



# 36TH INTERNATIONAL CONFERENCE ON COASTAL ENGINEERING 2018

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*The State of the Art and Science of Coastal Engineering*

## SIMULATION OF SEA STORMS INCLUDING MULTIVARIATE STORM EVOLUTION



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## □ Content

- Introduction (Motivation / Objectives )
- Methodology
- Application ( Results / Discussion)
- Conclusions

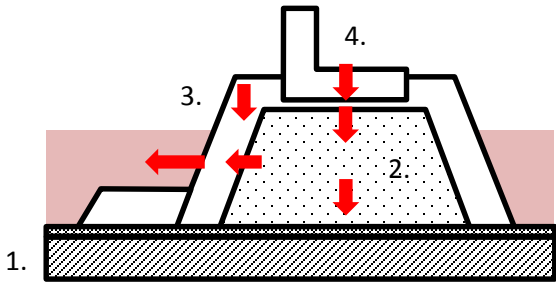


## □ Motivation

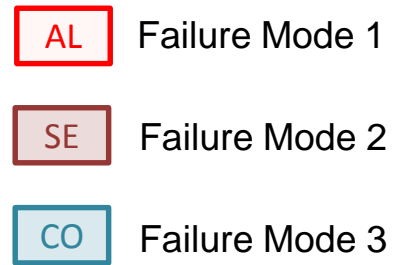
- The simulation of storms of met-ocean variables useful for probabilistic design and probabilistic coastal risk assessments (see e.g. Davies et al. 2017), and is required in case Damage Evolution is taken into account (ROM 1.1-18).



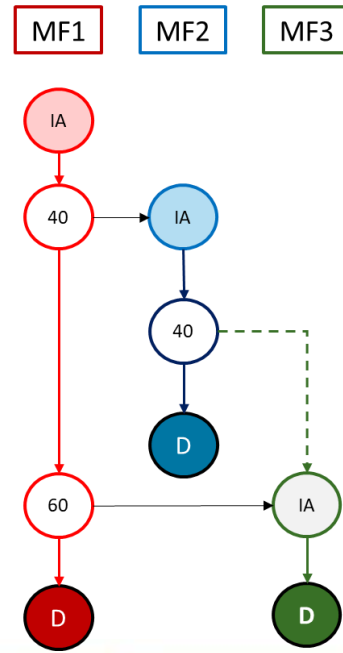
SLIDE BORROWED FROM 1468-"ACCUMULATED DAMAGE EVOLUTION AND INVESTMENT COSTS OF BREAKWATERS"  
FOLGUERAS ET AL. ; FRIDAY, AUGUST 3 ; 8:30 AM - 8:50 AM ; GRAND BALLROOM IX & X



