CHAPTER 114

Estimating the Sliding Distance of Composite Breakwaters
due to Wave Forces Inclusive of Impulsive Forces

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Abstract

Estimating the sliding distance is essential in the future probabilistic design of caisson breakwaters. In this paper, characteristics of the sliding phenomena are described, and a method based on the equivalent sliding forces to calculate the sliding distance is proposed. This calculation method is applicable for both impulsive and ordinary wave forces considering the shear force at the bottom of the caisson.

1. Introduction

Composite type breakwaters consisting of a rubble mound foundation and upright section have several advantages over conventional rubble mound breakwaters, since they are more stable, can be constructed faster and easier, and also reduce wave transmission.

In the conventional design process of a composite breakwater, the sliding stability of the caisson is evaluated by the sliding safety factor (S.F.). However, even if the S.F. is below 1.0, the breakwater can still maintain its function if the sliding distance is small. Consequently, to ensure economical design, it is necessary to determine the expected sliding distance occurring in the return period of the caisson.

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Ito, Fujishima, and Kitatani (1966) conducted the research on the stability of breakwaters and proposed the concept of the expected sliding distance. Horikawa, Ozawa, and Takahashi (1972) also discussed the expected sliding distance of high mound composite breakwater. However, it was difficult to estimate the wave pressure precisely, much more the sliding distance at that time.

Tanimoto, Kimura, and Miyazaki (1988) calculated the sliding distance based on the fourth order finite standing wave theory. This calculation is applicable for non-breaking wave conditions in deepwater area.

Goda (1974) developed a new wave pressure formula which included an impulsive pressure. This formula is quite useful and has become the standard method to obtain wave pressure against a vertical wall, although discrepancies arise under some impulsive pressure conditions. Takahashi, Tanimoto and Shimosako (1993, 1994b) proposed an impulsive pressure coefficient obtained by a re-analysis of the results of comprehensive sliding tests, which is introduced into the Goda pressure formula.

Takayama and Fujii (1991) carried out the probabilistic estimation of stability of sliding which considered the probabilistic property of wave height, wave pressure and friction coefficient between caissons and rubble mound. However, caisson's sliding distance was not included.

In order to estimate the caisson's sliding distance, the complex phenomena including the dynamic response of a breakwater caisson due to impulsive wave forces must be quantified. In the present study, model experiments with some non-linear FEM calculations to elucidate the characteristics of the dynamic response are described. A method is proposed to calculate the sliding distance, which is applicable for both impulsive and ordinary wave forces considering the shear force.

2. Present Design Method and Formulation of Caisson's Sliding

Present Design Method

The design wave forces acting on the caisson's upright section can be obtained using the Goda pressure formula. The present design method for determining the sliding stability is shown as follows:

\[ S.F. = \mu(W' - U)/P \] (1)

The safety factor for sliding \( S.F. \) is represented by the ratio of the friction resistance \( \mu(W' - U) \) to the horizontal wave force \( P \), where \( \mu \) is the friction coefficient between the caisson and rubble mound, \( W' \) is the caisson weight in water, and \( U \) is the uplift force. When \( S.F. \) is less than 1.0, the caisson is considered to be in an unstable condition. However, even if \( S.F. \) is less than 1.0, the breakwater can still maintain its function providing the sliding distance is small.
In order to optimize the design from an economical standpoint, we must determine the expected sliding distance occurring in the return period of the caisson. However, the sliding distance cannot be estimated using the present design method.

**Equation of Motion of Caisson**

Figure 1 shows the forces that act on the caisson when it is sliding. $M_a$ is the added mass, $F_R$ is the frictional resistance force, and $F_D$ is the force related to sliding velocity including the wave-making resistance force.

The equation of motion representing caisson sliding is presented as follows:

$$ (W' + M_a) \ddot{x} = P - F_R - F_D $$  \hspace{1cm} (2)

where

$$ F_R = \mu (W' - U) $$ \hspace{1cm} (3)

In Eq.(2), $P$ represents horizontal wave force, but the effective force producing caisson's sliding, that is the shear force at the caisson bottom, $P$, should be used instead of $P$ in order to include the effect of dynamic response of caisson. Although the magnitude of impulsive pressure intensity is quite large, the shear force is greatly reduced due to the caisson's dynamic response which is discussed later. If wave pressure is not impulsive, the shear force is equal to the horizontal wave force.

