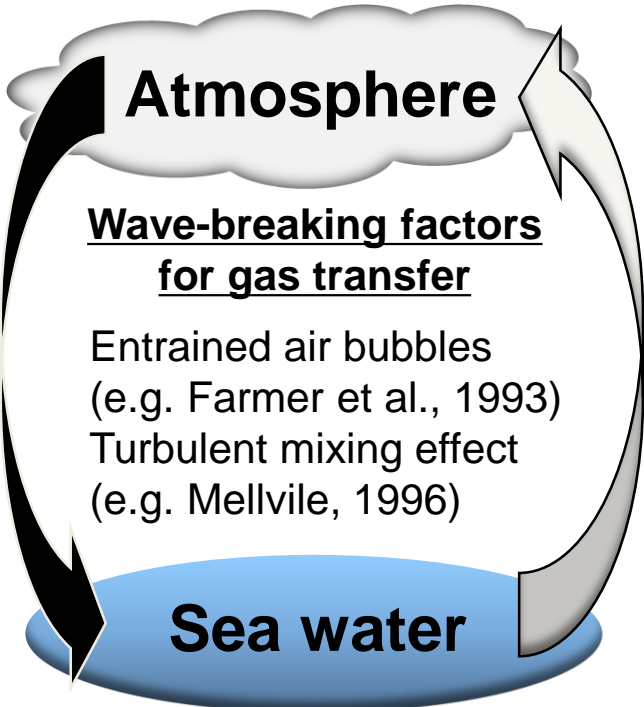
# Introduction

## Air-sea gas exchange over the ocean



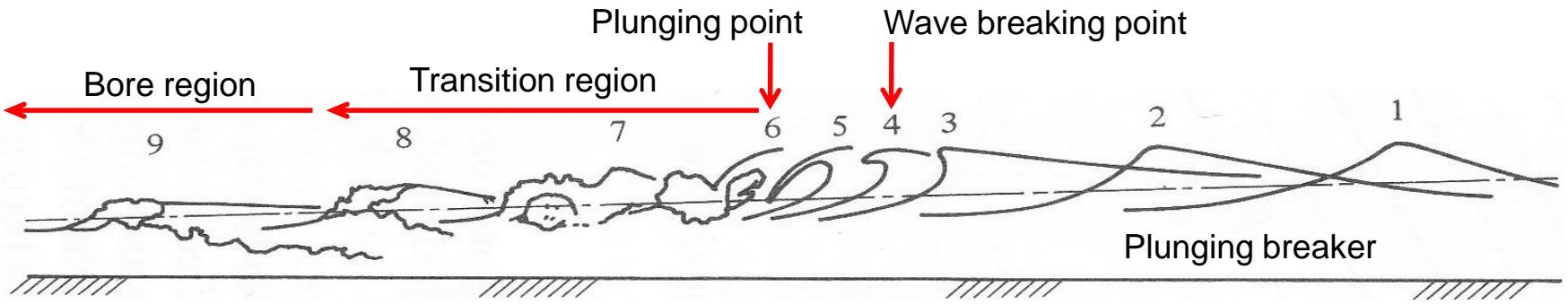
### Conventional gas exchange models

Simple model parameterized only by wind speed  $U_{10}$   
(e.g., Liss & Merlivat, 1986).



# Introduction

## Air-water turbulent flows in a surf zone



(R. G. Dean & R. A. Dalrymple, World Scientific)

Fully developed turbulent bore



Strong turbulence

Small number of air bubbles



Large number of air bubbles

Dissolved gas concentration and gas transfer velocity vary as waves propagate in a surf zone.

# Introduction

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## Final goal of our study

- To model the gas transfer velocity in a surf zone.

## Object of this study

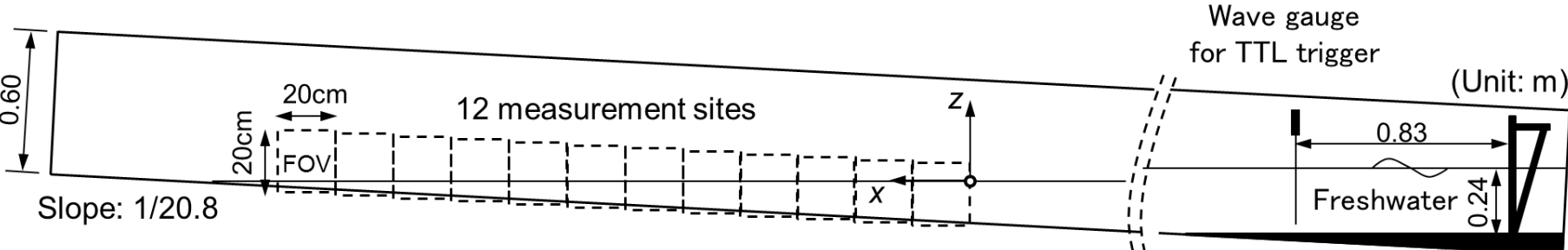
- To elucidate the gas transfer process in a surf zone.

## Methodology

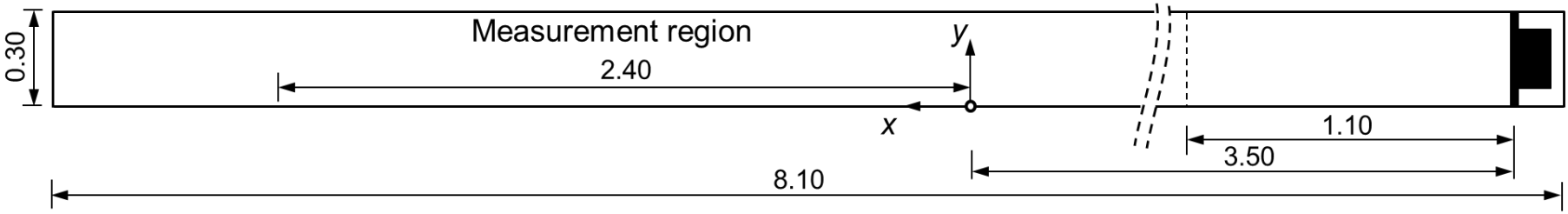
- Concentration field of dissolved carbon dioxide ( $\text{DCO}_2$ ), velocity field and entrained bubbles were experimentally measured in a wave flume.
  - $\text{DCO}_2$  concentration field: Laser induced fluorescence (LIF)
  - Velocity field: Particle image velocimetry (PIV)
  - Entrained bubbles: LED backlight

# Experimental setup and wave condition

(a) Cross-section view



(b) Plane view



- High speed video camera: 8 bit, 250 fps
- Image resolution: 1,000 x 1,000 pixels (0.02 cm/pixel)
- Duration of image recording: 21.8s

Case No.	Wave period $T$ (s)	Breaking wave height $H_b$ (cm)	Breaking wave depth $h_b$ (cm)	Bottom slope	Breaker type	Surf similarity parameter
Case1	1.5	13.0	13.9	1/20.8	Spilling/Plunging	0.247

# LIF measurement for $\text{DCO}_2$ concentration field

Concentration field of dissolved carbon dioxide ( $\text{DCO}_2$ ) was measured using LIF.