1. Foundation and Terrain (FT)
2. Core (CO)
3. Armor Layer (AL)
4. Superstructure (SE)

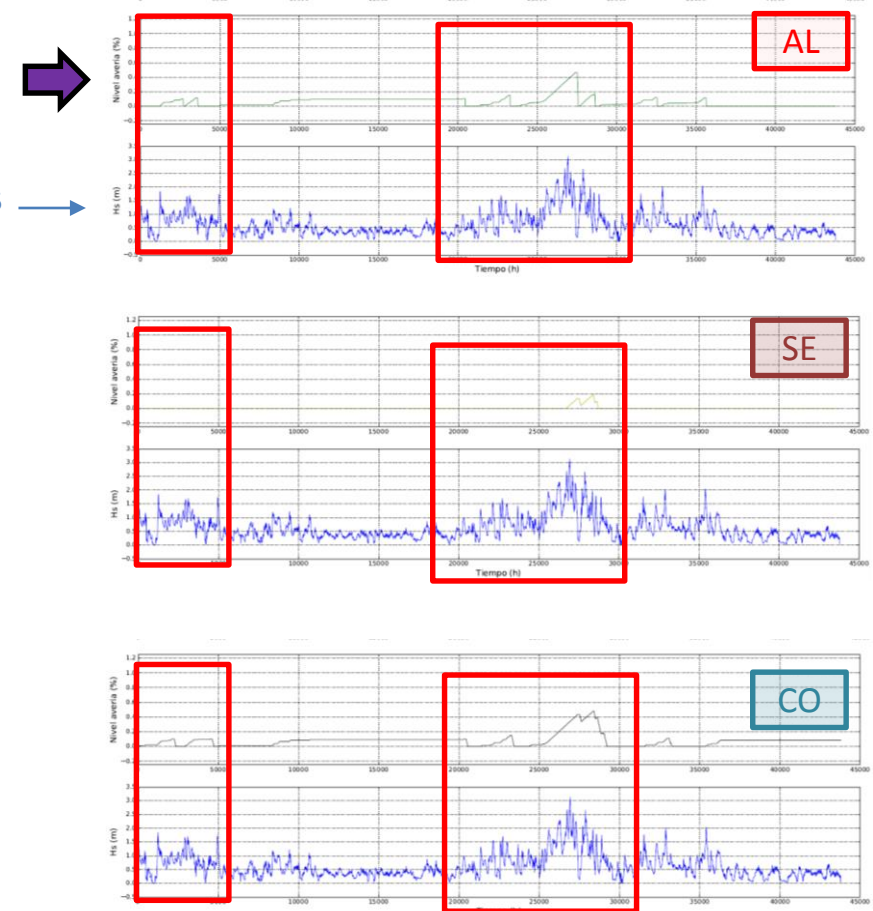


### DAMAGE PROPAGATION TREE



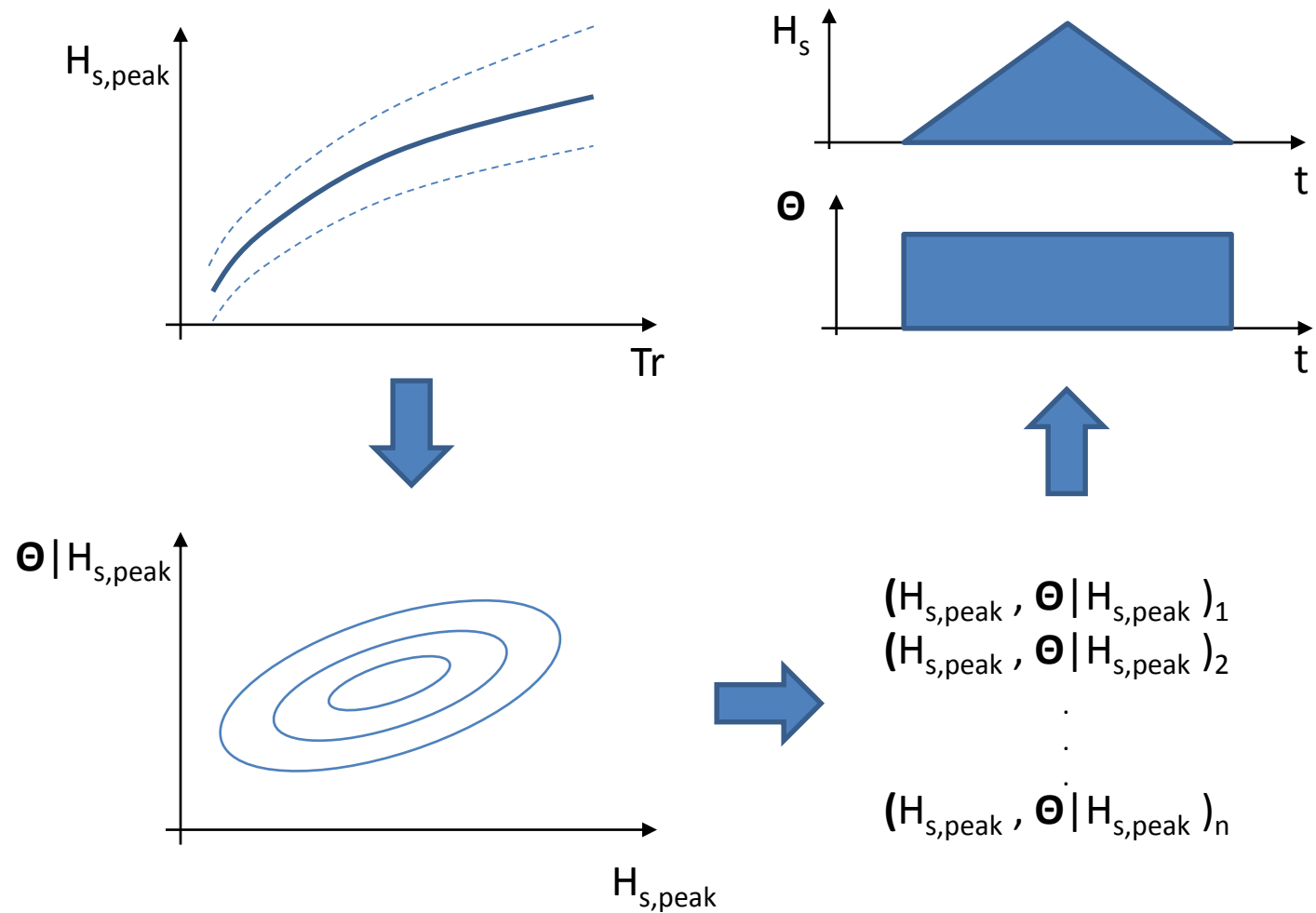
Damage Accumulation

Same time series of sea conditions

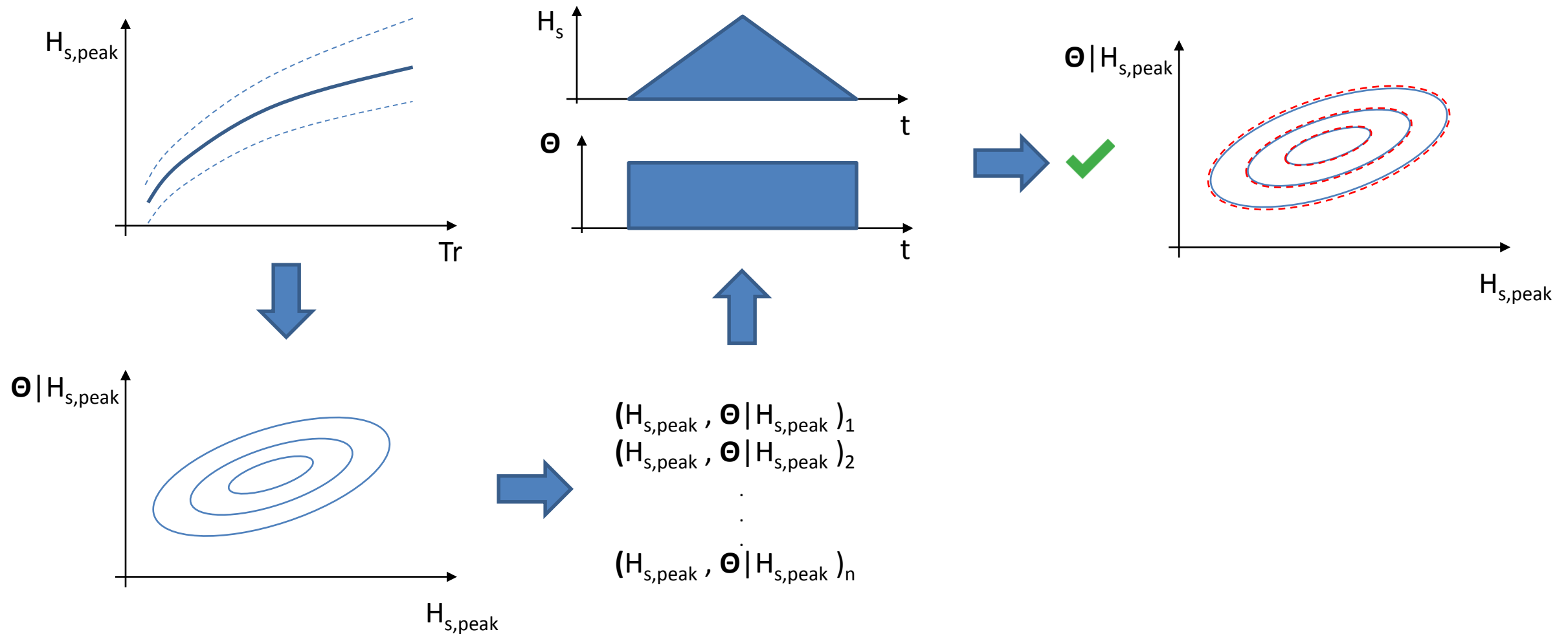




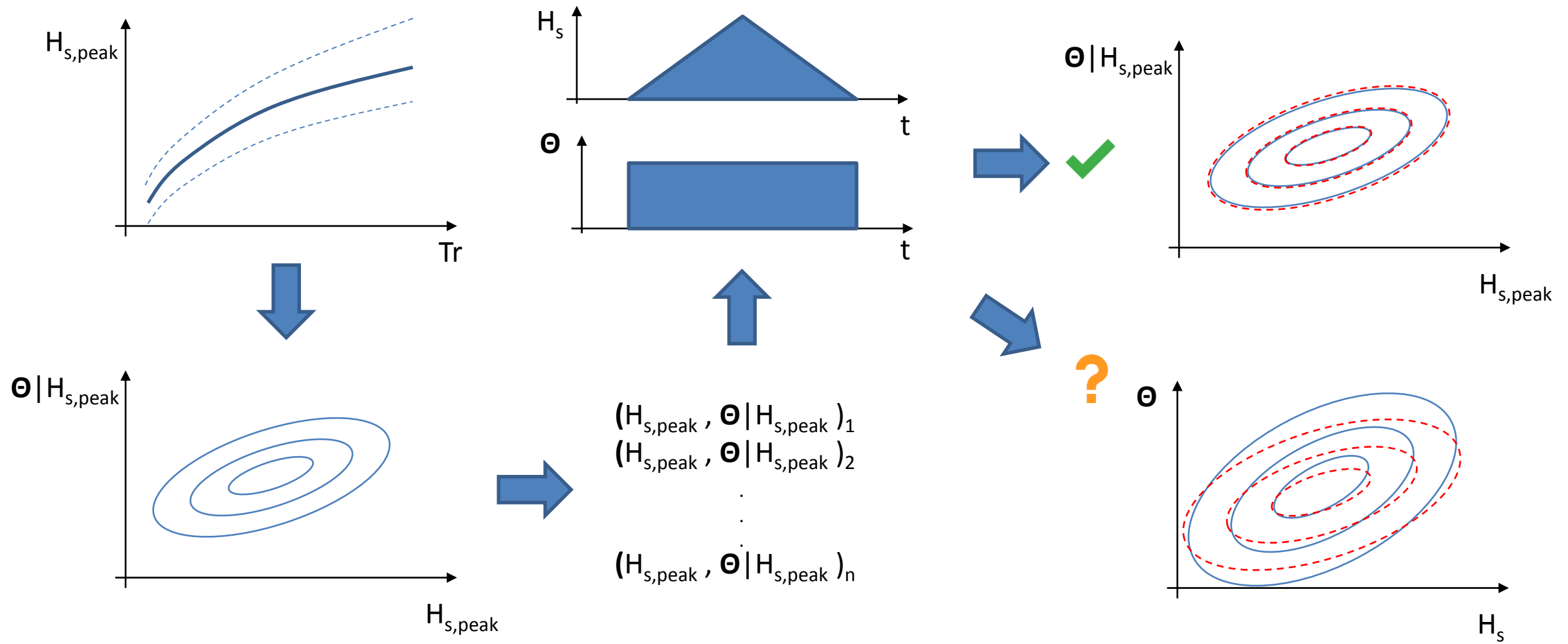
□ Motivation (traditional approach; Borgman 70's , Boccotti 90's)