![Figure 1 Forces acting on the caisson in sliding.](image-url)
In our simplified sliding model, it is assumed that $\mu$ is constant before and during sliding, and that $M_a$ and $F_d$ are small enough to be neglected. Consequently, Eq.(2) is rewritten as follows:

$$(W/g)x = F_T + \mu U - \mu W^\prime$$

(4)

Caisson's Dynamic Response due to Impulsive Wave Forces

The magnitude of impulsive pressure intensity is quite large, being several times that of ordinary wave pressure. However, the shear force at the caisson bottom, which is the effective pressure producing caisson sliding, is greatly reduced due to the caisson's dynamic response. Figure 2a shows the experimentally determined impulsive wave force $P$, inertia force $m\ddot{x}_G$, shear force $F_T$, and displacement $x_G$, where the peak shear force is about 80% of the peak impulsive force. The ratio of the peak shear force to the peak impulsive force varies according to the peak value and duration time of $P$. Note that the stability of the sliding is not dependent on $P$ itself, but instead on $F_T$.

To reproduce the dynamic response of the caisson, we adopted a FEM calculation method named "the Bank Earthquake Analysis with Dynamic Water Pressure (BEAD)" (Uwabe, 1983). One advantage of the BEAD method is that it takes into account the pore water in the seabed and the surrounding water of the caisson. The equations utilized are a kind of Biot's equations. The BEAD program can simulate the behavior of the caisson, as well as that of the rubble mound and soil bed. The input data consists of the shear modulus, the Poisson ratio, and the permeability of the rubble mound and soil bed, as well as the input force on

![Figure 2a Experimental caisson response.](image-url)
the caisson. At each time step in the simulation, the acceleration, velocity, displacement, stress, and strain are evaluated. Figure 2b shows the corresponding FEM-calculated results using the same impulsive wave force, where good agreement is present with experimental results. (Takahashi, Tanimoto, and Shimosako, 1994a)

In actuality, sand bed and rubble mound are relatively soft in comparison with those of the model, and therefore, the dynamic response is much more significant. For instance, when applying the same impulsive force profile, the FEM-calculated ratio of the peak shear force to peak impulsive force under field conditions is about 40%, whereas about 75% in the 1/20 scale model.

Calculation Method of the Sliding Distance

The sliding distance of the caisson can be calculated by integrating the acceleration twice. Figure 3 shows the acceleration $\ddot{x}$, velocity $\dot{x}$, and displacement $x$ over time. $x$ can be calculated from Eq.(4) if the shear force $F_T$, uplift force $U$, friction coefficient $\mu$, caisson weight in water $W$ and in the air $W'$ are known. In the proposed model, we defined the equivalent sliding wave force $F_S$ as follows:

$$F_S = F_T + \mu U$$ (5)

The time series of $F_S(t)$ is considered to be a triangular pulse having a duration of $\tau_0$, which becomes smaller as the wave force increases. Figure 4 shows the time-dependent mathematical model used to simulate caisson displacement, where $F_S(t)$ is defined as follows:
$$F_s(t) = \begin{cases} 
(2t/\tau_0) F_{S_{\text{max}}} & (0 \leq t < \tau_0/2) \\
2(1-t/\tau_0) F_{S_{\text{max}}} & (\tau_0/2 \leq t < \tau_0) \\
0 & (t \geq \tau_0)
\end{cases}$$

Figure 3 Acceleration, velocity, and displacement of the caisson.