Fluorescent dye uranine was used in the LIF.

Fluorescence intensity of uranine is sensitive to pH in the range of pH4 to pH8.

$\text{CO}_2$  gas into water

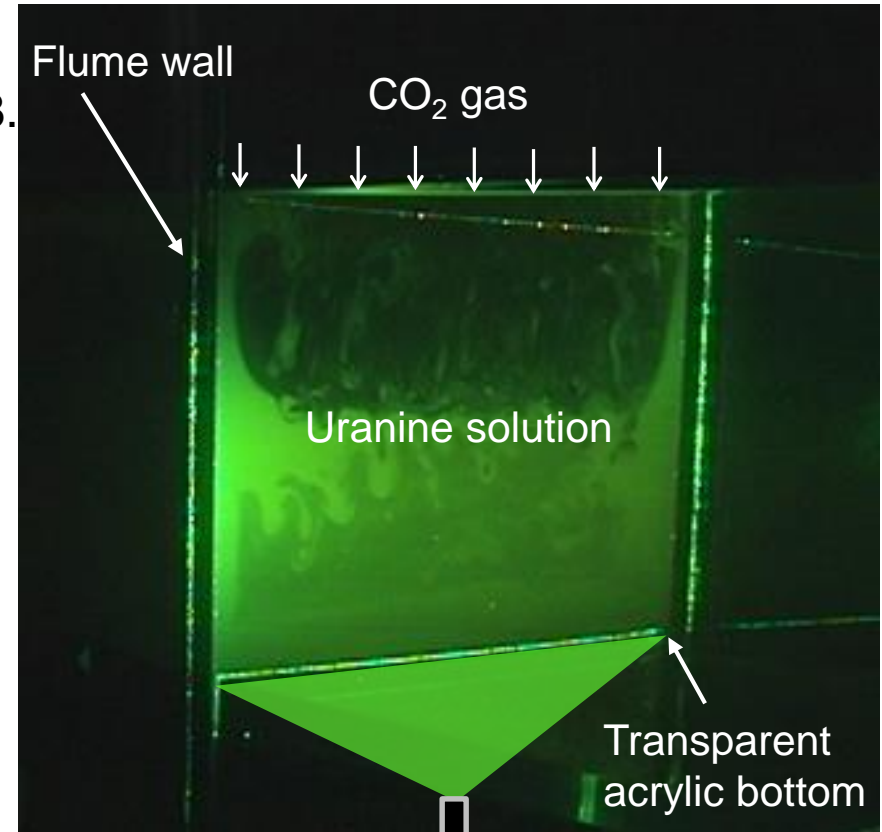


pH decreases



Fluorescence intensity decreases

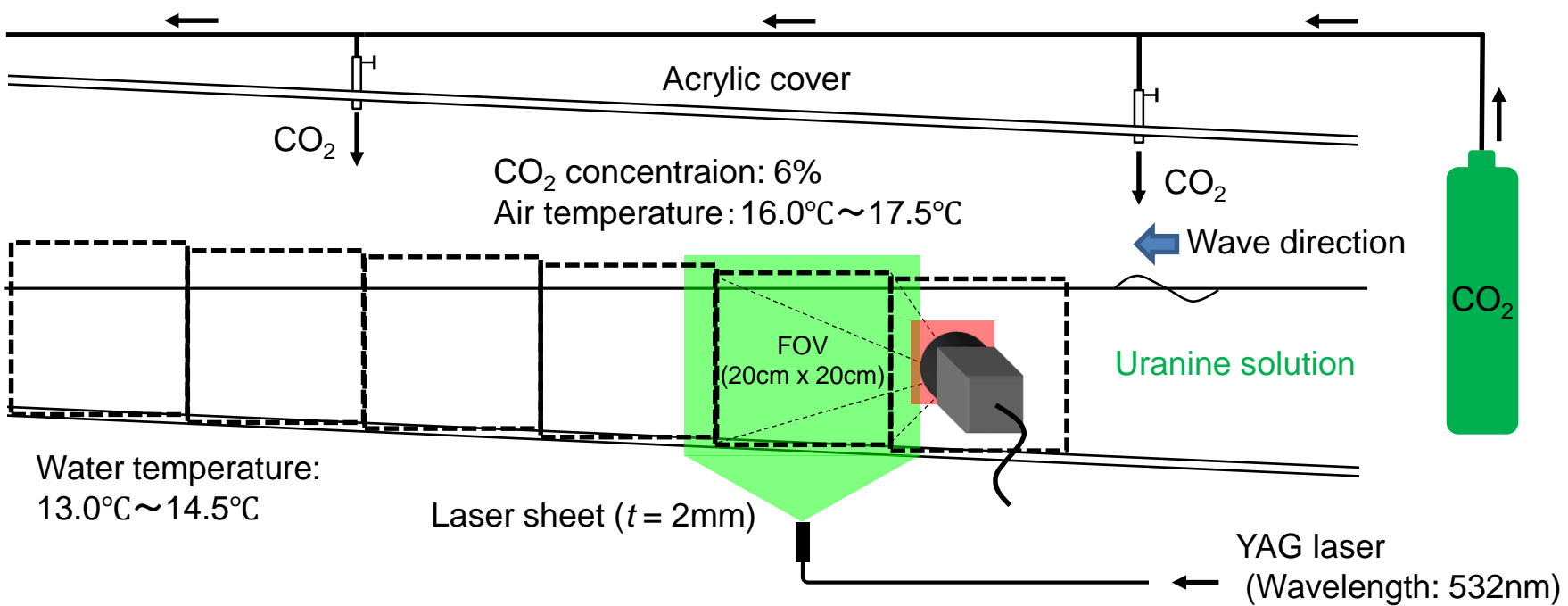
$\text{DCO}_2$  concentration was visualized by obtaining the relation between fluorescence intensity and  $\text{DCO}_2$  concentration.