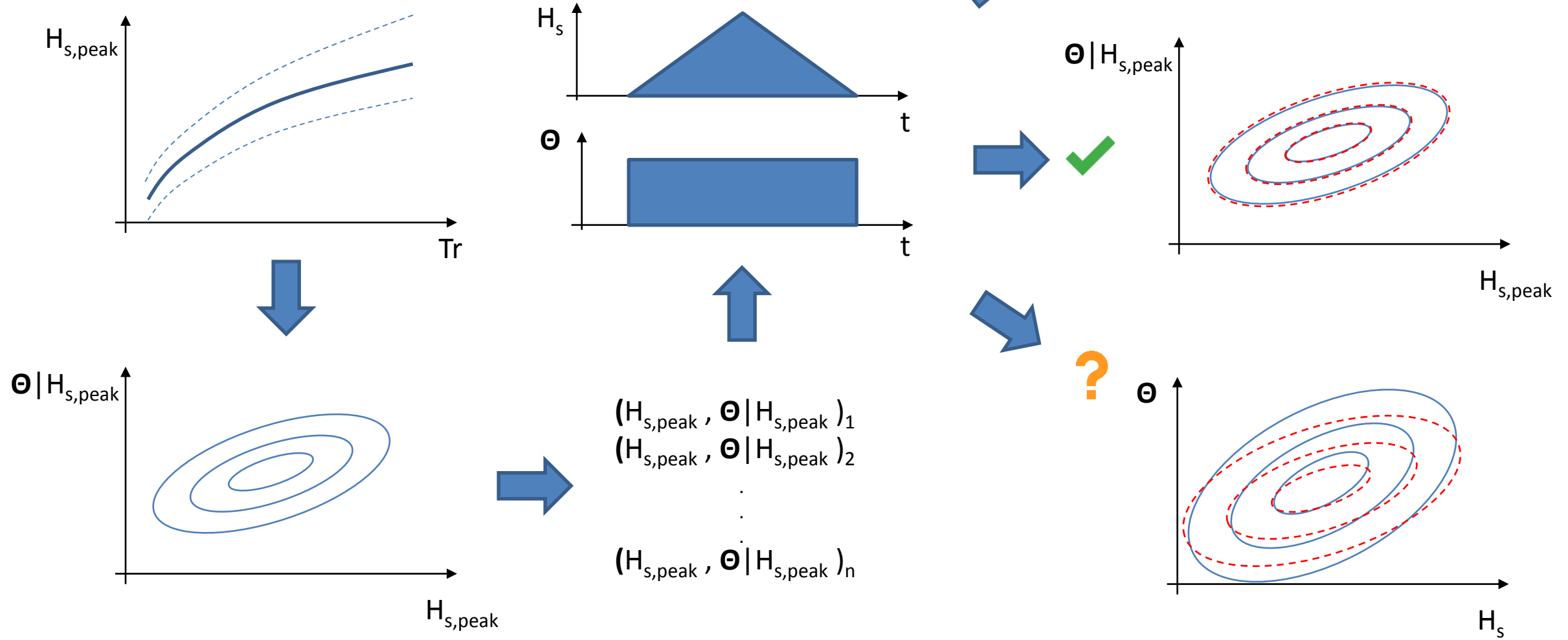
## □ Motivation



## □ Motivation



## □ Motivation





## ❏ Objectives

- To devise a methodology for multivariate sea storm simulations that:
  - Properly reproduces the multivariate distribution of the variables at storm peak, but...
  - also reproduces the multivariate distribution of all sea states included in the storm, and...
  - is capable of innovation in the storm evolution (for all variables involved).
- To test this methodology in a case study.



## ❏ Methodology

- Multivariate storm evolution given by an expected multivariate evolution plus multivariate noise
- Noise modeled using a Vector Autoregressive model
- Expected multivariate evolutions given by few form that cluster in the ( $H_{s,peak}$ -Duration) space



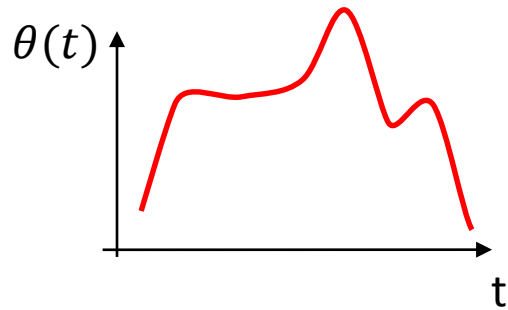
## ❏ Methodology

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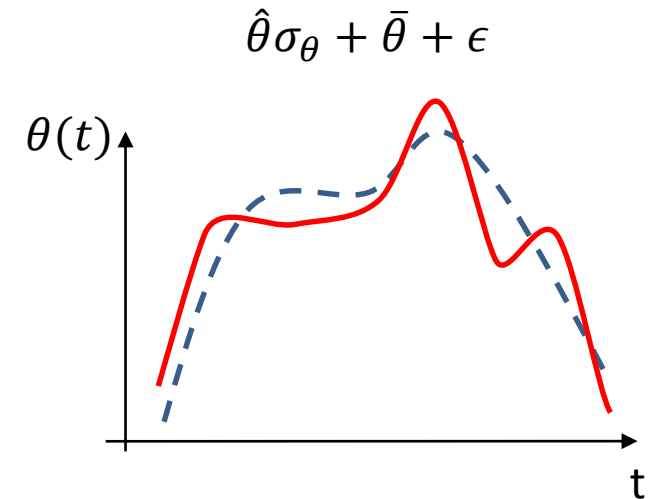
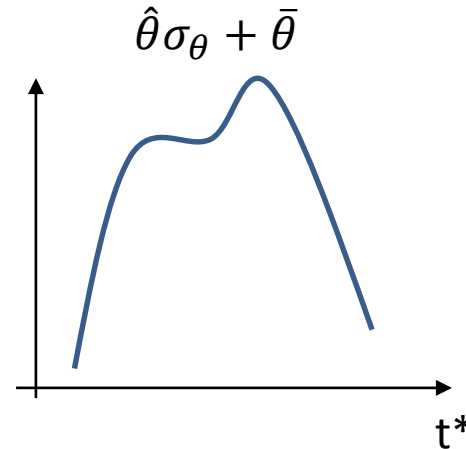
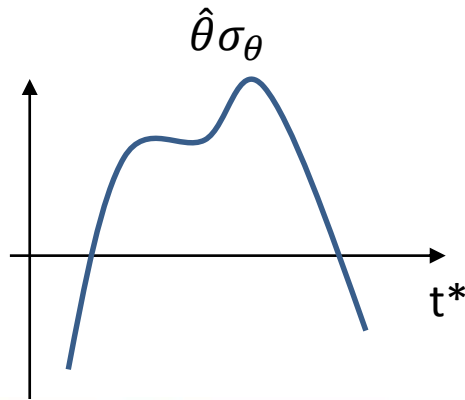
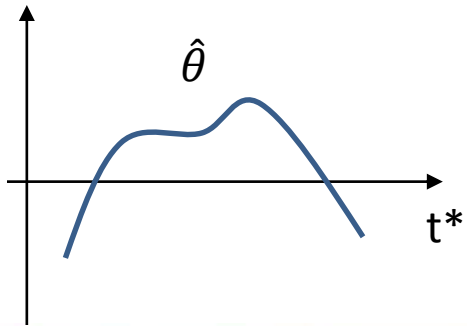