Figure 4 Proposed calculation model of the sliding distance.
The caisson begins to slide when $F_s(t)$ becomes larger than $\mu W$. $S_1$ indicates the sliding distance while $F_s(t)$ is larger than $\mu W$, and $S_2$ is that after $F_s(t)$ becomes smaller than $\mu W$. The total sliding distance $S$ is evaluated as follows:

$$S = S_1 + S_2 = \frac{g\tau_0^2 (F_{S_{\text{max}}} - \mu W)^3 (F_{S_{\text{max}}} + \mu W)}{8 \mu W W' F_{S_{\text{max}}}^2}$$

$F_{S_{\text{max}}}$ can be obtained by the Goda pressure formula, but we still must determine $\tau_0$ to evaluate $S$. We used theoretical analysis and model experiments to determine $\tau_0$. Consequently, $\tau_0$ is represented as follows:

$$\tau_0 = k \tau_{0F}$$

$$k = \frac{1}{(\alpha^* + 1)^2}$$

$$\alpha^* = \max \{\alpha_1, \alpha_2\}$$

$$\tau_{0F} = (0.5 - H/(8h))T \quad (0 \leq H/h \leq 0.8)$$

where $\alpha_1$ is an impulsive pressure coefficient (Takahashi, Tanimoto and Shimosako, 1993), $\alpha_2$ is a coefficient indicating the effect of impulsive pressure in Goda pressure formula, $H$ is wave height, $h$ is water depth, and $T$ is wave period. In non-breaking wave, $\tau_0$ is almost the same as $\tau_{0F}$, whereas for impulsive wave, $\tau_0$ is 0.1-0.2 s in the model experiment. Note that $\tau_0$ is determined based on the duration time of shear force. Actually, the duration time of impulsive pressure is much smaller than $\tau_0$.

3. Experiments

Experimental Procedure

Figure 5 shows a cross section of the caisson model which is made of synthetic acrylic plates and has its bottom comprised of a concrete slab that simulates the friction factor. Additional concrete blocks were placed in front of the caisson to generate impulsive wave pressures. Seven pressure transducers and a load cell are attached to the front plate to measure the applied wave pressure and force. Two acceleration meters and two displacement meters measure caisson movement. The caisson was mainly subjected to regular waves with a period $T = 3.04$ s.

Sliding tests using both impulsive and non-breaking waves were conducted with the same caisson model and wave conditions. Based on the wave force, caisson weight was accordingly adjusted by putting lead weights inside it.
Sliding due to Non-breaking Wave Forces

Figure 6 shows typical recorded profiles of non-breaking wave. $P$ is the horizontal wave force, $U$ is the uplift force, and $F_s$ is the equivalent sliding wave force as mentioned before. $x_{\text{GEXP}}$ indicates the displacement of the caisson's center of gravity, while $S_{\text{CAL}}$ is the calculated sliding distance. $S_{\text{CAL}}$ is calculated from the measured $F_s$ and $x_0$ calculated from Eq.(8)-(11). The caisson starts to move before when $F_s$ becomes larger than $\mu W'$. This is because $x_{\text{GEXP}}$ includes the elastic displacement of rubble mound and soil bed. Actually, it is considered that the caisson starts to slide when $F_s$ becomes larger than $\mu W'$, and it stops when $x_{\text{GEXP}}$ is
maximum. Notice that the elastic displacement continues until $F_s$ becomes 0. The residual displacement of $x_{GEXP}$ is slightly smaller than $S_{CAL}$.

Figure 7 shows a typical wave pressure distribution for a non-breaking wave as measured by a model experiment. The solid lines show the design wave pressure distributions calculated by the Goda pressure formula. Note the horizontal wave pressure distribution is almost uniform, except near the top of the caisson. In addition, the measured and calculated pressures indicate good agreement.

**Sliding due to Impulsive Wave Forces**

Figure 8 shows typical profiles recorded for an impulsive wave force hitting the caisson, where $m\ddot{x}_G$ indicates the inertia force, and $F_T$ is the shear force ($= P - m\ddot{x}_G$). The peak value of $F_T$ is smaller than that of $P$, and when $m\ddot{x}_G$ is negative peak, $F_T$ is larger than $P$. Displacement begins at the same time when impulsive pressure starts, and it peaks after $P$ becomes smaller than $\mu W'$. The elastic motion is found just as non-breaking wave, however, it stops before $F_T$ becomes 0. Therefore, the caisson does not move in the wave period, but the oscillation period of it. Good agreement is present between $S_{CAL}$ and $x_{GEXP}$, although the residual displacement of $x_{GEXP}$ is slightly smaller than $S_{CAL}$. 
Figure 8 Recorded profiles of the impulsive wave.