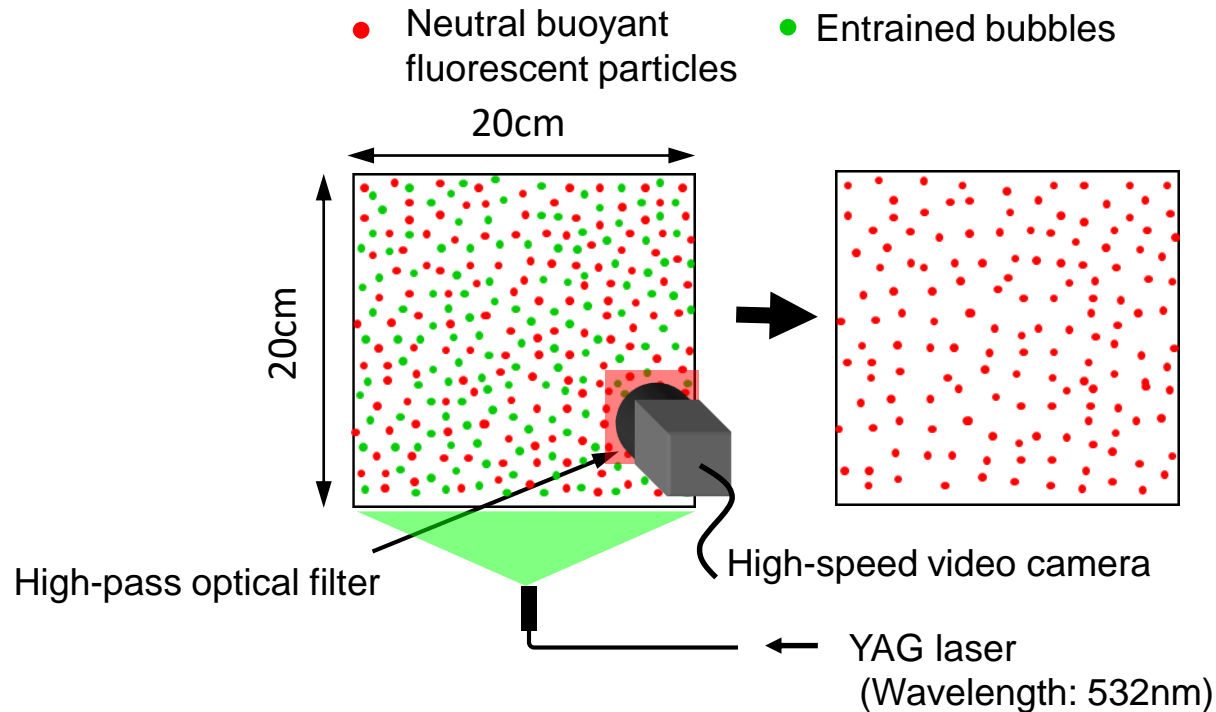
YAG laser sheet  
(Wave length: 532 nm)

# LIF measurement for DCO<sub>2</sub> concentration field

<Cross-section view>



# PIV measurement for velocity field



- Sixteen trials were performed for each measurement site.
- Ensemble average was taken over the 16 trials to define the ensemble averaged velocity  $\bar{u}$  and  $\bar{v}$ .

Turbulent energy  $k$  is defined as

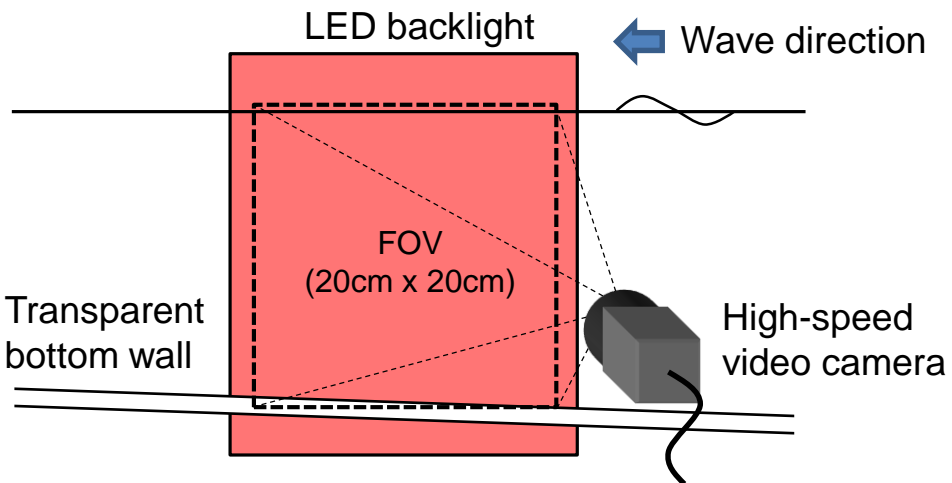
$$k = \frac{1}{2} (\overline{u'^2} + \overline{v'^2})$$

$u' = u - \bar{u}$        $u$ : instantaneous horizontal velocity  
 $v' = v - \bar{v}$        $v$ : instantaneous vertical velocity  
—: ensemble-averaging operation for instantaneous values