## Methodology

- Multivariate storm evolution given by an expected multivariate evolution plus multivariate noise



$$\theta(t) = \hat{\theta}(t)\sigma_{\theta} + \bar{\theta} + \epsilon(t)$$





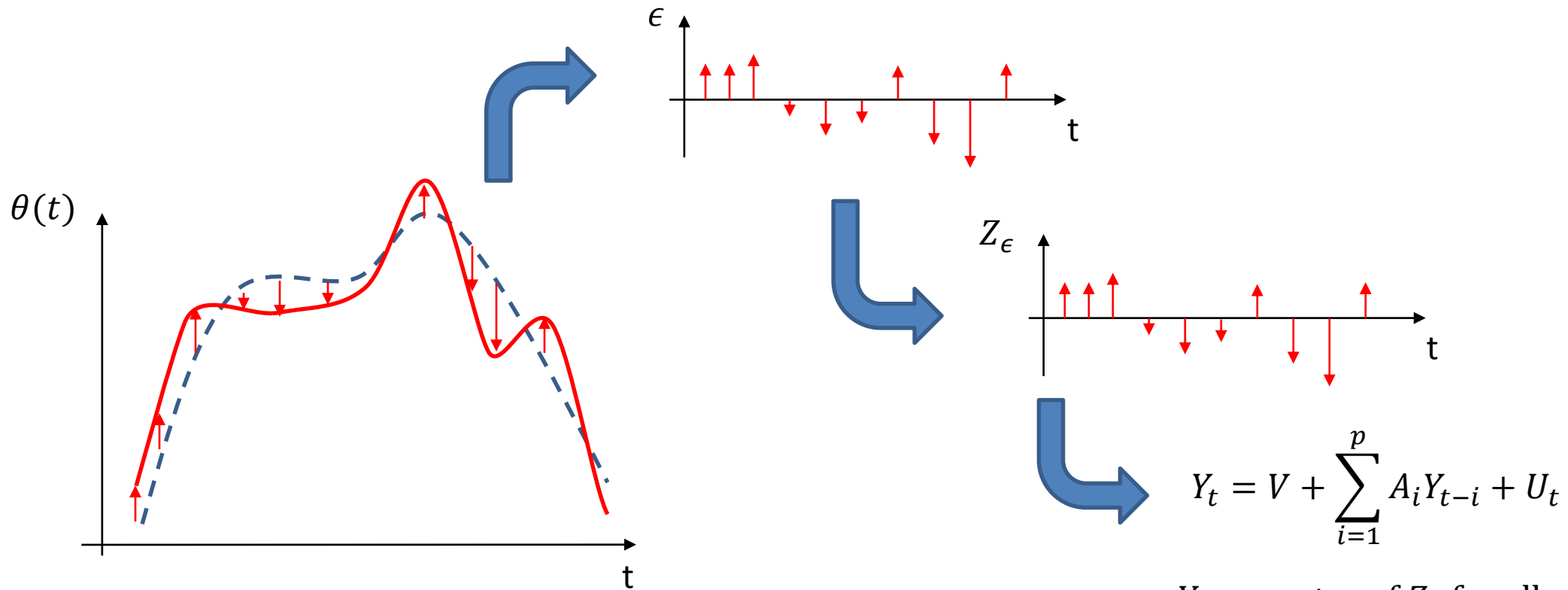
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## □ Methodology

- Noise modeled using a Vector Autoregressive model



$Y_t$  = vector of  $Z_\epsilon$  for all variables at time  $t$   
 $V, A_i$  = parameters of the VAR model  
 $U_t$  = multivariate normal noise



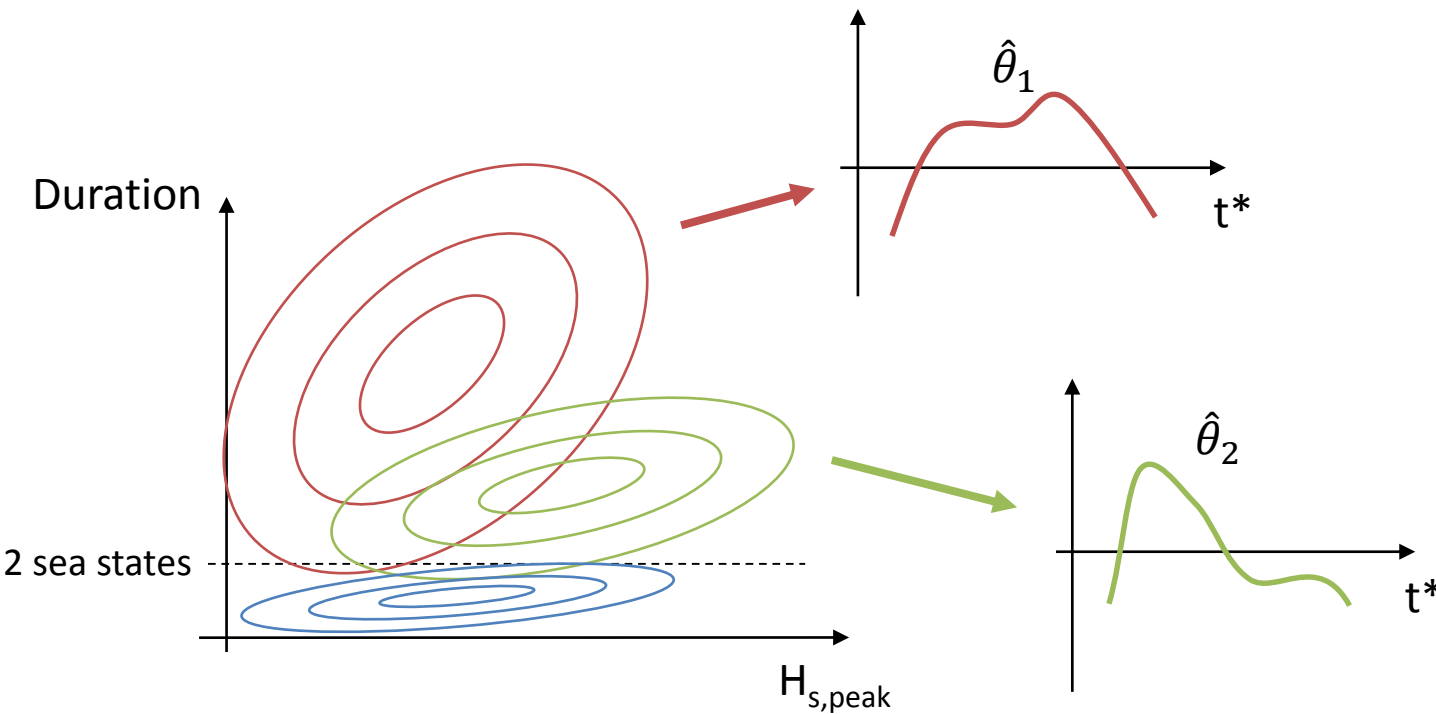
## ☐ Methodology

- Multivariate storm evolution given by an expected multivariate evolution plus multivariate noise
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## Methodology

- Expected multivariate evolutions given by few form that cluster in the ( $H_{s,peak}$ -Duration) space



Given  
( $H_{s,peak}$ -Duration)

$\downarrow$   
( $\pi_1, \pi_2, \pi_3$ )

where  $\pi_i$  is the probability of the storm having mean time evolution  $\hat{\theta}_i$





## □ Methodology

- In summary we need...

$$\theta(t) = \hat{\theta}(t)\sigma_{\theta} + \bar{\theta} + \epsilon(t)$$

Multivariate mean (normalized) evolution forms  $\hat{\theta}$ , as obtained by cluster analysis of the data.

Probability of the mean forms conditional to  $H_{s\_peak}$  and *Duration*.

Marginals and joint distribution of  $H_{s\_peak}$  and *Duration*.

A VAR model for the noise of the storm evolution.