Figure 9 Wave pressure distribution of the impulsive wave.
Figure 9 shows a typical wave pressure distribution for an impulsive wave. The solid lines and the dotted lines are design wave pressure distributions calculated by the Goda pressure formula using and not using the "Impulsive Pressure Coefficient" respectively. Note the calculated value by the Goda pressure formula is much smaller than measured pressure. However, the shear force at the caisson bottom, which is the effective pressure producing caisson sliding, is greatly reduced due to the caisson's dynamic response as described before. The "Impulsive Pressure Coefficient" is determined based on the result of sliding experiments in order to represent the effective sliding force.

Sliding Distance

Figure 10a compares the experimental and calculated results of sliding distance $S$ versus the sliding safety factor $S.F.$ for a non-breaking wave. Calculated results is obtained from the peak value of the measured equivalent sliding wave force $F_s$ and the calculated of $\tau_0$ (not measured $\tau_0$). Note that the sliding distance increases as the sliding safety factor decreases, and also that good agreement exists between the experimental and calculated results.

In the present design method, the friction coefficient $\mu$ is considered as 0.6. However, as $\mu$ scatters in the experiment, the sliding distance $S$ also scatters. Most of the experimental results are close to the calculations using $\mu = 0.5 \sim 0.7$.

Figure 10b shows the corresponding results for an impulsive wave. Notice it has almost the same general characteristics as the non-breaking wave. However, at the same sliding safety factor value, the sliding distance for the impulsive wave is smaller.

![Figure 10a Sliding distance as a function of the sliding safety factor. (Non-breaking wave)]
4. Estimation of Expected Sliding Distance

Calculation Procedure of Expected Sliding Distance

In the future breakwater designs, calculation method of expected sliding distance should be established to allow some sliding of the caisson. In that case, the proposed method should be extended to estimate the expected sliding distance.

Goda pressure formula with the impulsive pressure coefficient and the calculation model of the sliding distance can be applied as they were mentioned. In addition, all wave data during its return period are needed to calculate the expected sliding distance, and the probabilistic property of wave height, wave force, water level, friction coefficient, and caisson weight should be taken into consideration.

Sample Calculation

As an example, using 9-year wave data observed at a certain point, the expected sliding distance is calculated for a caisson breakwater. Figure 11 shows the cross section of the designed breakwater. The return period of the breakwater is usually 50 years, however, only 9-year observed wave data is used, and the fluctuation of wave force, friction coefficient, etc. are not considered.

Figure 12 shows the wave height distribution expressed in the form of probability density. Using the significant wave height, each wave height is reproduced according to the Rayleigh distribution. The number of waves which is larger than a certain wave height can calculate from this distribution. For instance, the number of waves which is larger than 12.1 m is 3.7, and that larger than 10.5 m is 36.3, where 12.1 m is the maximum significant wave height, and 10.5 m is the
average value of the annual maximum significant wave heights for 9 years. The total number of waves during 9 years is almost 32.7 million.

Figure 13 shows the relation between wave height and sliding distance for one wave in various design wave heights. When the design wave height $H_D = 12.1$ m and sliding safety factor $S.F. = 1.0$, the sliding distance at $H = 18.0$ m is 72 cm.

The expected sliding distance for 9 years can be obtained using the sliding distance for one wave and the probability density of wave height. Figure 14 shows the relation between the design wave height and the expected sliding distance caisson for 9 years. The wave height distribution and the sliding distance for one wave are also shown in this figure. For instance, when the design wave heights $H_D$ are 12.1 m and 10.5 m, the probable sliding distances are 0.6 cm and 45 cm, respectively.
5. Concluding Remarks

A practical method was derived to estimate the sliding distance due to wave forces including impulsive ones. In future breakwater designs, probabilistic design method should be adopted to ensure economical considerations are optimized. Subsequent research will be directed at extending the proposed sliding model to estimate the sliding distance of the caisson during its return period considering the fluctuation of wave force, friction coefficient, and caisson weight.
References