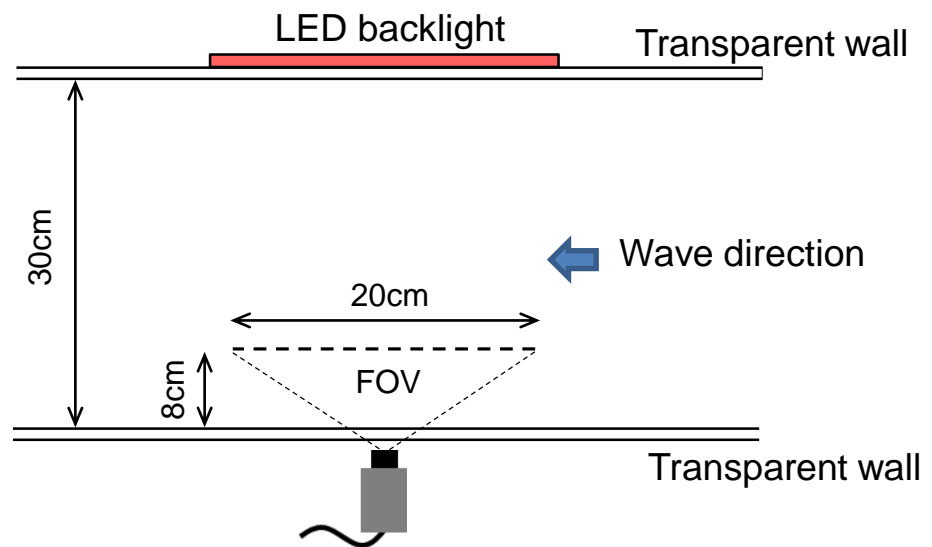


# LED backlight for visualization of entrained bubbles

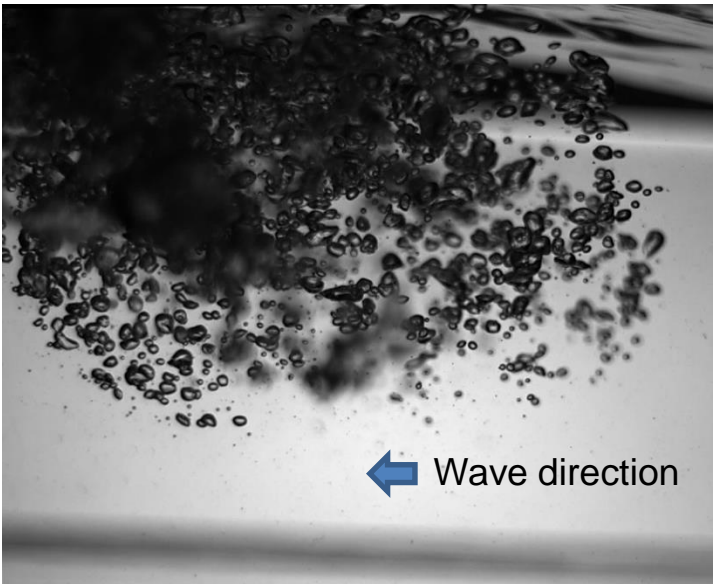
<Cross-section view>



<Plane view>



Visualized entrained bubbles



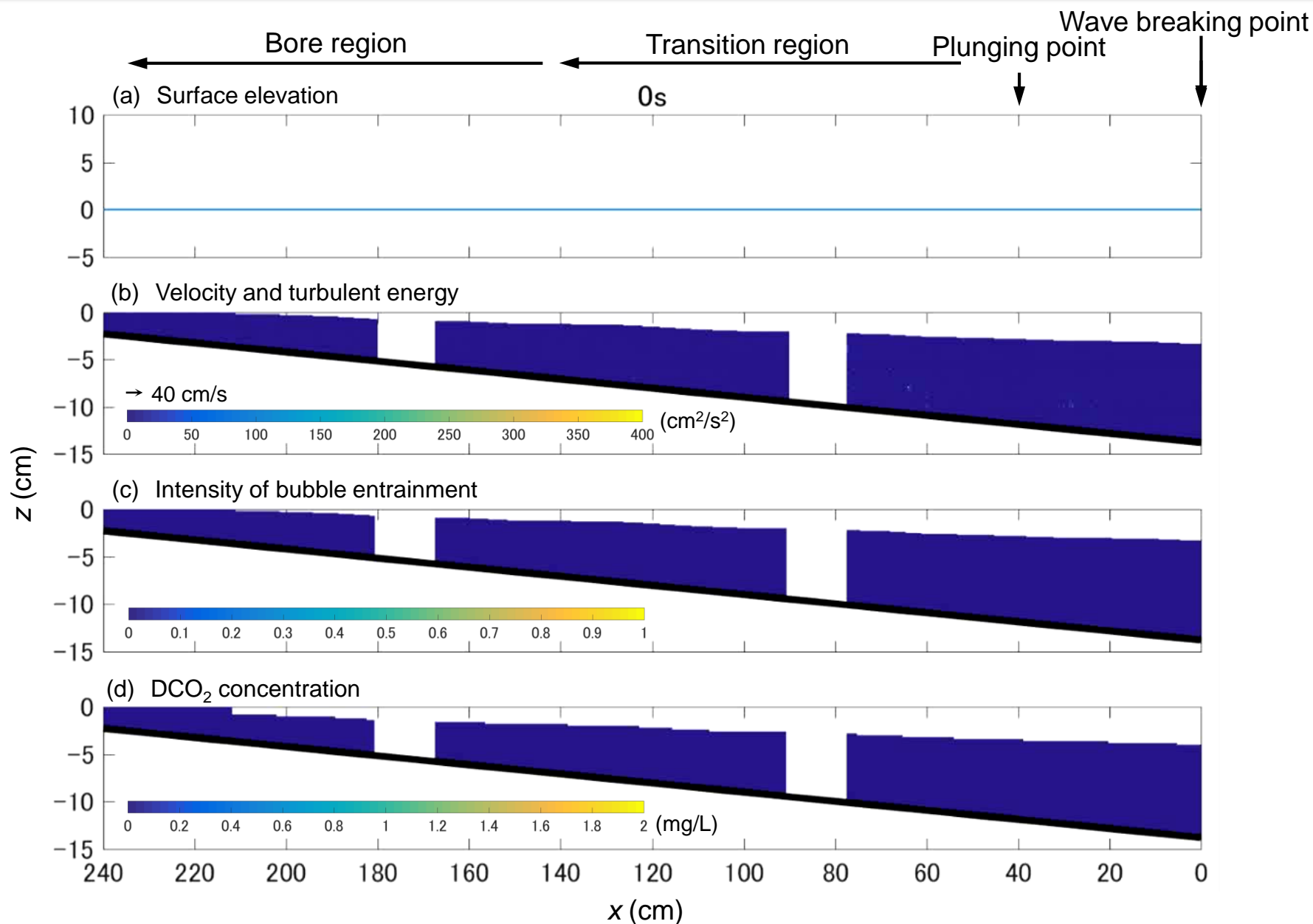
Intensity of bubble entrainment:

$$= \frac{I_{ini} - I_{bub}}{I_{ini}}$$

$I_{ini}$ : Non-aerated state image intensity

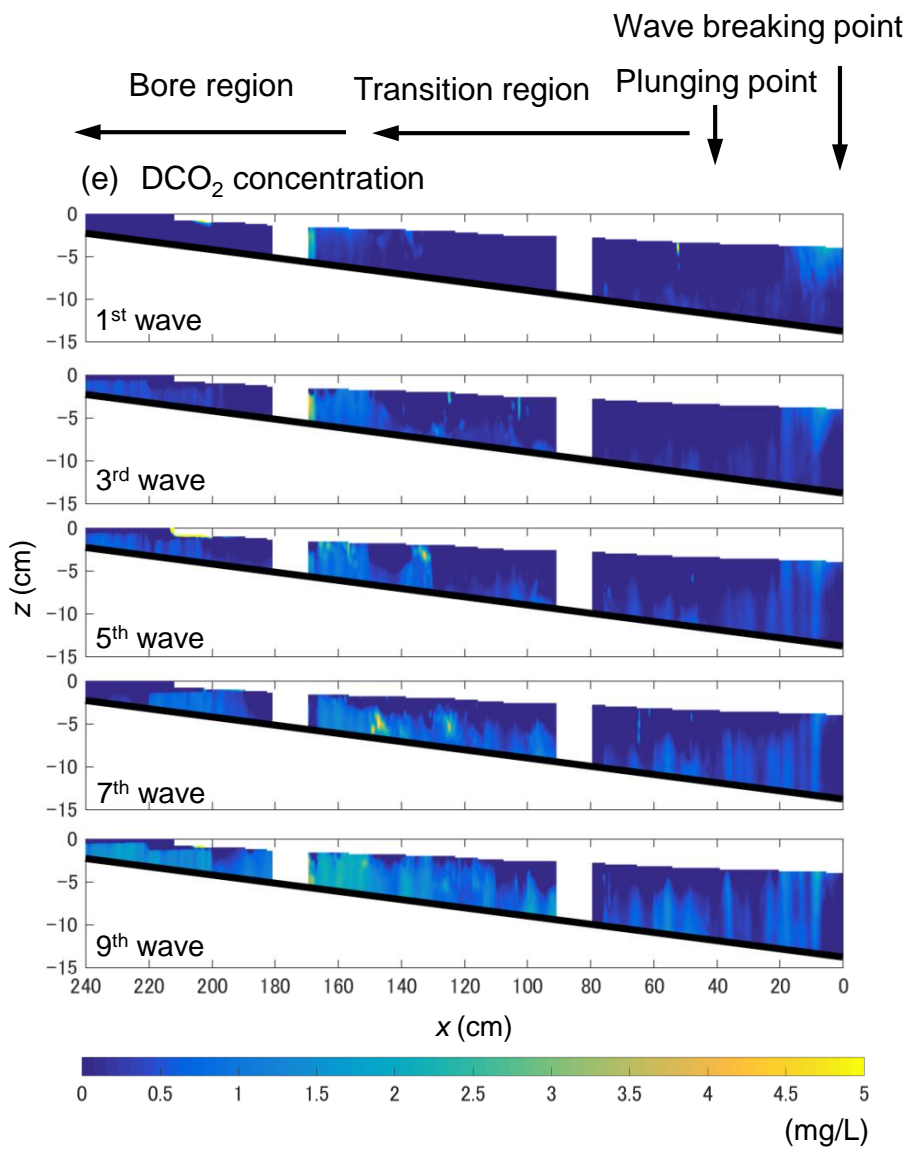
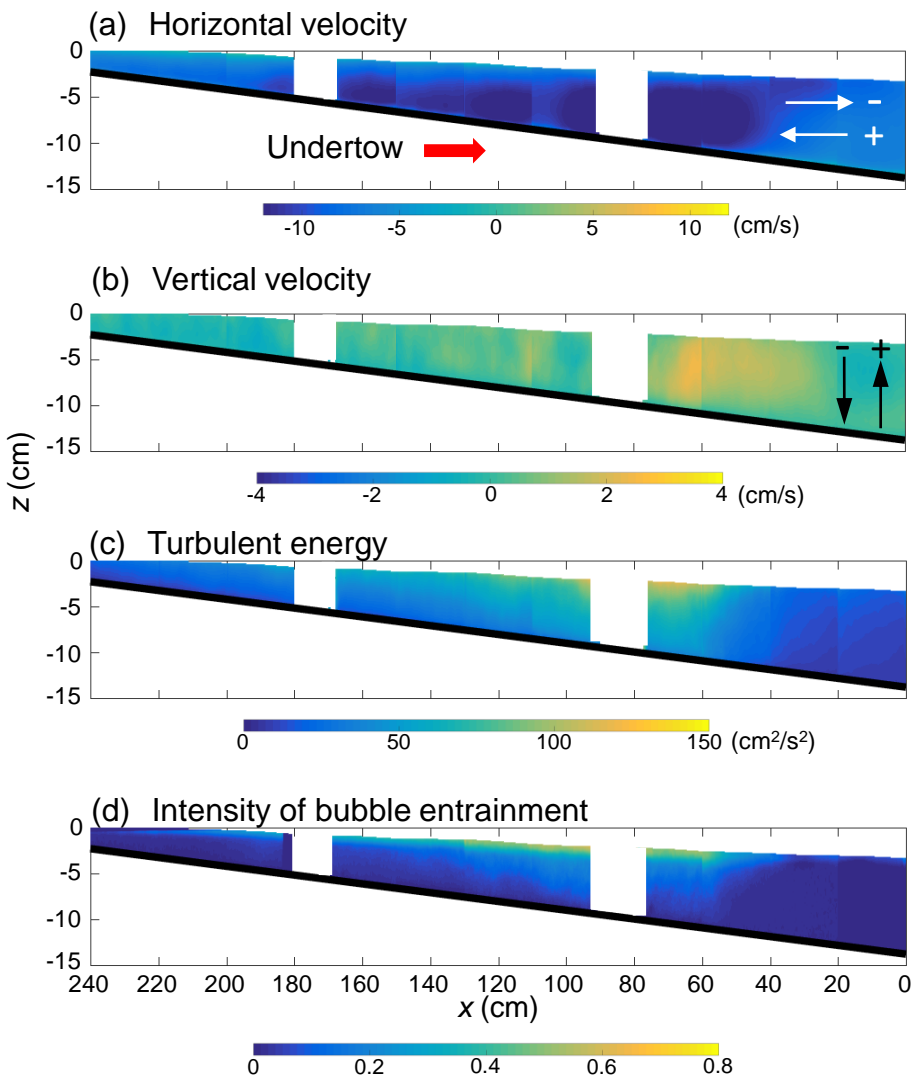
$I_{bub}$ : Bubble image intensity

# Temporal variations in cross-shore distributions of surface elevation, velocity, turbulent energy, bubble image intensity and DCO<sub>2</sub> concentration



# Cross-shore distributions of time-averaged velocity, turbulent energy, bubble intensity and DCO<sub>2</sub> concentration

Averaged over 10 waves



# Estimation of gas transfer velocity in the surf zone

- Gas flux can be expressed as:

$$F = U\Delta C \quad (1)$$

$U$ : gas transfer velocity

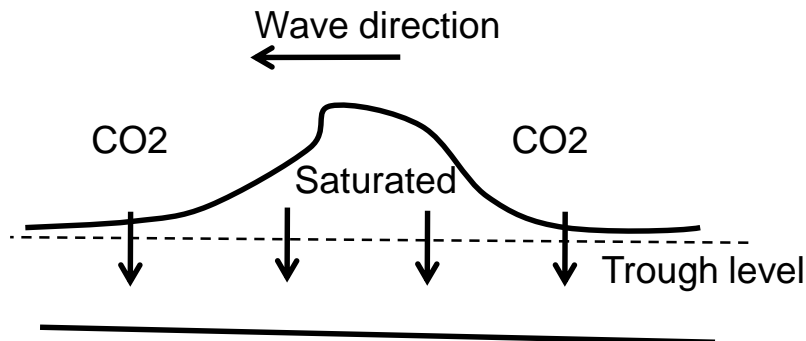
$\Delta C$ : difference of gas concentration across the water surface

- Assumption:  
the region above wave trough level is saturated

$$\Delta C = C_s - C_f \quad (2)$$

$C_s$ : concentration above wave trough level (6%)

$C_f$ : concentration under wave trough level



- Gas flux also can be expressed as:

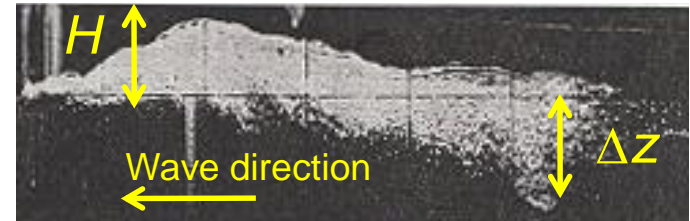
$$F = \frac{dC}{dt} \Delta z \quad (3)$$

$\Delta z$ : turbulent mixing depth

- Assumption:

$$\Delta z \cong H \quad (4)$$

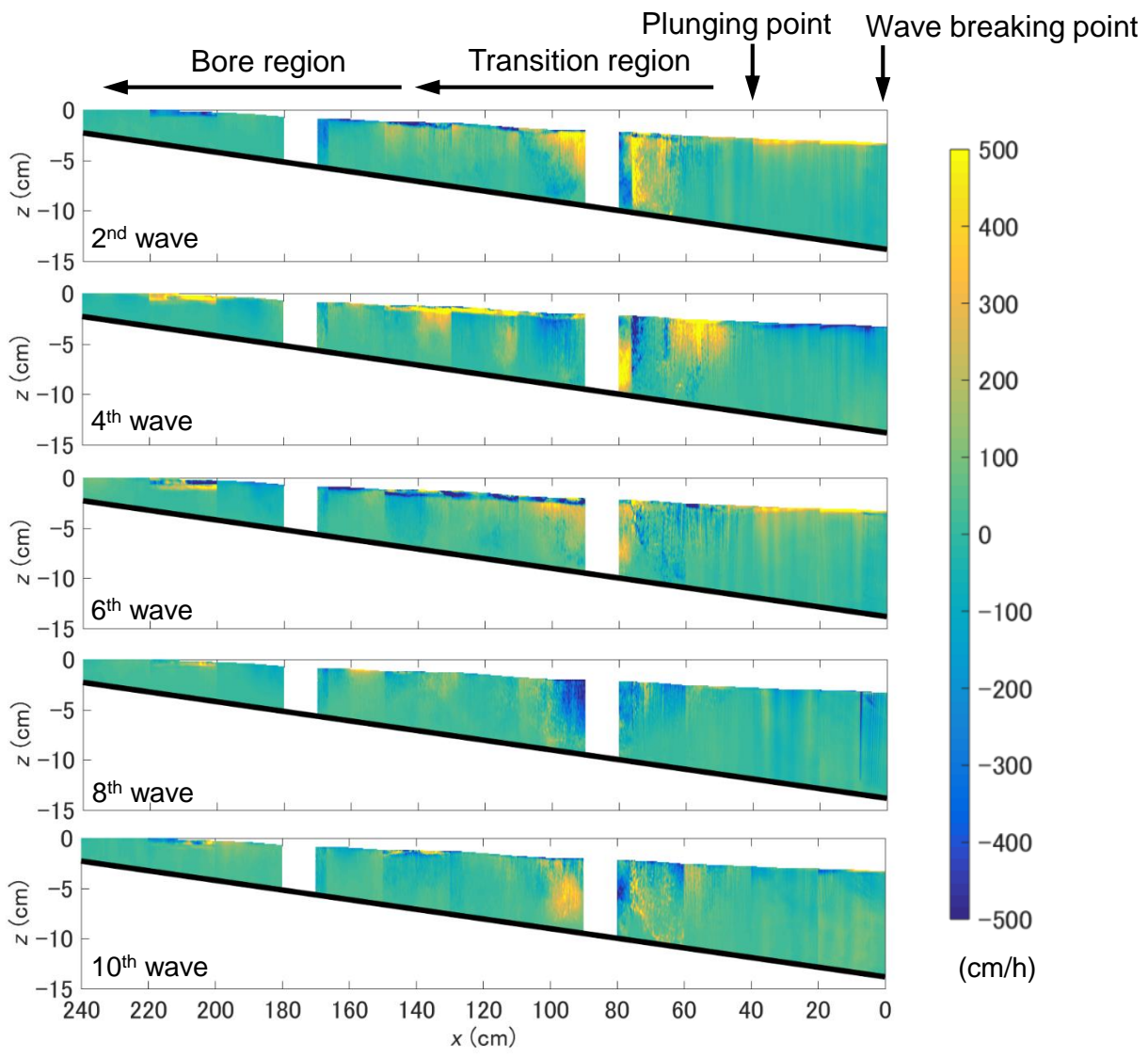
$H$ : wave height



- From eq.(1) to eq.(4), gas transfer velocity in a surf zone can be estimated in:

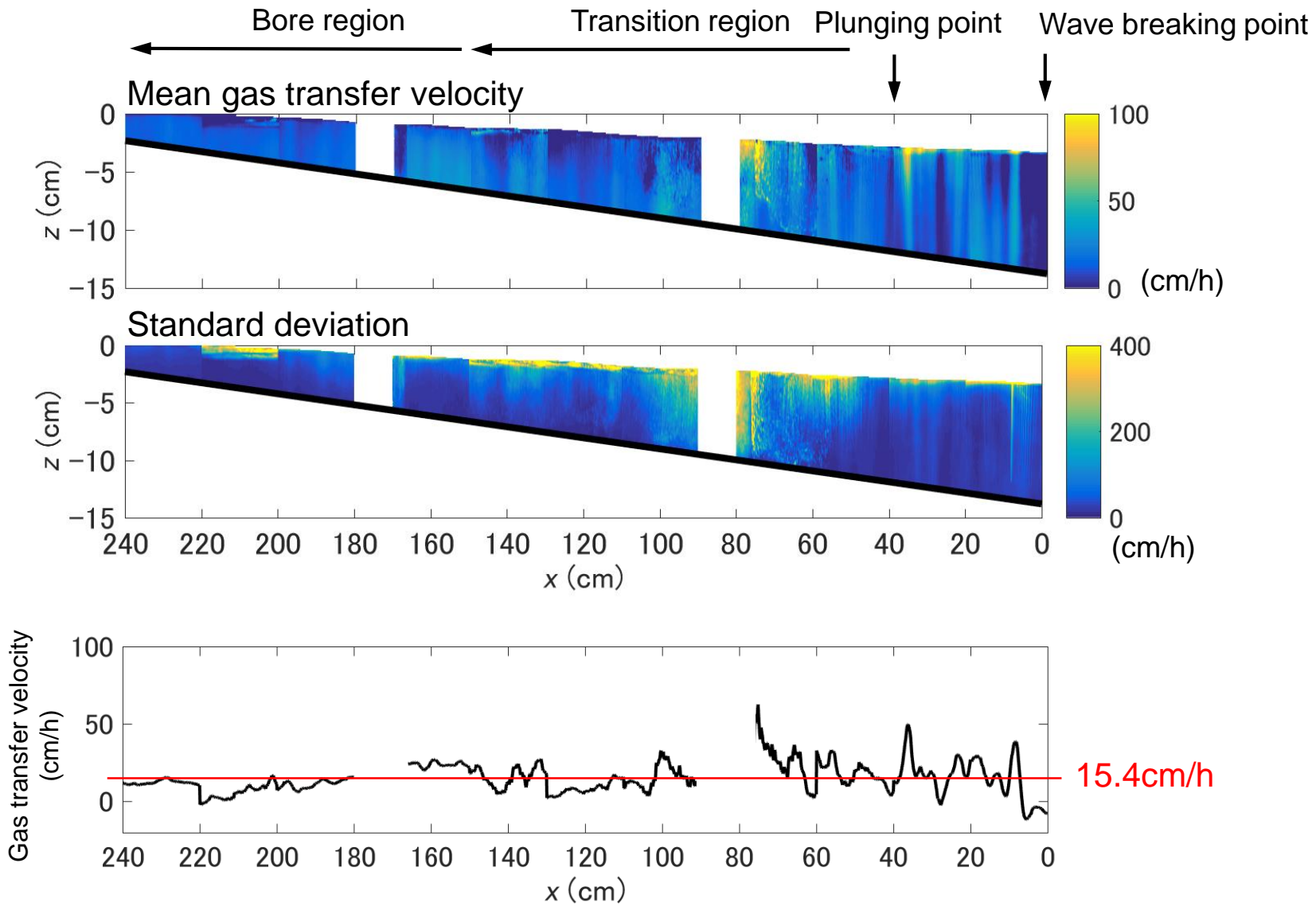
$$U = \frac{dC}{dt} \frac{H}{C_s - C_f} \quad (5)$$