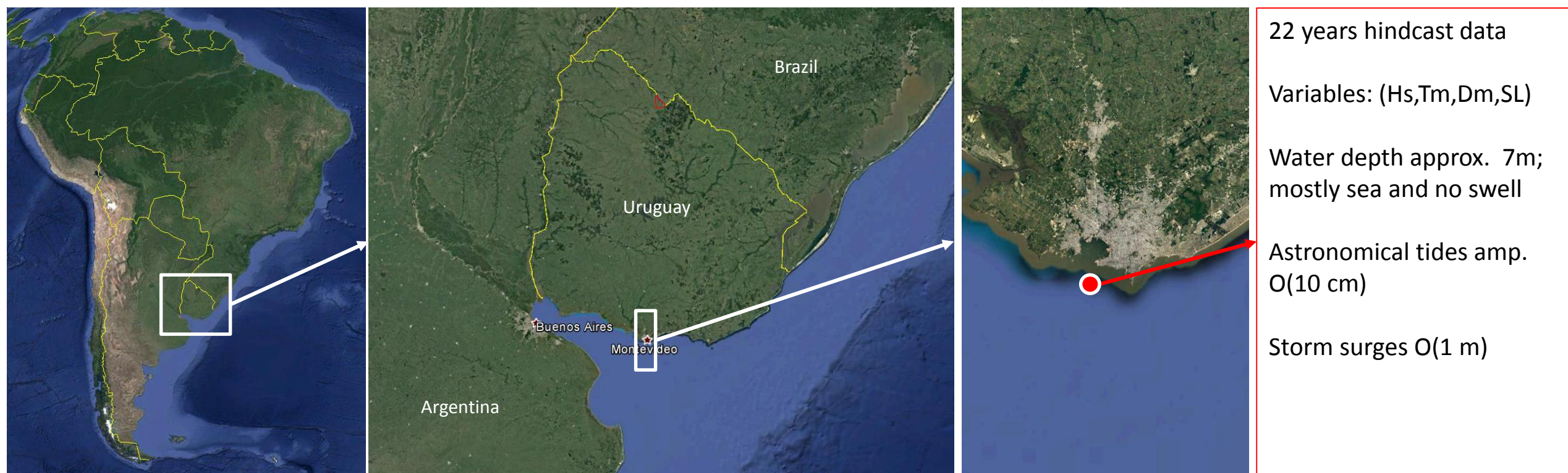
A model for the mean  $\bar{\theta}$  and the standard deviation  $\sigma_{\theta}$  of the storm evolution, for every variable involved (e.g. wave period, storm surge, etc.), conditional to  $H_{s\_peak}$  and/or *Duration*.

Could be one multivariate model or several bivariate models (by means of e.g. regression, copulas, etc.).



## □ Application

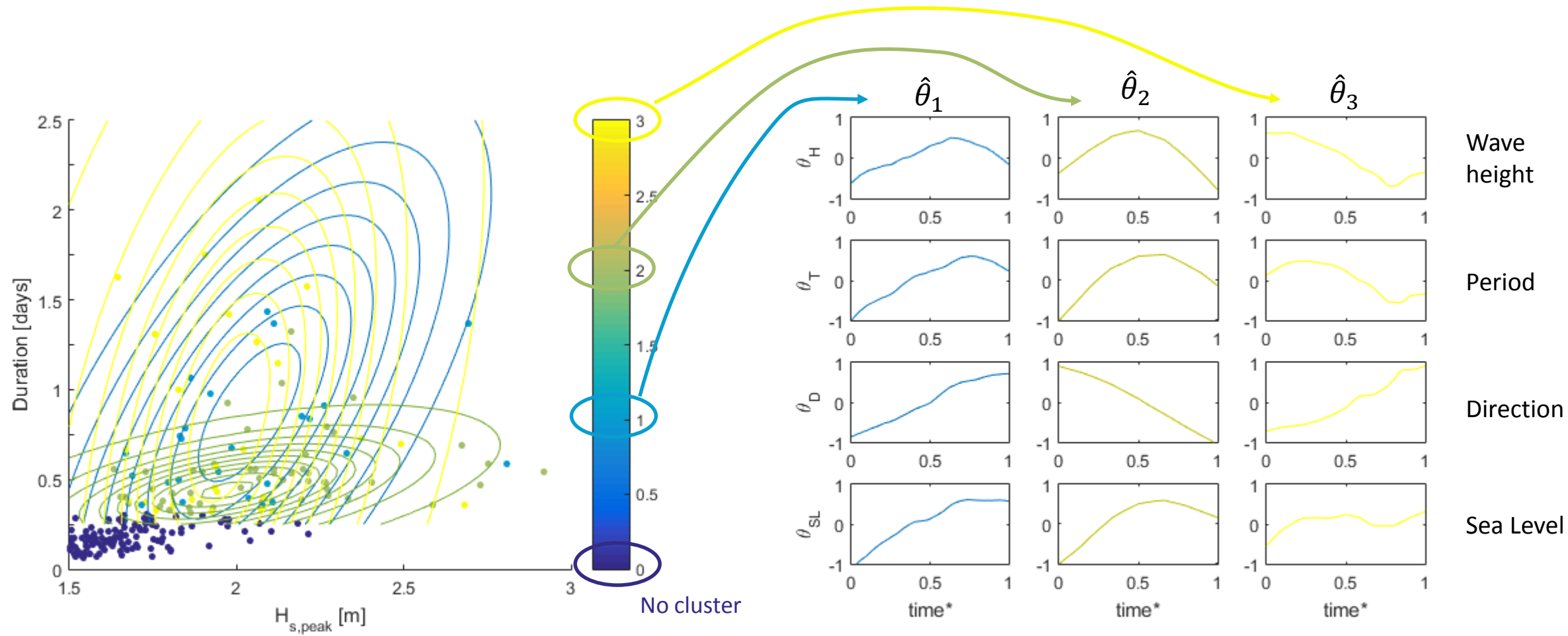
- Case study: Wave and total sea level hindcasts off Montevideo coast, in Rio de la Plata estuary



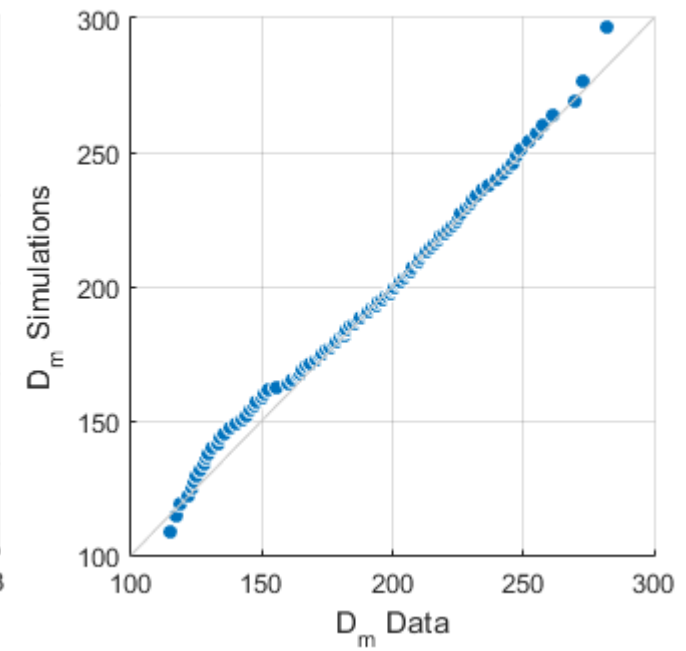
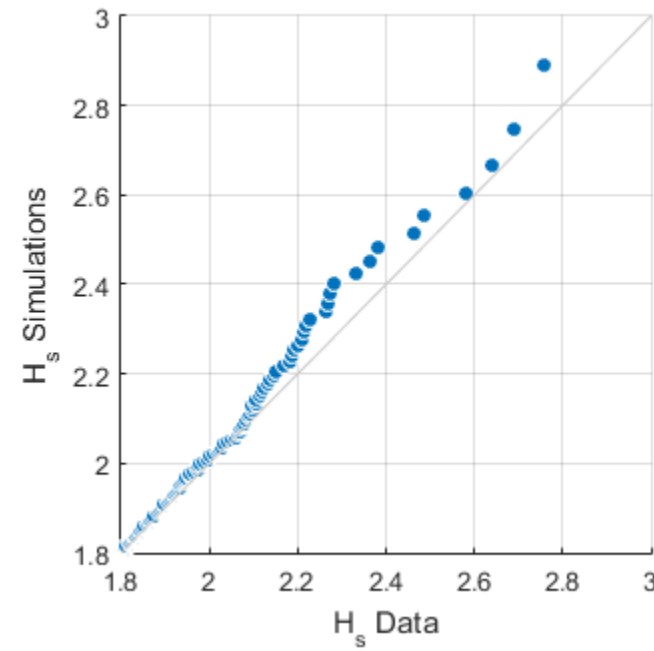
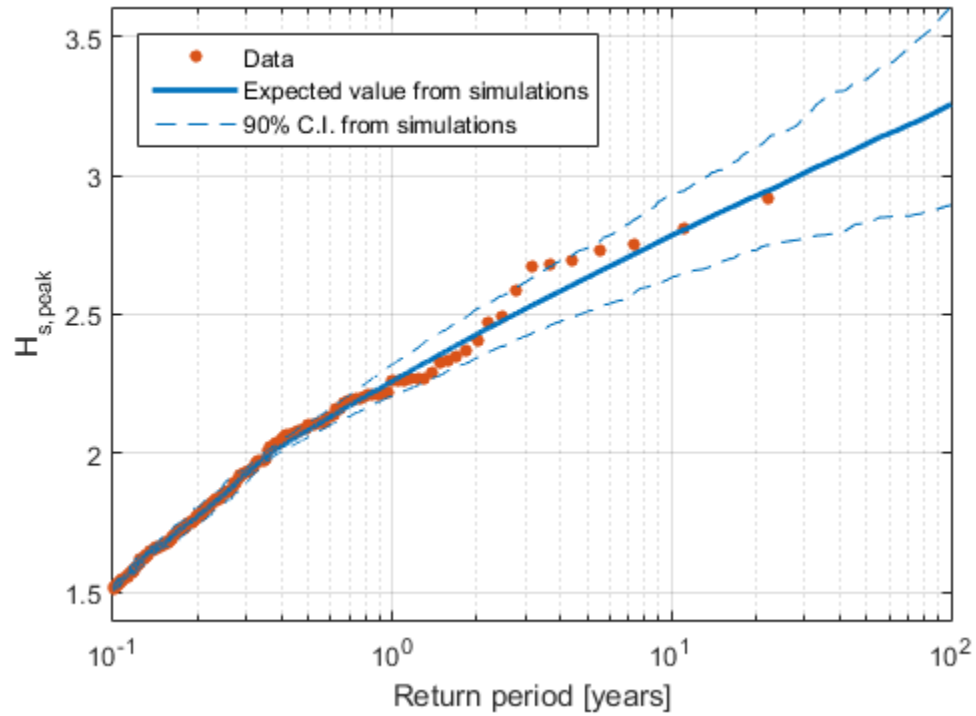


## Results and discussion

$$\theta(t) = \hat{\theta}(t)\sigma_{\theta} + \bar{\theta} + \epsilon(t)$$



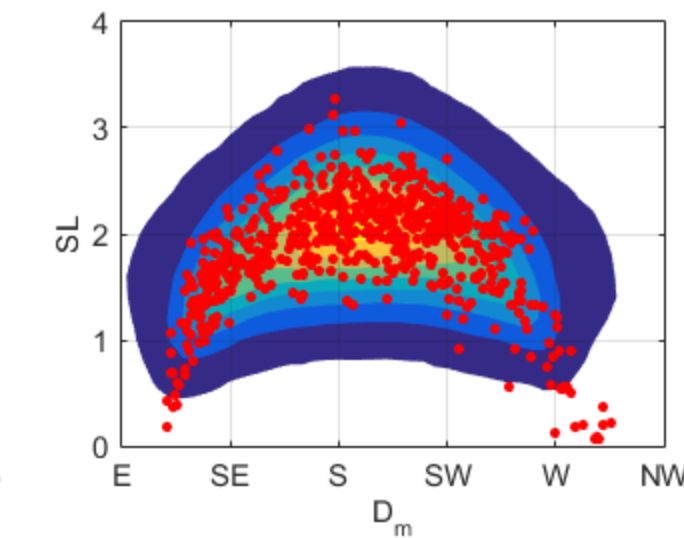
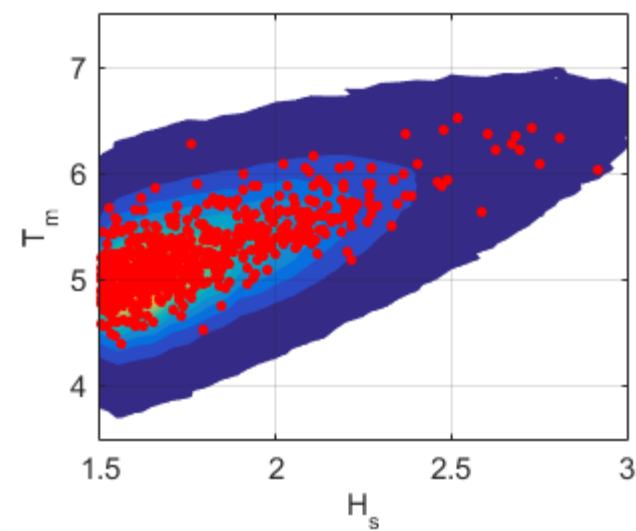
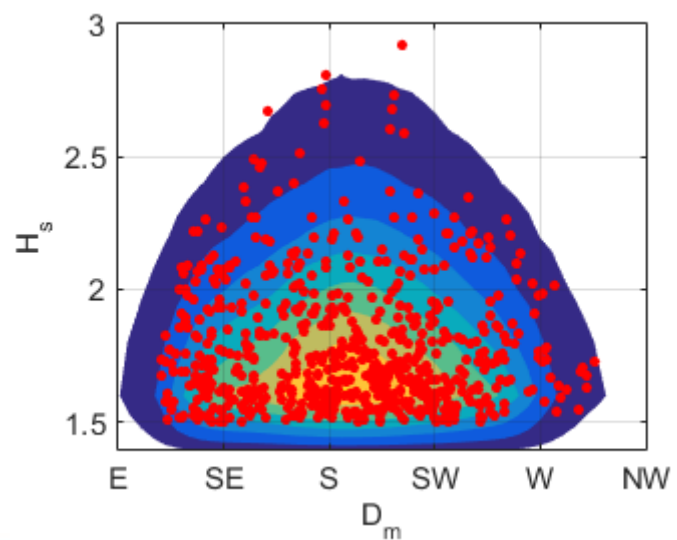
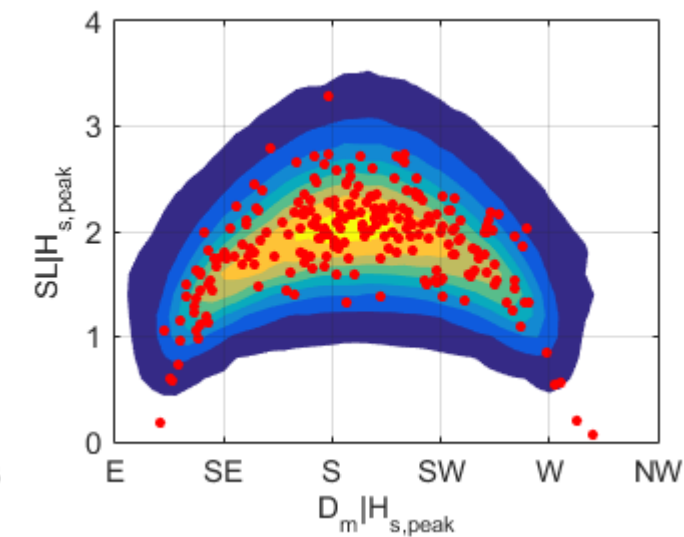
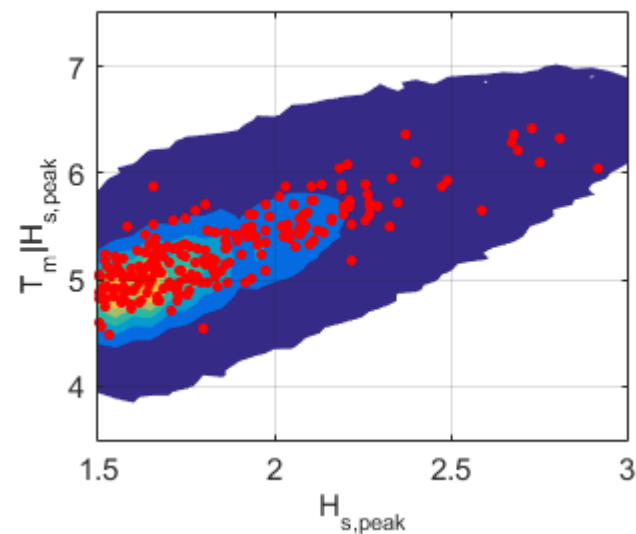
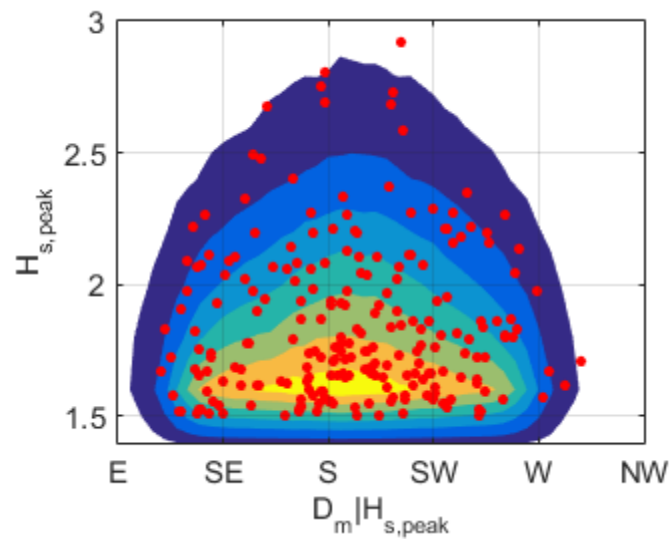
## □ Results and discussion