# Gas transfer velocity in the surf zone



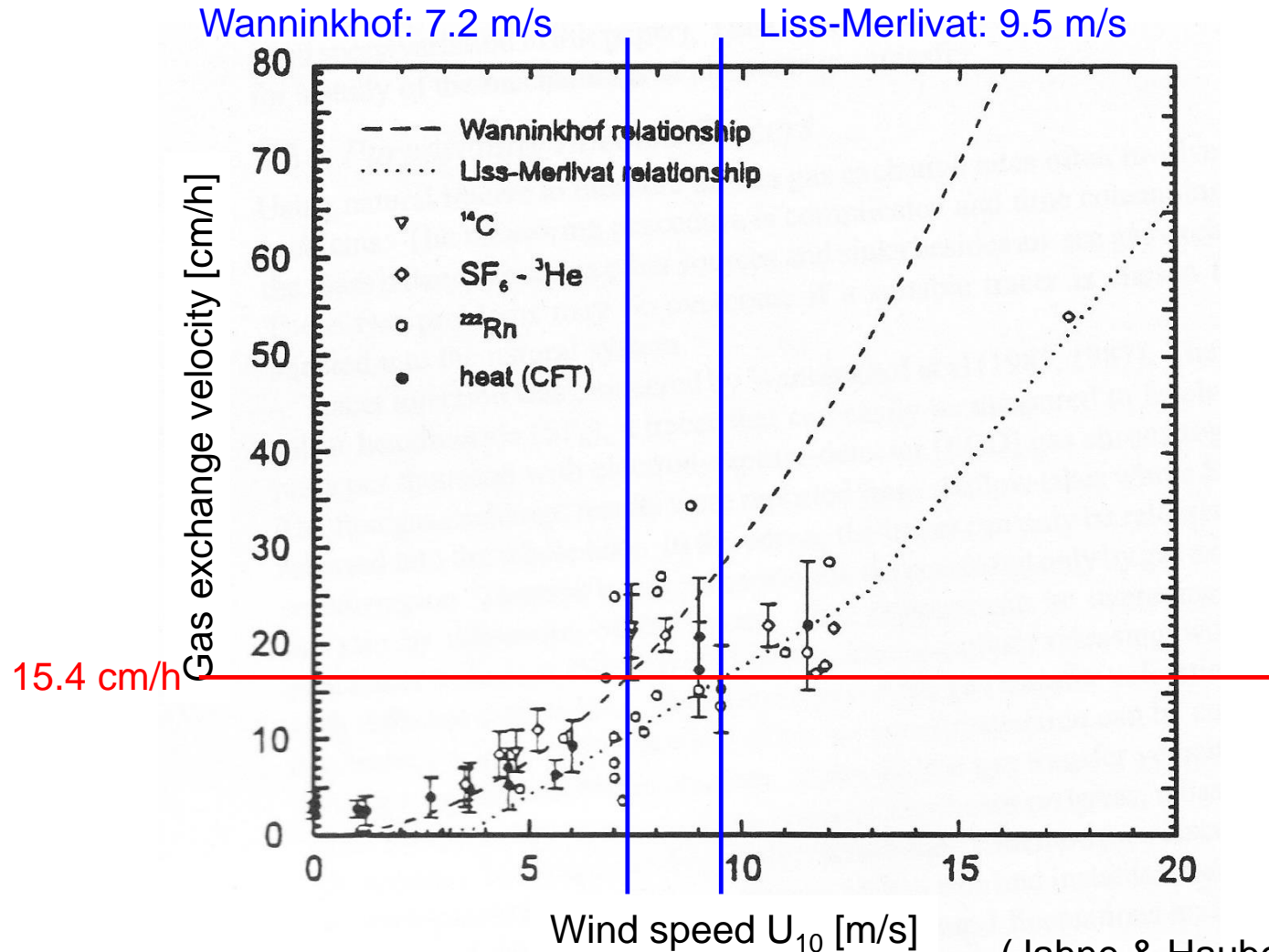
# Gas transfer velocity in the surf zone

Mean gas transfer velocity averaged over 10 waves



# Gas transfer velocity in a surf zone

Gas transfer velocity over the surf zone: 15.4 cm/h



(Jahne & Haubecker, Annu Rev Fluid Mech, 1998)



# Conclusions

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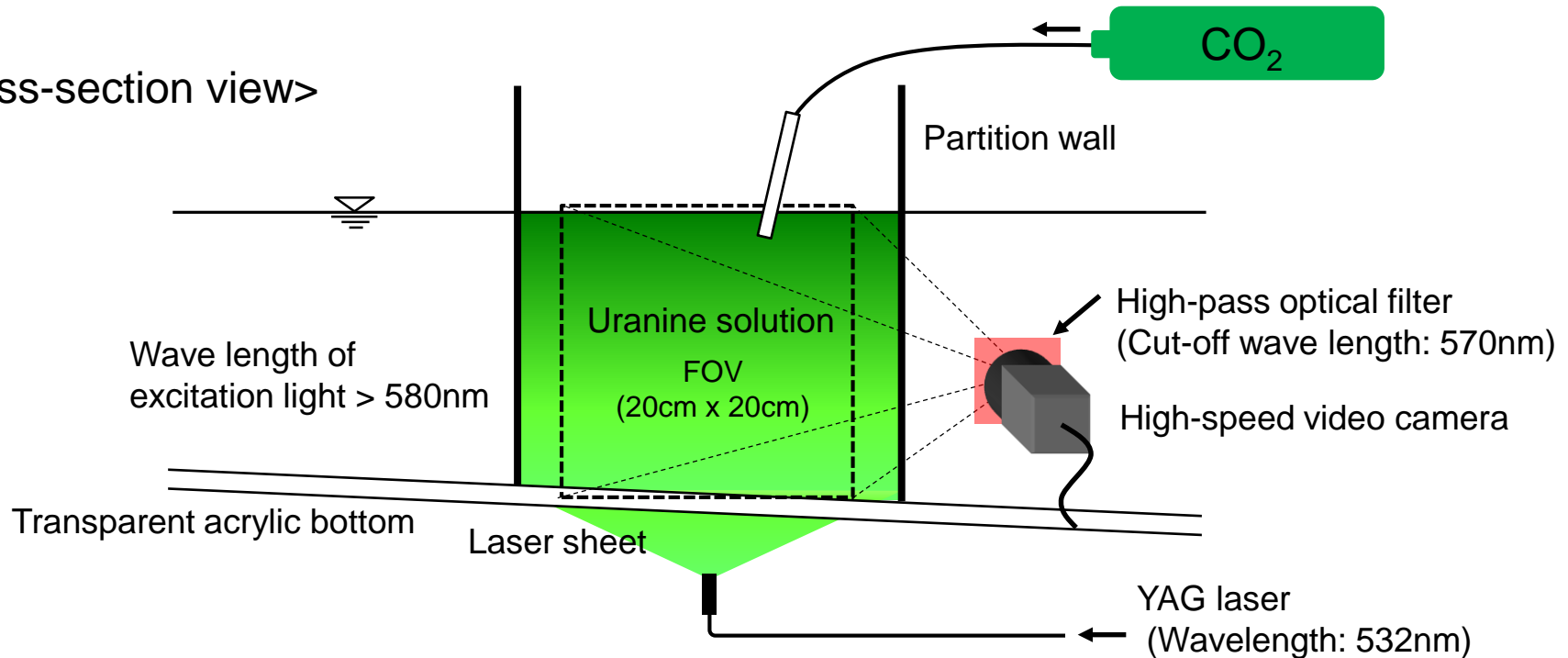
- ◆ DCO<sub>2</sub> concentration and air-water turbulent flow field in a surf zone were measured using LIF, PIV and LED backlight.
- ◆ In the transition region, local gas supply due to entrained bubbles was very active. However, spatial concentration does not increase in a short time because the local dissolved gas is mixed in the deep water mass by strong turbulence.
- ◆ In the bore region, the concentration increases in a short time because water is shallow. Undertow transports the concentrated DCO<sub>2</sub> toward the wave breaking point through near the bottom.
- ◆ While entrained bubbles and turbulent mixing have important roles in local gas transfer, undertow is contribute to the steady gas transfer from the bore region to the wave breaking point.