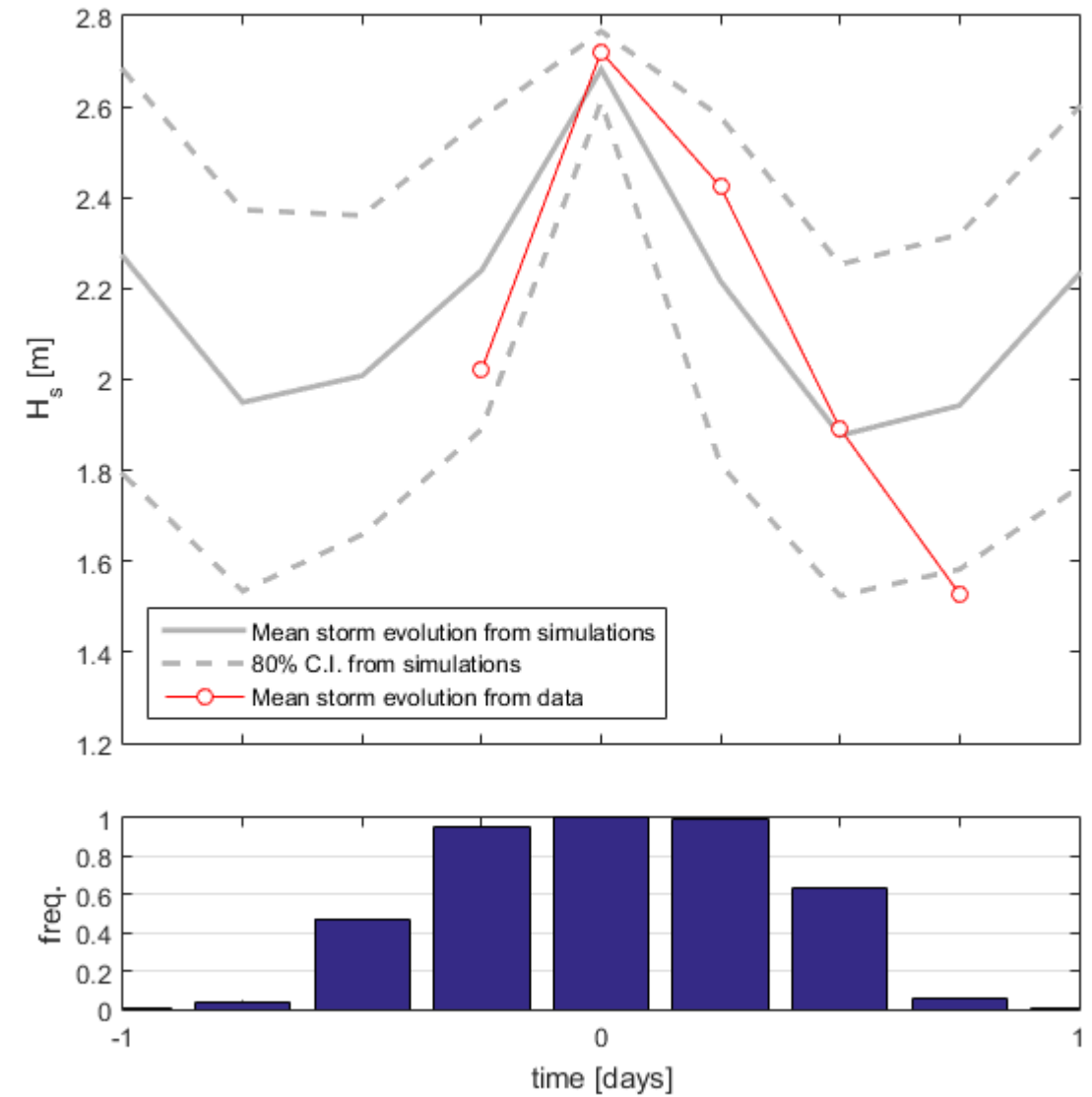
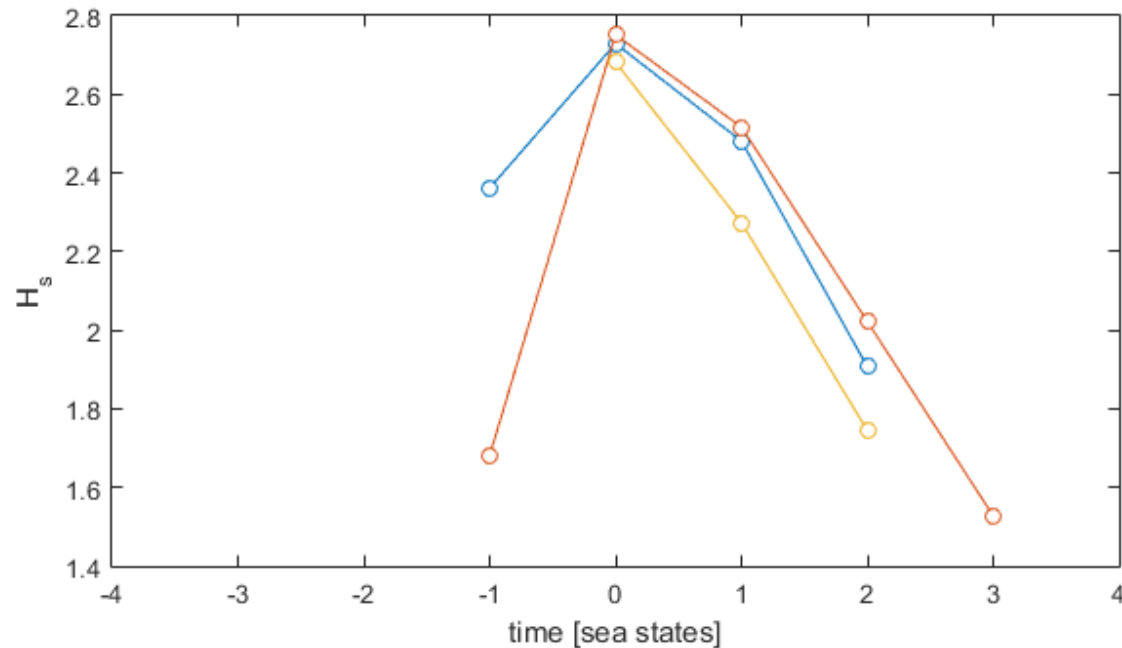
Red Dots: Data

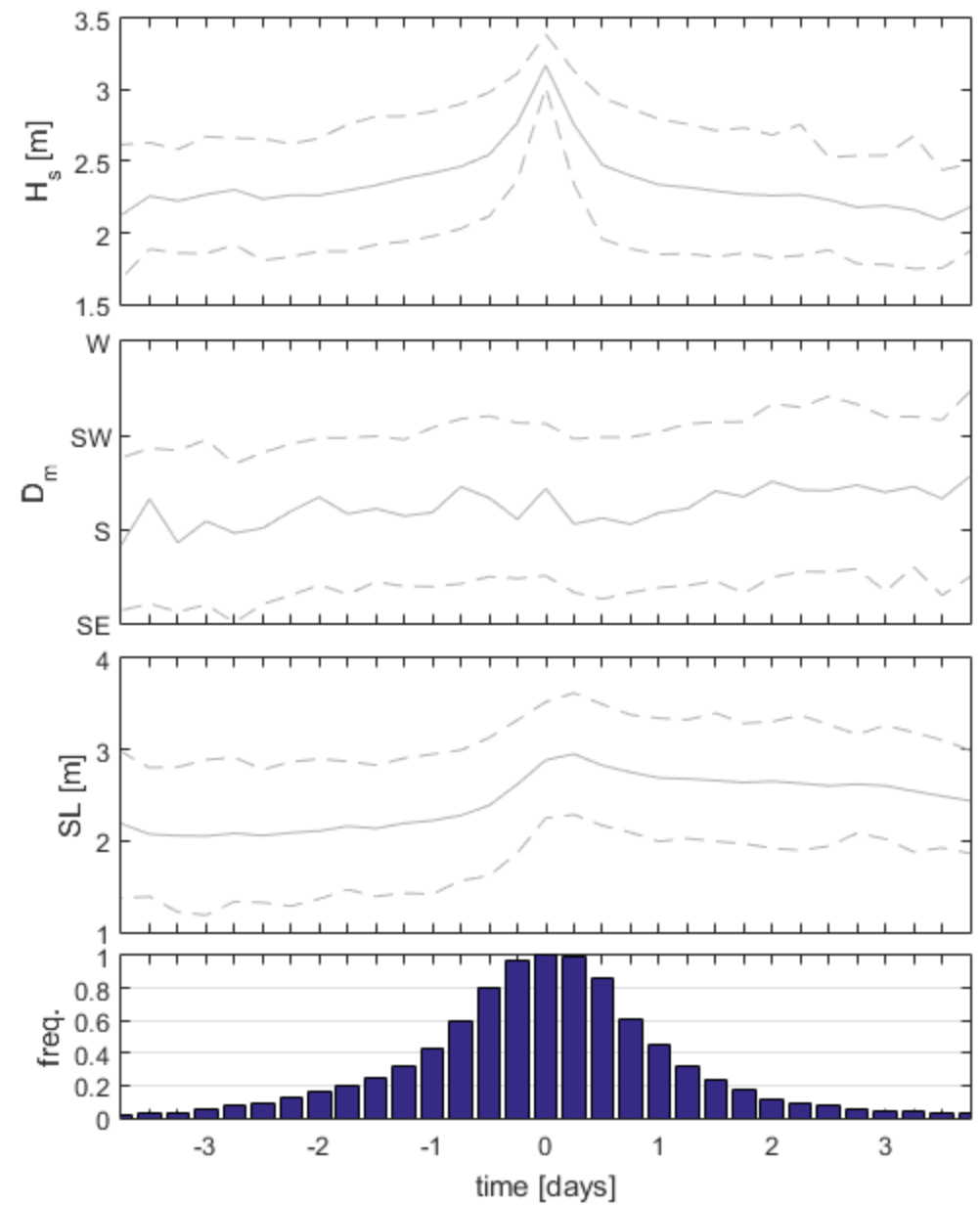
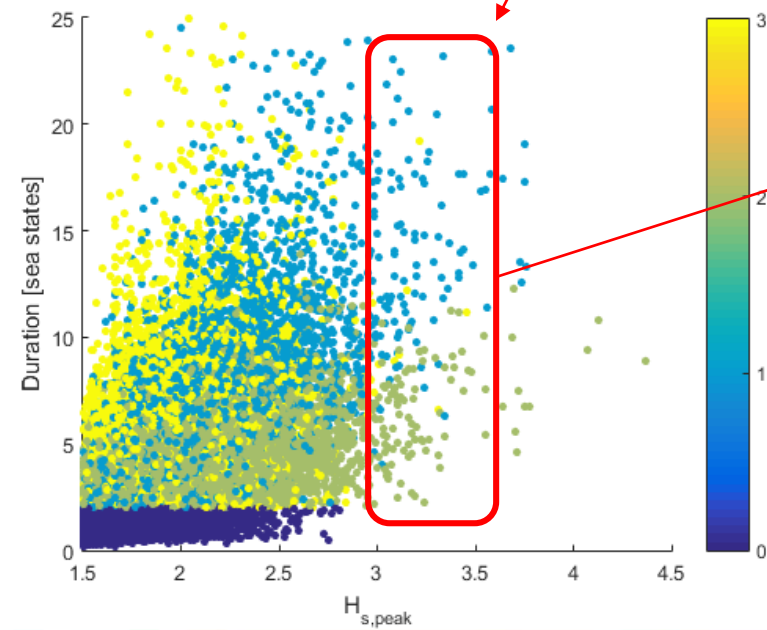
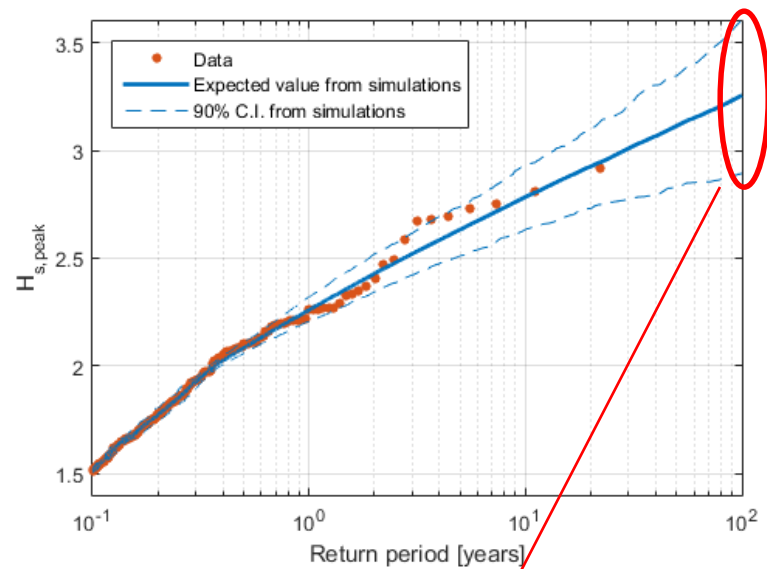
Color Contours: Simulations



## Results and discussion

Data: 3 storms with duration approx. 1,5 days and  $H_{s,peak}$  between 2.6 m and 2.8 m.





## □ Conclusions

- The methodology is able to reproduce marginal and joint distribution of the values occurring simultaneously (all values simulated indirectly).
  - Although some features of the bivariate distributions still missing
  - Simulated storm evolutions mimics observed evolution, and the “innovation” in the storm evolution forms seems reasonable.
- The methodology allows for the simulation of multivariate sea storms that can be used for probabilistic verification and risk analysis including damage evolution of structures (or beaches).