# LIF measurement for $\text{DCO}_2$ concentration field

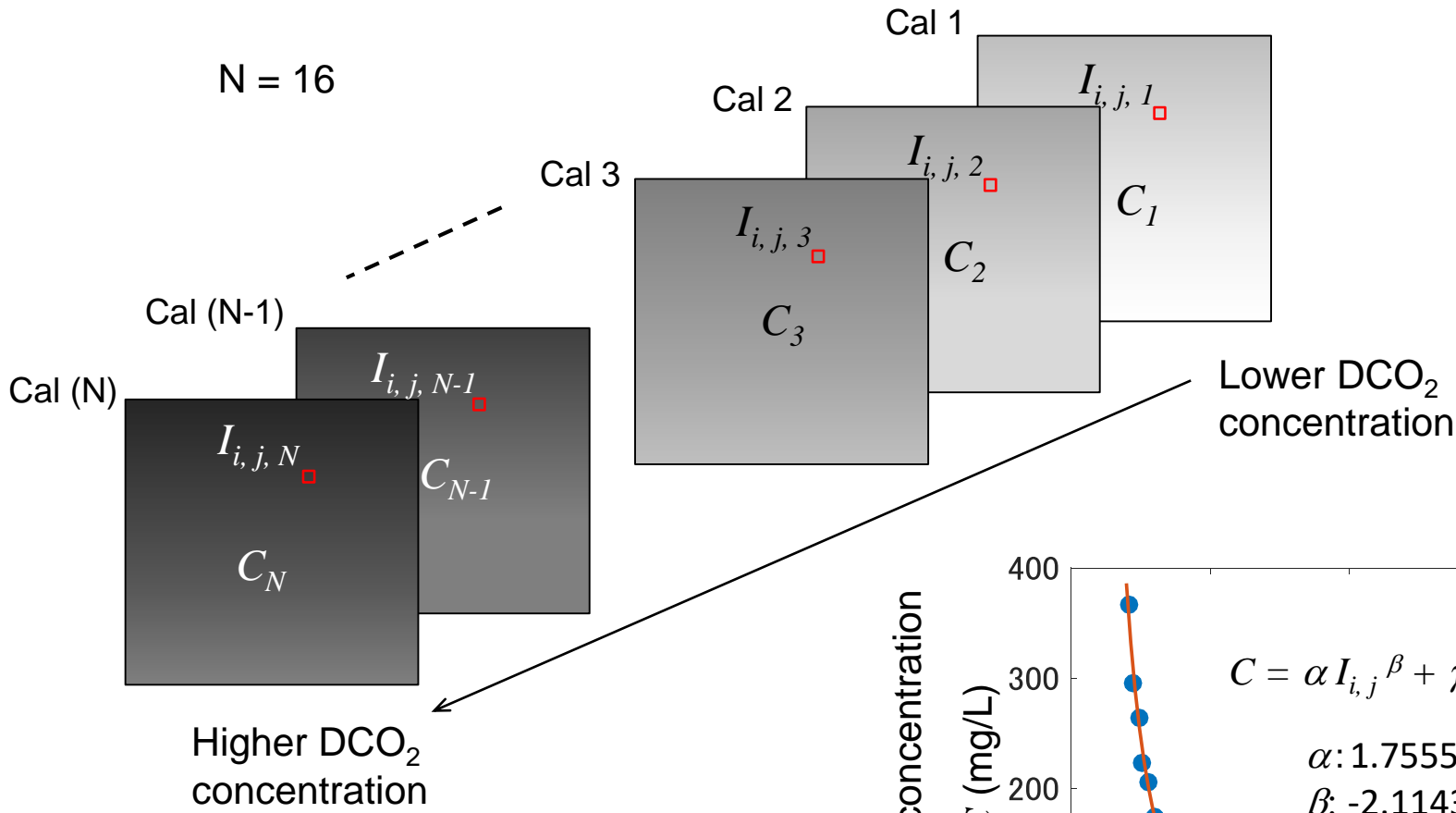
## Calibration method

<Cross-section view>



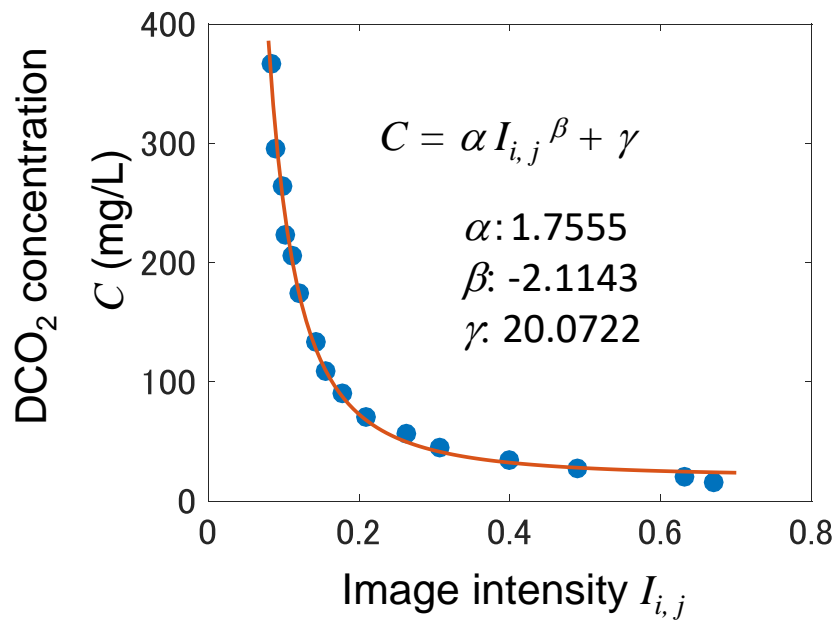
1. Adding  $\text{CO}_2$  into water.
2. Stirring uranine solution until the fluorescence intensity became spatially uniform.
3. Measuring bulk  $\text{DCO}_2$  concentration using a grass electrode  $\text{CO}_2$  meter.
4. Recording an image of fluorescence intensity.

# LIF measurement for DCO<sub>2</sub> concentration field



$I_{i,j}$ : Fluorescence intensity at an individual pixel

$C_n$ : Bulk DCO<sub>2</sub> concentration in a calibration area



# Gas transfer velocity estimated from mean turbulent energy

Gas transfer velocity estimated from turbulent energy:

$$U = \sqrt{K}/S_c$$

$K$ : Mean turbulent energy ( $\text{cm}^2/\text{s}^2$ ).

$S_c$ : Schmidt number (600).

